

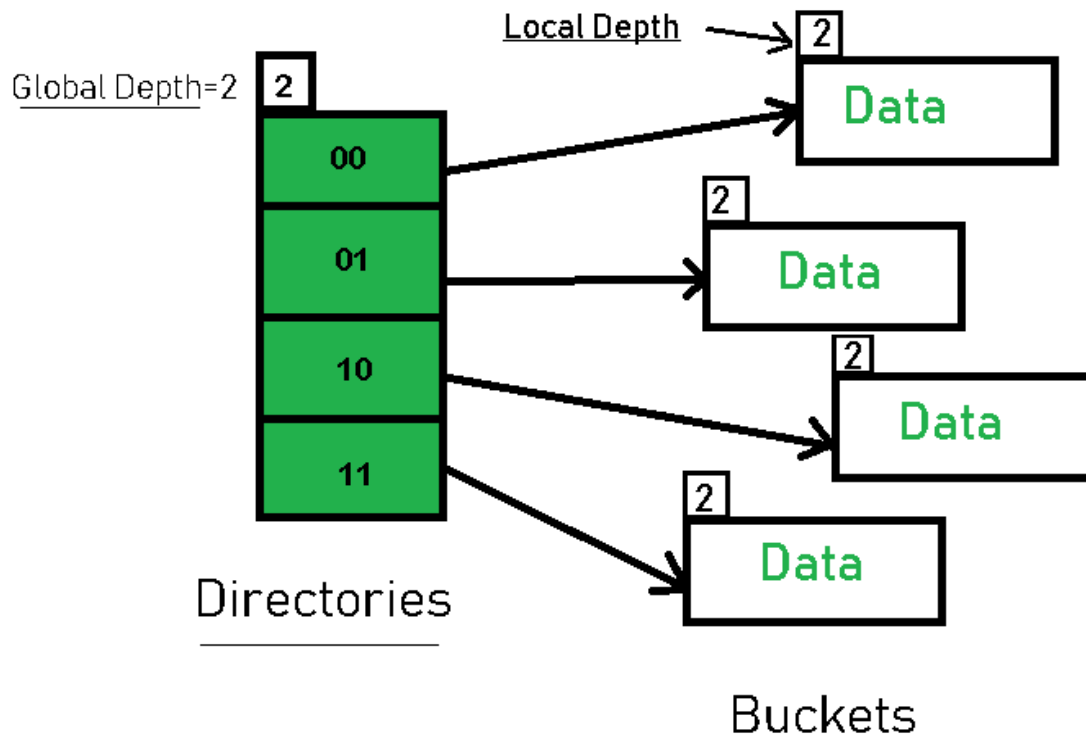
EXTENDIBLE HASHING

It is a dynamic hashing method.

The main terms in hashing technique are:

- **Directories:** These containers store pointers to buckets. Each directory is given a unique id which may change each time when expansion takes place. The hash function returns this directory id which is used to navigate to the appropriate bucket. Number of Directories = $2^{\text{Global Depth}}$.
- **Buckets:** They store the hashed keys. Directories point to buckets. A bucket may contain more than one pointer to it if its local depth is less than the global depth.
- **Global Depth:** It is associated with the Directories. They denote the number of bits which are used by the hash function to categorize the keys. Global Depth = Number of bits in directory id.
- **Local Depth:** It is the same as that of Global Depth except for the fact that Local Depth is associated with the buckets and not the directories. Local depth in accordance with the global depth is used to decide the action that to be performed in case an overflow occurs. Local Depth is always less than or equal to the Global Depth.
- **Bucket Splitting:** When the number of elements in a bucket exceeds a particular size, then the bucket is split into two parts.
- **Directory Expansion:** Directory Expansion Takes place when a bucket overflows. Directory Expansion is performed when the local depth of the overflowing bucket is equal to the global depth

