1.9 SIGNALFLOWGRAPH

The diagrammatic or pictorial representation of a set of simultaneous linear algebraic equations of a more complicated system is known as signal flow graph (SFG). It shows the flow of signals in the system. It is important to note that the flow of signals in SFG is only in one direction. To represent these to f algebraic equations using SFG, it is necessary that those algebraic equations are to be represented in the s-domain. The transfer function of the system which is represented by SFG can be obtained by using Mason's gain formula. The dependent and independent variables in the set of algebraic equations are represented by the nodes in the SFG. The branches are used to connect different nodes present in SFG. The connection between the different nodes is based on the relationship given in the algebraic equation. The arrow and the multiplication factor indicated on the branch of SFG represent the signal direction. The SFG and the block diagram representation of a system yield the same transfer function; but when a system is represented by SFG, the transfer function is obtained easily and quickly without using the SFG reduction techniques. The terminologies used in SFG are explained with the help of SFG of a system as shown in figure 1.9.1.

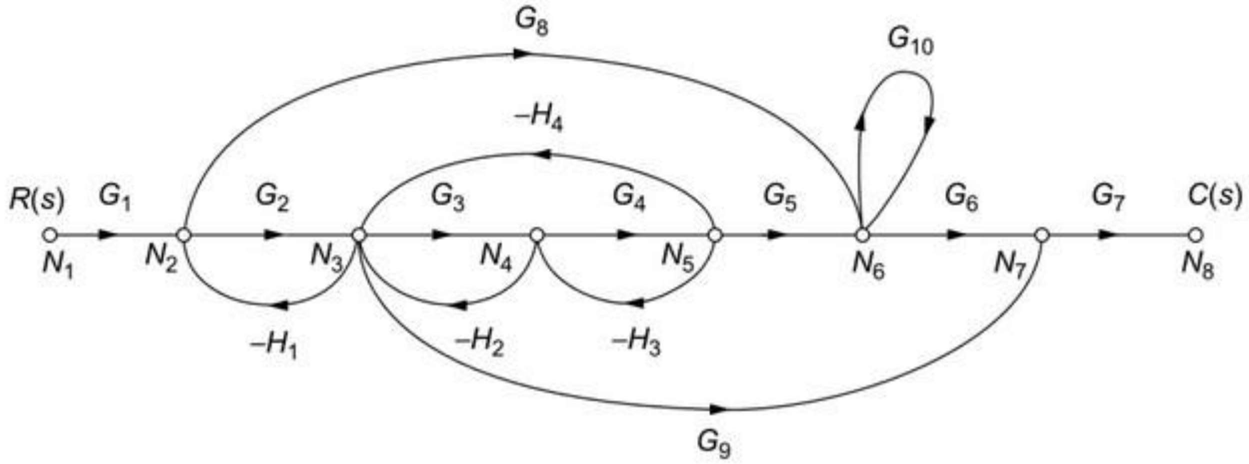

Figure1.9.1 Signal flow graph of a system

Node: The variables present in the set of algebraic equations are represented by a point called node.

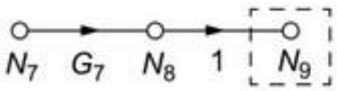

Figure1.9.2 Node in signal flow graph

Branch

The line segment joining the two nodes with a specific direction is known as a branch. The specific direction is indicated by an arrow in the branch.

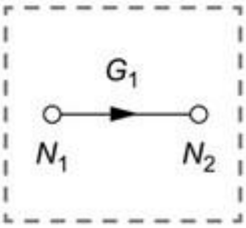

Figure1.9.3 Branch in signal flow graph

MASON'S GAIN FORMULA

A technique to reduce a signal flow graph to a single transfer function requires the application of one formula. The transfer function of a system represented by a signal flow graph is

$$T = \frac{C(s)}{R(s)} = \frac{\sum_{i=1}^{n} P_i \Delta_i}{\Delta}$$

where, k –number of forward path

P_i – ith forward path gain

Δ –1-(sum of individual loop gains)+(sum of product of two non-touching loop gains)-(sum of product of three non-touching loop gains)+……

Δ_i –1-(Δ of the loop non-touching the ith forward path)

Steps to determine the transfer function of a system using SFG Method

Step1: Identify the number of forward paths.

Step2: Identify the individual loops and find their respective loop gains.

Step 3: Identify the two non-touching loops and find the product of their gains.

Step4: Identify the three non-touching loops and find the gain product and soon…

Step 5: Calculate the Δ value.

Step6: Calculate the Δ_i value.

Step7: Use Mason's gain formula to calculate the transfer function value, T.

Characteristics	Block Diagram	Signal flow graph
Time Consumption	More since the diagrams have to be redrawn repeatedly	Less since there is no necessary to redraw the diagrams
Technique applied	Block Diagram reduction technique	Mason's gain formula
Representation of elements	Blocks are used to represent the element.	Nodes are need to represent the elements
Representation of transfer function of each element	Represented inside the block of each element	Represented along the branches above the arrow ahead
Feedback paths	Present and hence the formula, (G/(1±GH)) is used to reduce the paths	Present, but there is no need for any formulae to reduce the paths
Self-loops	Absence of self-loops	Presence of self-loops
Summing points and takeoff points	Present in block diagram	Absence in SFG