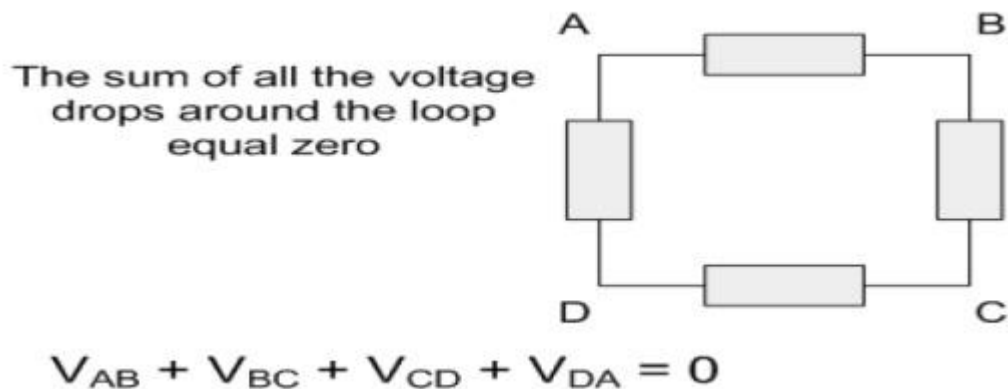


Kirchoff's Second Law - The Voltage Law, (KVL)

"In any closed loop network, the total voltage around the loop is equal to the sum of all the voltage drops within the same loop" which is also equal to zero. In other words the algebraic sum of all voltages within the loop must be equal to zero. This idea by Kirchoff is known as the Conservation of Energy.

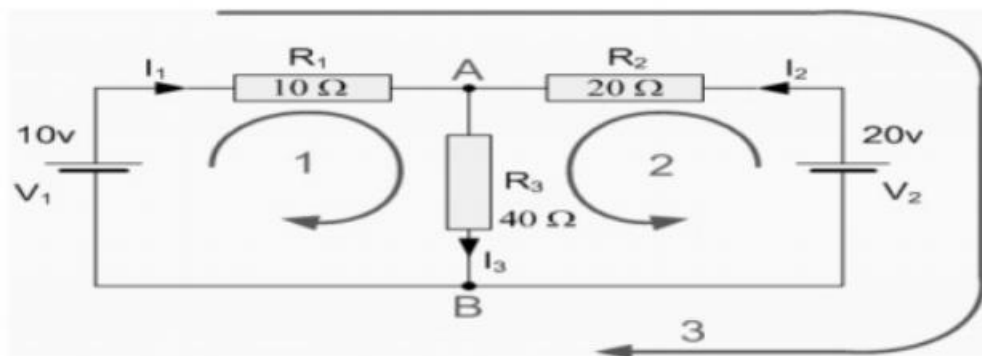
Starting at any point in the loop continue in the same direction noting the direction of all the voltage drops, either positive or negative, and returning back to the same starting point. It is important to maintain the same direction either clockwise or anti-clockwise or the final voltage sum will not be equal to zero.

We can use Kirchoff's voltage law when analyzing series circuits.



Problem: 1

Find the current flowing in the 40Ω Resistor,



Solution:

The circuit has 3 branches, 2 nodes (A and B) and 2 independent loops.

Using Kirchoff's Current Law, KCL the equations are given as;

At node A: $I_1 + I_2 = I_3$

At node B: $I_3 = I_1 + I_2$

Using Kirchoff's Voltage Law, KVL the equations are given as;

Loop 1 is given as: $10 = R_1 \times I_1 + R_3 \times I_3 = 10I_1 + 40I_3$

Loop 2 is given as: $20 = R_2 \times I_2 + R_3 \times I_3 = 20I_2 + 40I_3$

Loop 3 is given as: $10 - 20 = 10I_1 - 20I_2$

As I_3 is the sum of $I_1 + I_2$ we can rewrite the equations as;

Eq. No 1: $10 = 10I_1 + 40(I_1 + I_2) = 50I_1 + 40I_2$

Eq.No 2: $20 = 20I_1 + 40(I_1 + I_2) = 40I_1 + 60I_2$

We now have two "Simultaneous Equations" that can be reduced to give us the value of both I_1 and I_2