The basic structure of extendible hashing



Extendible Hashing

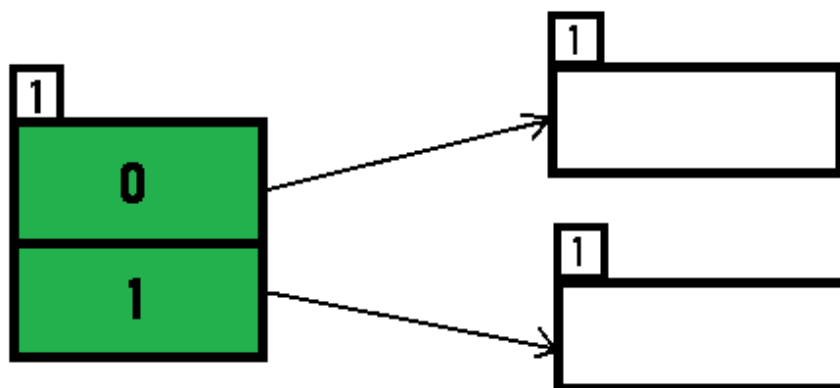
Example

Now, let us consider a example of hashing the following elements: **16,4,6,22,24,10,31,7,9,20,26.**

Bucket Size: 3 (Assume)

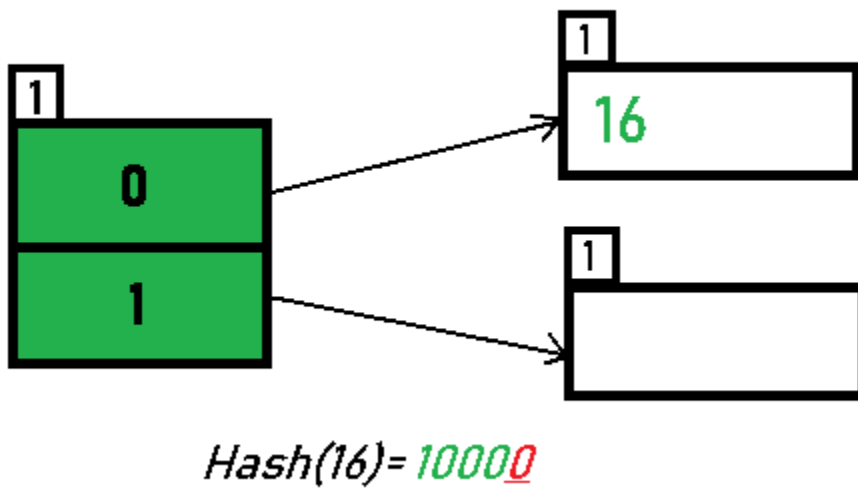
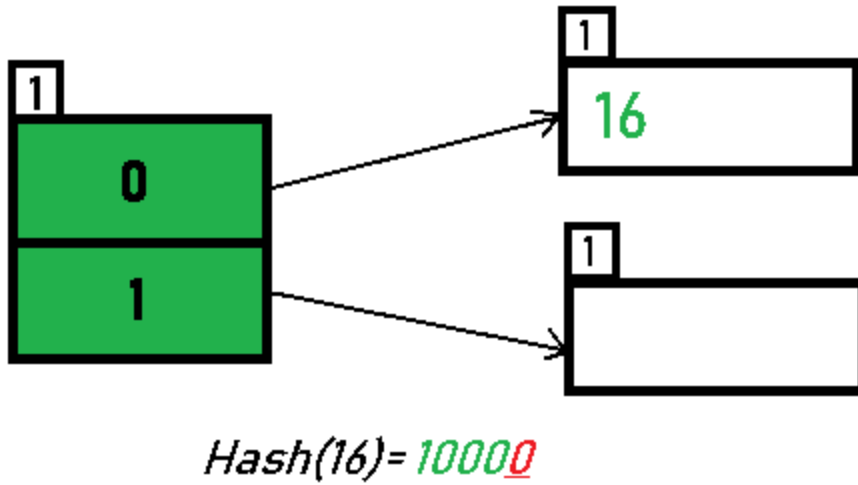
Hash Function: Suppose the global depth is X. Then the Hash Function returns X LSBs.

- **Solution:** First, calculate the binary forms of each of the given numbers.
 16- 10000
 4- 00100
 6- 00110
 22- 10110
 24- 11000
 10- 01010
 31- 11111
 7- 00111
 9- 01001
 20- 10100
 26- 11010
- Initially, the global-depth and local-depth is always 1. Thus, the hashing frame looks like this:

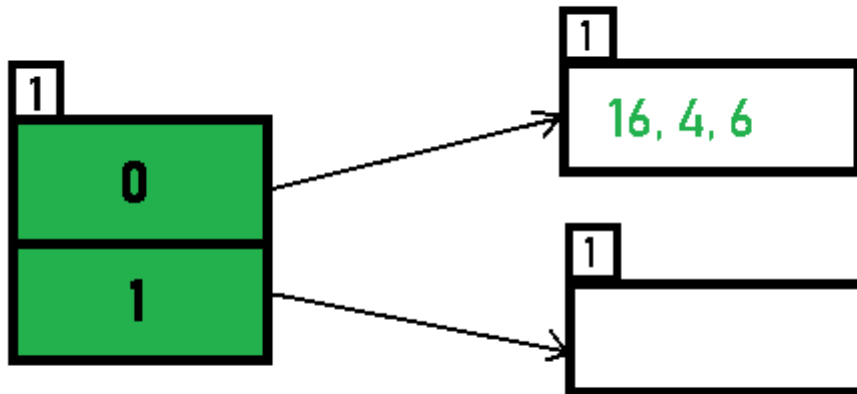


- **Inserting 16:**
 The binary format of 16 is 10000 and global-depth is 1. The hash function returns 1 LSB of 10000 which is 0. Hence, 16 is mapped to the

directory with id=0.



- **Inserting 4 and 6:**
Both 4(100) and 6(110) have 0 in their LSB. Hence, they are hashed as follows:

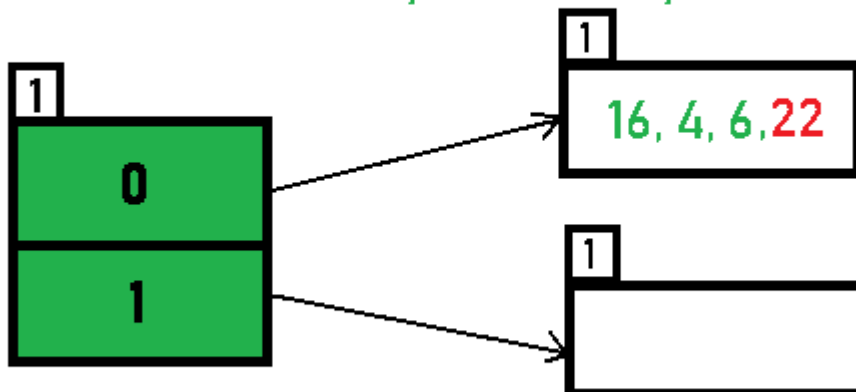


$Hash(4) = 100$
 $Hash(6) = 110$

- **Inserting 22:** The binary form of 22 is 10110. Its LSB is 0. The bucket pointed by directory 0 is already full. Hence, Over Flow occurs.

