### 2.3 LATIN SQUARE:

## Steps in constructing Latin Square

## Step:1

Square the Grand total (T) and divide it by the number of observations (N). i.e), Find $\frac{T^{2}}{N}$ which is called the correction factor (C.F)

## Step:2

Add the squares of the individual observations ( $X_{i}{ }^{\prime} s$ ) and substract the C.F from it to get the total sum of squares. i.e)., Find Total sum of squares TSS

$$
\text { i.e)., } \operatorname{TSS}=\sum_{i}\left(X_{i}\right)^{2}-\frac{T^{2}}{N}
$$

## Step:3

Add the squares of the row sums $\left(R_{i}\right)$ divide it by the number of items in a row and substract the C.F from the result to get the row sum of squares.

Row sum of squares $S S R=\frac{\left(\sum R_{i}\right)^{2}}{n_{1}}-C . F$
Where $n_{1}$ is the number of items in a row.

## Step:4

Add the squares of the columns sums $\left(C_{i}\right)$ divide it by the number of items and substract the C.F from the result to get the column sum of squares.

Column sum of squares $S S C=\frac{\left(\Sigma c_{j}\right)^{2}}{n_{2}}-C . F$
Where $n_{2}$ is the number of items in a column.

## Step:5

Sum of the squares of the treatment sums ( $T_{i}$ ) divide it by the number of treatments and substract the C.F from it to get the treatment sum of squares, i.e., Treatment sum of squares.

$$
S S T=\frac{\left(\sum T_{i}\right)^{2}}{n_{i}}-C . F
$$

Where $n_{i}$ is the number of treatments.
Step: 6

Substract the sum obtained in steps 3,4 , and 5 from 2 we get residual.
i.e)., Residual $S S E=T S S-(S S R+S S C+S S T)$

## Step:7

Prepare the ANOVA table using all these and calculate the various mean squares as follows.

| Source of variation | Sum of Degrees | Degrees of Freedom | Mean Square | F-Ratio |
| :---: | :---: | :---: | :---: | :---: |
| Between Rows | SSR | $\mathrm{n}-1$ | $\mathrm{MSR}=\frac{S S R}{n-1}$ | $F_{R}=\frac{M S R}{M S E}$ if MSR $>$ <br> MSE <br> $F_{R}=\frac{M S E}{M S R}$ if MSE $>$ <br> MSR |
| Between Columns | SSC | $\mathrm{n}-1$ | $\mathrm{MSC}=\frac{S S C}{n-1}$ | $F_{c}=\frac{M S C}{M S E}$ if MSC> <br> MSE <br> $F_{c}=\frac{M S E}{M S C}$ if MSE $>$ <br> MSC |
| Treatments | SST | $\mathrm{n}-1$ | $\mathrm{MST}=\frac{S S T}{n-1}$ | $F_{T}=\frac{M S T}{M S E}$ if MST $>$ <br> MSE <br> $F_{T}=\frac{M S E}{M S T}$ if MSE $>$ <br> MST |
| Residual or Error | SSE | $(\mathrm{n}-1)(\mathrm{n}-2)$ | $\begin{aligned} & \mathrm{MSE}= \\ & \frac{S S E}{(\mathrm{n}-1)(\mathrm{n}-2)} \end{aligned}$ |  |

## Step:8

Compute the F-ratio and find out whether the differences are significant or not according to the given level of significance.

1. Set up the analysis of variance for the following results of a Latin square design.

| A | C | B | D |
| :---: | :---: | :---: | :---: |
| 12 | 19 | 10 | 8 |
| $\mathbf{C}$ | B | D | A |
| 18 | 12 | $\mathbf{6}$ | 7 |
| B | D | A | C |
| 22 | 10 | 5 | 21 |
| $\mathbf{C}$ | A | C | B |
| 12 | 7 | 27 | 17 |

Solution:
Set the null hypothesis $H_{0}$ : There is no significance difference between the rows, columns and treatments.