Substitution of I_1 in terms of I_2 gives us the value of I_1 as -0.143 Amps

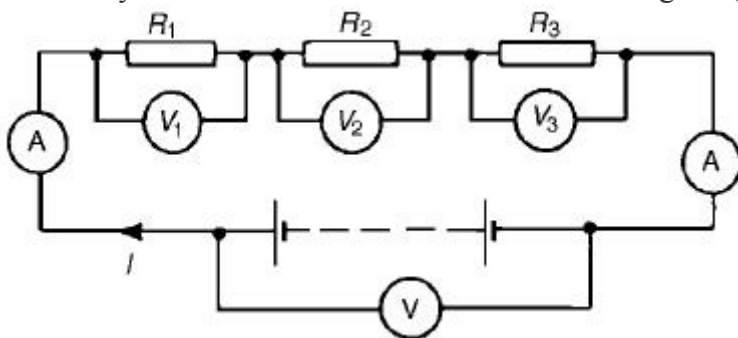
Substitution of I_2 in terms of I_1 gives us the value of I_2 as +0.429 Amps

As: $I_3 = I_1 + I_2$

The current flowing in resistor R_3 is given as: $-0.143 + 0.429 = 0.286$ Amps and the voltage across the resistor R_3 is given as : $0.286 \times 40 = 11.44$ volts

Resistors in series and parallel circuits:**Series circuits:**

Figure shows three resistors R_1 , R_2 and R_3 connected end to end, i.e. in series, with a battery source of V volts. Since the circuit is closed a current I will flow and the p.d. across each resistor may be determined from the voltmeter readings V_1 , V_2 and V_3

**In a series circuit**

(a) the current I is the same in all parts of the circuit and hence the same reading is found on each of the two ammeters shown, and

(b) the sum of the voltages V_1 , V_2 and V_3 is equal to the total applied voltage, V , i.e.

$$V = V_1 + V_2 + V_3$$

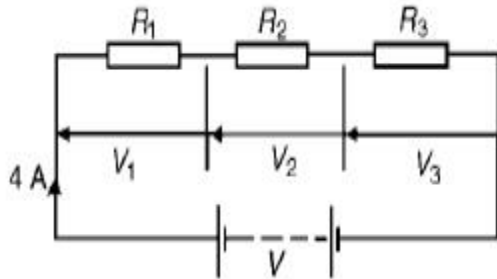
From Ohm's law:

$$V_1 = IR_1, V_2 = IR_2, V_3 = IR_3 \text{ and } V = IR \text{ where } R \text{ is the total circuit resistance. Since } V = V_1 + V_2 + V_3$$

$$\text{then } IR = IR_1 + IR_2 + IR_3 \text{ Dividing throughout by } I \text{ gives } R = R_1 + R_2 + R_3$$

Thus for a series circuit, the total resistance is obtained by adding together the values of the separate resistances.

Problem 1: For the circuit shown in Figure 5.2, determine (a) the battery voltage V , (b) the total resistance of the circuit, and (c) the values of resistance of resistors R_1 , R_2 and R_3 , given that the p.d.'s R_1 , R_2 across and R_3 are 5V, 2V and 6V respectively.



(a) Battery voltage $V = V_1 + V_2 + V_3 = 5 + 2 + 6 = 13V$

(b) Total circuit resistance $R = V / I$
 $= 13 / 4 = 3.25 \Omega$

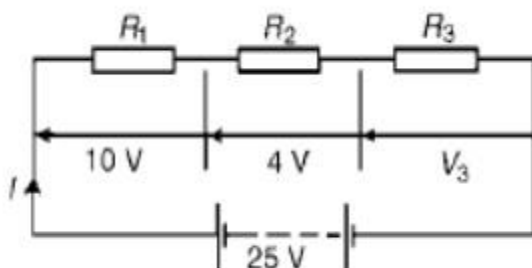
(c) Resistance $R_1 = V_1 / I$
 $= 5 / 4$

$$= 1.25 \Omega \text{ Resistance } R_2 = V_2 / I$$

$$= 2 / 4 = 0.5 \Omega$$

$$\text{Resistance } R_3 = V_3 / I = 6 / 4 = 1.5 \Omega$$

Problem 2. For the circuit shown in Figure determine the p.d. across resistor R_3 . If the total resistance of the circuit is 100Ω , determine the current flowing through resistor R_1 . Find also the value of resistor R_2 .