OverFlow Condition

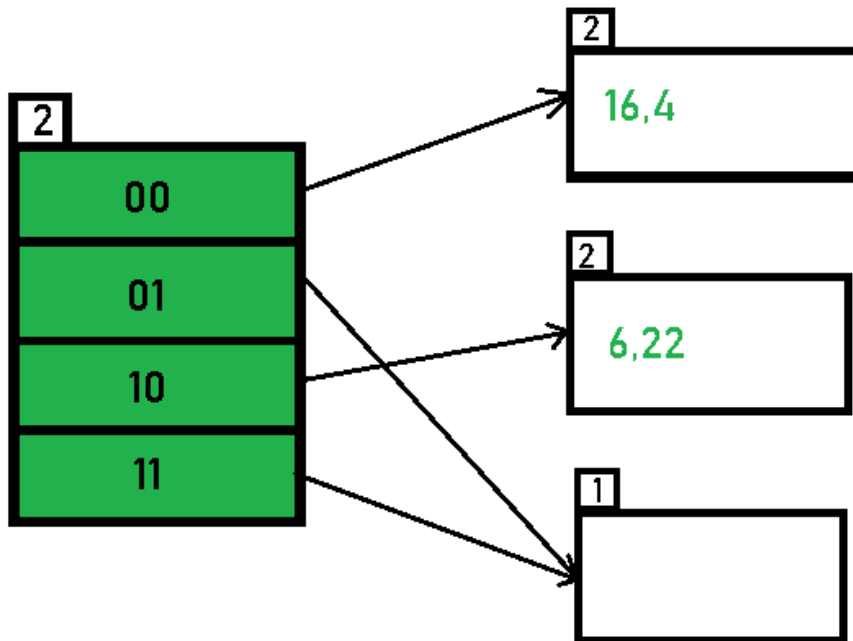
Here, Local Depth = Global Depth



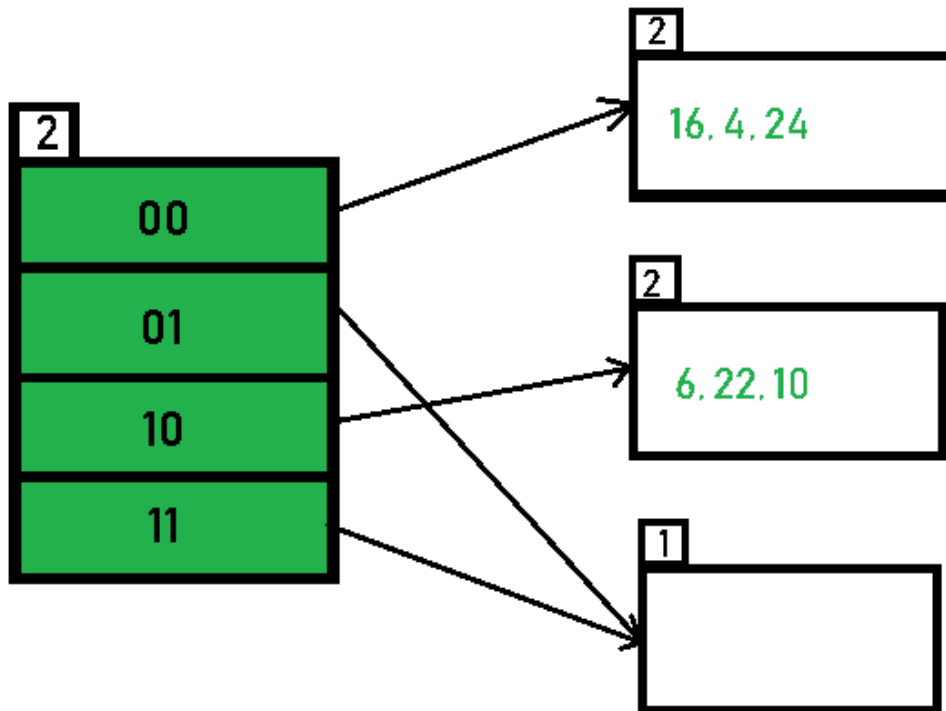
$Hash(22) = 10110$

- Since Local Depth = Global Depth, the bucket splits and directory expansion takes place. Also, rehashing of numbers present in the overflowing bucket takes place after the split. And, since the global depth is incremented by 1, now, the global depth is 2. Hence, 16,4,6,22 are now rehashed w.r.t 2 LSBs. [16(10000),4(100),6(110),22(10110)]

After Bucket Split and Directory Expansion



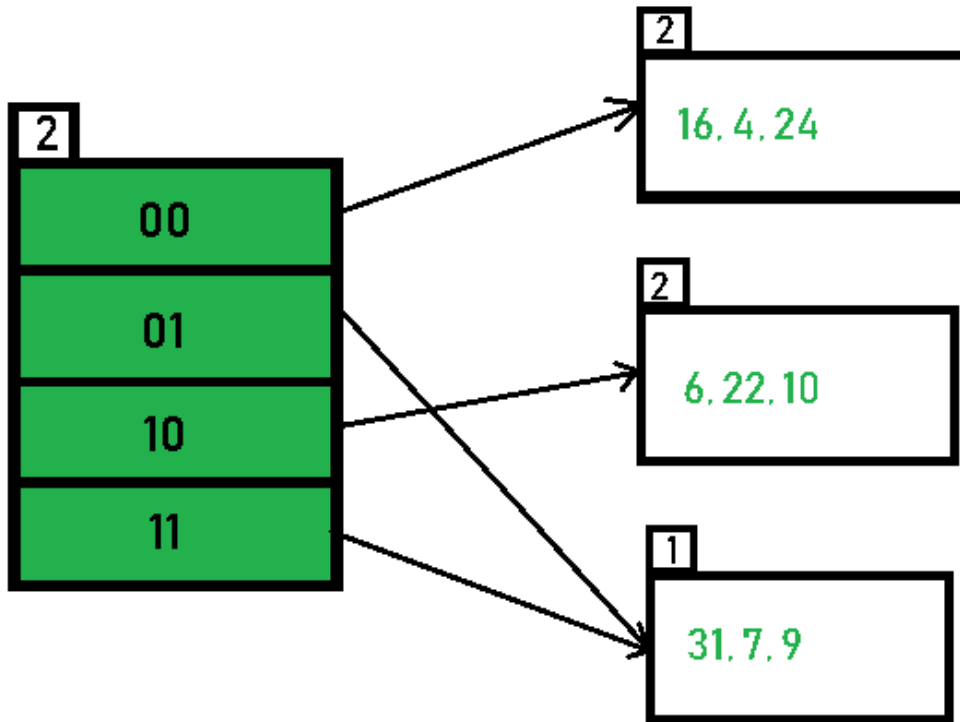
Inserting 24 and 10: 24(11000) and 10 (1010) can be hashed based on directories with id 00 and 10. Here, we encounter no overflow condition.