Table I (To find TSS, SSR and SSC)

|  | $C_{1}$ | $C_{2}$ | $C_{3}$ | $C_{4}$ | Row <br> Total <br> $R_{i}$ | $R_{i}{ }^{2} / 4$ |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| $R_{1}$ | 12 | 19 | 10 | 8 | 49 | 600.25 |
| $R_{2}$ | 18 | 12 | 6 | 7 | 43 | 462.25 |
| $R_{3}$ | 22 | 10 | 5 | 21 | 58 | 841 |
| $R_{4}$ | 12 | 7 | 27 | 17 | 63 | 992.25 |
| Column <br> Total <br> $C_{j}$ | 64 | 48 | 48 | 53 | $213(\mathrm{~T})$ | 2895.75 |
| $C_{j}{ }^{2} / 4$ | 1024 | 576 | 576 | 702.25 | 2895.75 |  |
| $R_{4}{ }^{2} / 4$ |  |  |  |  |  |  |

Table II (To find SST)

|  | 1 | 2 | 3 | 4 | Row <br> Total $T_{i}$ | $T_{i}{ }^{2} / 4$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## Step:1

## Grand total ( $\mathbf{T}$ ) $=\mathbf{2 1 3}$

## Step: 2

Correction factor (C.F) $=\frac{T^{2}}{N}=\frac{(213)^{2}}{16}=2835.56$
Step:3
Sum of squares of individual observations

$$
\begin{aligned}
= & (12)^{2}+(7)^{2}+(5)^{2}+(7)^{2}+(10)^{2}+(12)^{2}+(22)^{2}+(17)^{2}+ \\
& (19)^{2}+(18)^{2}+(21)^{2}+(27)^{2}+(8)^{2}+(6)^{2}+(10)^{2}+(12)^{2}
\end{aligned}
$$

$$
=3483
$$

## Step:4

TSS =sum of squares of individual observations - C.F

$$
=\sum_{i}\left(X_{i}\right)^{2}-\frac{T^{2}}{N}=3486-2835.56=647.44
$$

## Step:5

Row sum of squares

$$
S S R=\frac{\left(\sum R_{i}\right)^{2}}{4}-C . F=2895.75-2835.56=60.19
$$

## Step:6

Column sum of squares $S S C=\frac{\left(\Sigma C_{j}\right)^{2}}{4}-C . F=2878.25-2835.56$

$$
=42.69
$$

## Step:7

Sum of squares of Treatment

$$
S S T=\frac{\left(\sum T_{i}\right)^{2}}{n_{i}}-C . F=3300.75-2835.56=465.19
$$

## Step:8

$$
\begin{aligned}
\text { Residual } S S E & =T S S-(S S R+S S C+S S T) \\
& =647.44-(60.19+42.69+465.19)=79.37
\end{aligned}
$$

## Step:9

Prepare the ANOVA table using all these and calculate the various mean squares as follows.

| Source of <br> variation | Sum of <br> Degrees | Degrees of <br> Freedom | Mean Square | F - Ratio |
| :--- | :--- | :--- | :--- | :--- |


| Between <br> Rows | $\mathrm{SSR}=60.19$ | $4-1=3$ | $\mathrm{MSR}=\frac{S S R}{n-1}$ <br> $=20.06$ | $F_{R}=\frac{M S R}{M S E}=1.52$ |
| :--- | :--- | :--- | :--- | :--- |
| Between <br> Columns | $\mathrm{SSC}=42.69$ | $4-1=3$ | $\mathrm{MSC}=\frac{S S C}{n-1}$ <br> $=14.23$ | $F_{C}=\frac{M S C}{M S E}=1.08$ |
| Treatments | $\mathrm{SST}=465.19$ | $4-1=3$ | $\mathrm{MST}=\frac{S S T}{n-1}$ <br> $=155.06$ | $F_{T}=\frac{M S T}{M S E}=11.73$ |
| Residual or <br> Error | $\mathrm{SSE}=79.37$ | $(4-1)(4-2)$ <br> $=6$ | $\mathrm{MSE}=$ <br> $\frac{S S E}{}$ |  |

## Step: 10

d.f for $(3,6)$ at $5 \%$ level of significance is 4.76

Step: 11 Conclusion:
Calculated value $F_{c}<$ Table value, then we accept null hypothesis.
There is no significance difference between the columns.
Calculated value $F_{R}<$ Table value, then we accept null hypothesis.
There is no significance difference between the rows.
Calculated value $F_{T}>$ Table value, then we reject null hypothesis.
There is a significance difference between the rows.