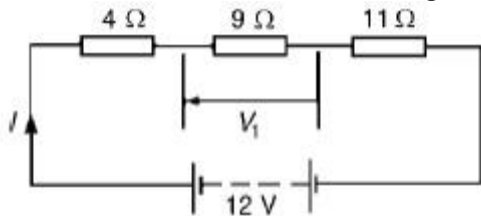
$$\text{P.d. across } R_3, V_3 = 25 - 10 - 4 = 11V \text{ Current } I = V / R$$

$$= 25/100$$

$$= 0.25 \text{ A, which is the current flowing in each resistor Resistance } R_2 = V_2 / I$$

$$= 4 / 0.25 = 16 \Omega$$

Problem 3: A 12V battery is connected in a circuit having three series-connected resistors having resistances of 4 Ω , 9 Ω and 11 Ω . Determine the current flowing through, and the p.d. across the 9 Ω resistor. Find also the power dissipated in the 11 Ω resistor.



Total resistance $R = 4 + 9 + 11 = 24 \Omega$ Current $I = V / R$

$$= 12 / 24$$

$= 0.5 \text{ A, which is the current in the } 9 \Omega \text{ resistor. P.d. across the } 9 \Omega \text{ resistor, } V_1 = I \times 9 = 0.5 \times 9$

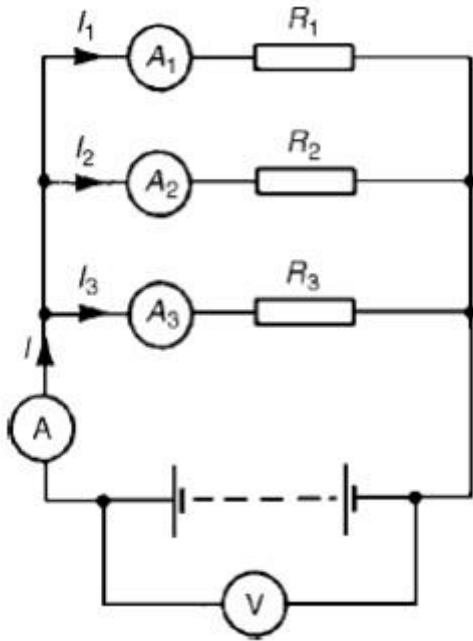
$$= 4.5 \text{ V}$$

Power dissipated in the 11 Ω resistor, $P = I^2 R = 0.5^2 (11)$
 $= 0.25 (11)$
 $= 2.75 \text{ W}$

8. PARALLEL NETWORKS:

Problem 1: Figure shows three resistors, R1, R2 and R3 connected across each other, i.e. in parallel, across a battery source

of V volts.



In a parallel circuit:

(a) the sum of the currents I_1 , I_2 and I_3 is equal to the total circuit current, I , i.e. $I = I_1 + I_2 + I_3$, and

the source p.d., V volts, is the same across each of the

From Ohm's law:

$$I_1 = V/R_1$$

$$, I_2 = V/R_2$$

$$, I_3 = V/R_3 \text{ and } I = V/R$$

where R is the total circuit resistance. Since $I = I_1 + I_2 + I_3$

then

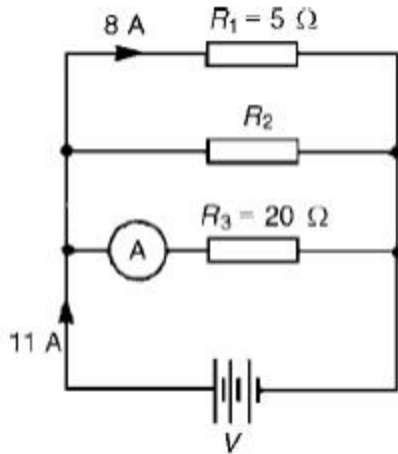
$V/R = V/R_1 + V/R_2 + V/R_3$ Dividing throughout by V gives:

$$\boxed{\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}}$$

This equation must be used when finding the total resistance R of a parallel circuit. For the special case of two resistors in parallel

$$\boxed{R = \frac{R_1 R_2}{R_1 + R_2}}$$

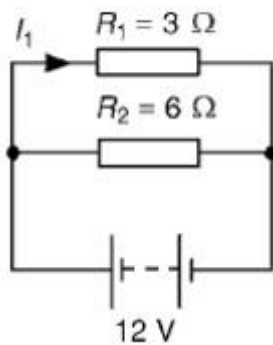
Problem 2: For the circuit shown in Figure , determine (a) the reading on the ammeter, and (b) the value of resistor R_2 .



P.d. across R_1 is the same as the supply voltage V .
Hence supply voltage, $V = 8 \times 5 = 40\text{V}$

(a) Reading on ammeter, $I = \frac{V}{R_3} = \frac{40}{20} = 2\text{A}$

Current flowing through $R_2 = 11 - 8 - 2 = 1\text{A}$
Hence, $R_2 = \frac{V}{I_2} = \frac{40}{1} = 40\ \Omega$

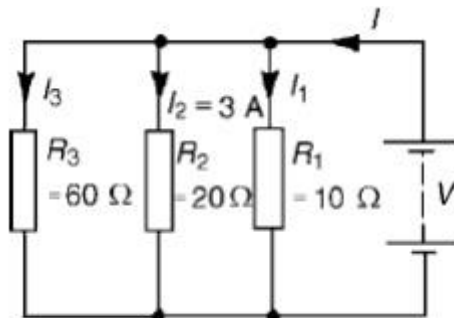


(a) The total circuit resistance R is given by $\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{1}{3} + \frac{1}{6}$

$\frac{1}{R} = \frac{2}{6} + \frac{1}{6} = \frac{3}{6}$ Hence, $R = \frac{6}{3} = 2\ \Omega$

(b) Current in the $3\ \Omega$ resistance, $I_1 = \frac{V}{R_1} = \frac{12}{3} = 4\text{A}$

Problem 3: For the circuit shown in Figure find (a) the value of the supply voltage V and (b) the value of current I .



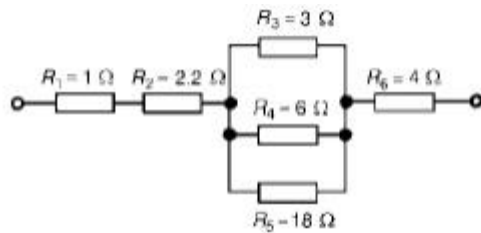
(a) P.d. across $20\ \Omega$ resistor $= I_2 R_2 = 3 \times 20 = 60\text{V}$, hence supply voltage $V = 60\text{V}$ since the circuit is connected in parallel.

(b) Current $I_1 = V/R_1 = 60/10 = 6\text{A}$; $I_2 = 3\text{A}$
 $I_3 = V/R_3 = 60/60 = 1\text{A}$

Current $I = I_1 + I_2 + I_3$ and hence $I = 6 + 3 + 1 = 10\text{A}$ Alternatively,

$1/R = 1/60 + 1/20 + 1/10 = 1 + 3 + 6/60 = 10/60$ Hence total resistance $R = 60/10 = 6\ \Omega$ Current $I = V/R = 60/6 = 10\text{A}$

Problem 4: Find the equivalent resistance for the circuit shown in Figure



R_3 , R_4 and R_5 are connected in parallel and their equivalent resistance R is given by: $1/R = 1/3 + 1/6 + 1/18 = 6 + 3 + 1/18 = 10/18$

Hence $R = 18/10 = 1.8\ \Omega$

The circuit is now equivalent to four resistors in series and the equivalent circuit resistance $= 1 + 2.2 + 1.8 + 4 = 9\ \Omega$