$Hash(24) = 11000$

$Hash(10) = 1010$

- **Inserting 31,7,9:** All of these elements [31(11111), 7(111), 9(1001)] have either 01 or 11 in their LSBs. Hence, they are mapped on the bucket pointed out by 01 and 11. We do not encounter any overflow condition here.



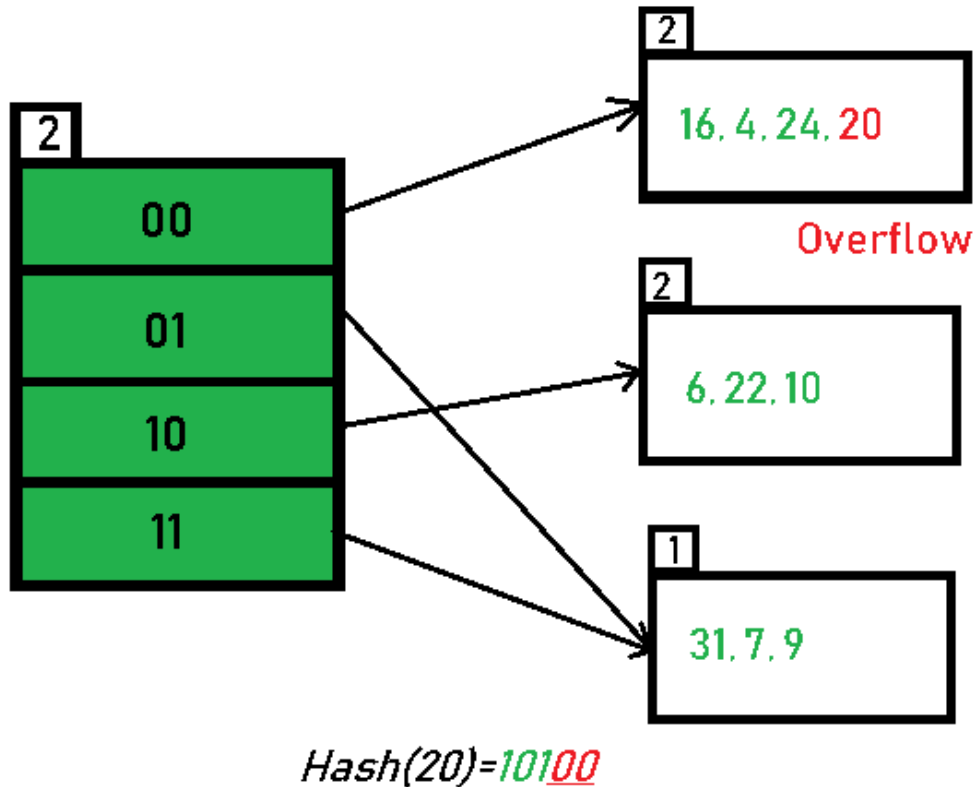
Hash(31) = 11111

Hash(7) = 111

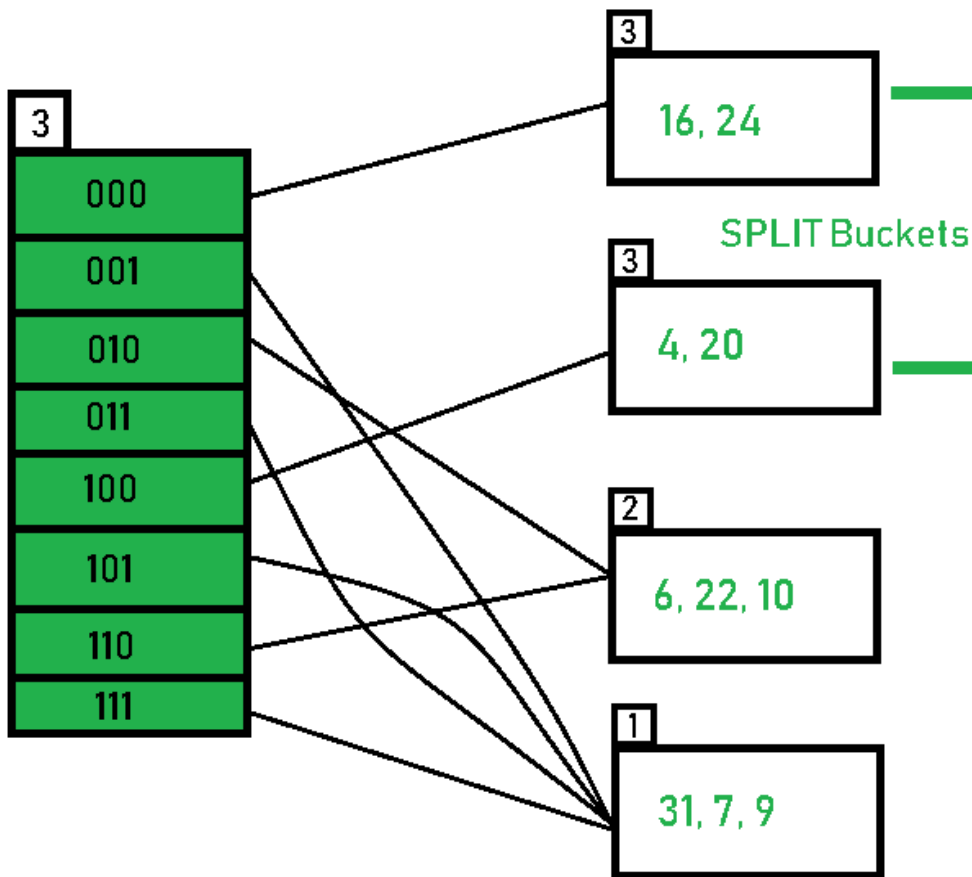
Hash(9) = 1001

- **Inserting 20:** Insertion of data element 20 (10100) will again cause the overflow problem.

OverFlow, Local Depth=Global Depth



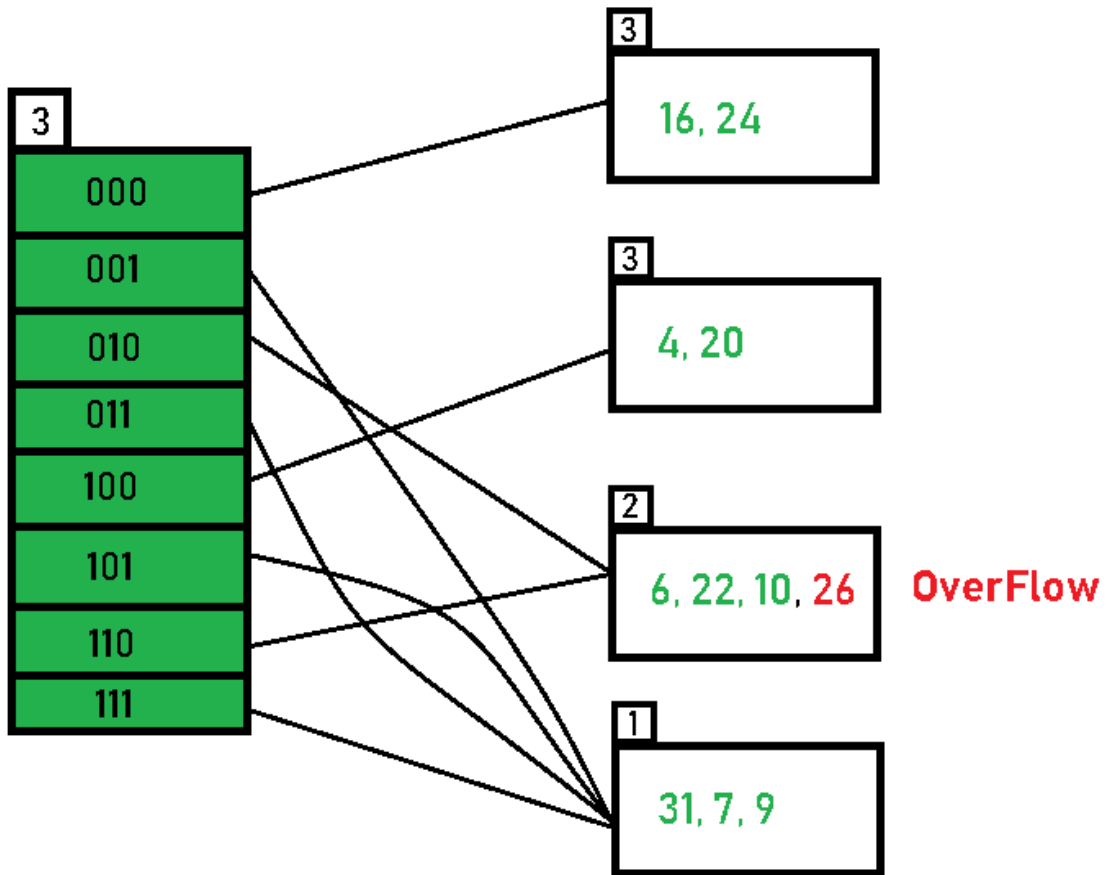
- 20 is inserted in bucket pointed out by 00. Since the **local depth of the bucket = global-depth**, directory expansion (doubling) takes place along with bucket splitting. Elements present in overflowing bucket are rehashed with the new global depth. Now, the new Hash table looks like this:



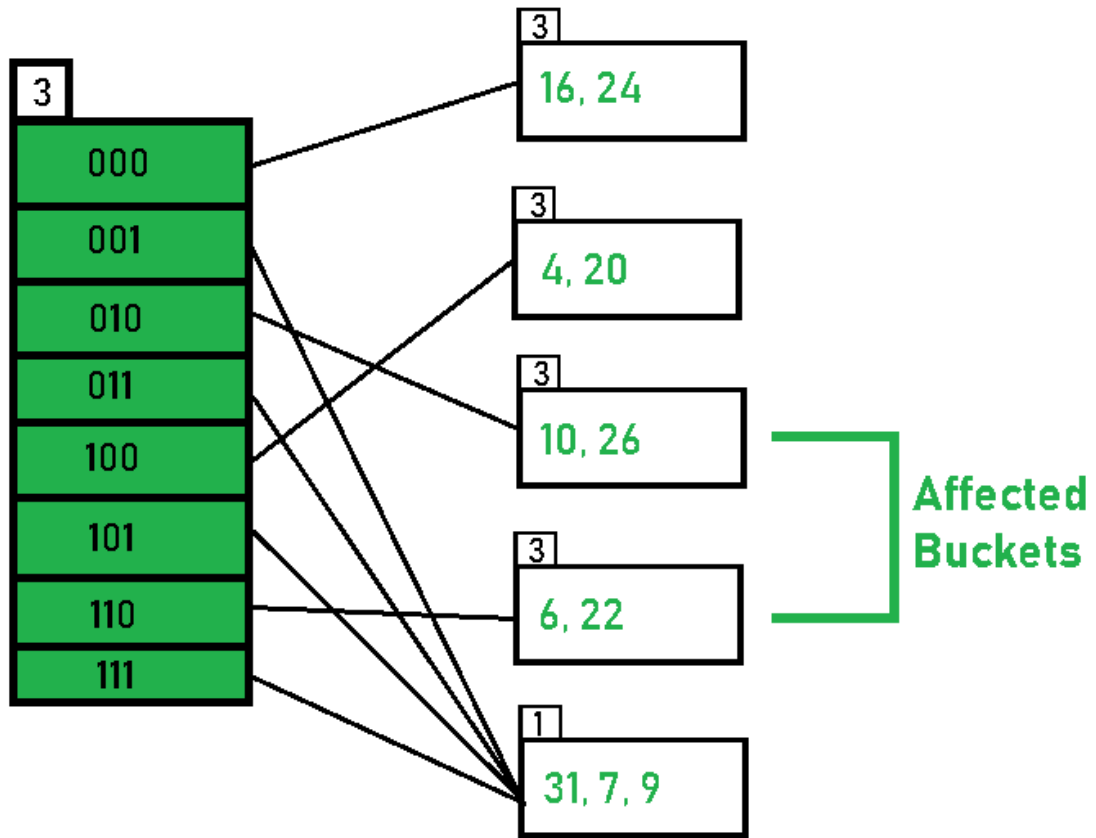
- **Inserting 26:** Global depth is 3. Hence, 3 LSBs of 26(11010) are considered. Therefore 26 best fits in the bucket pointed out by directory 010.

$Hash(26) = 11010$

Overflow, Local Depth < Global Depth



- The bucket overflows, and, since the **local depth of bucket < Global depth (2 < 3)**, directories are not doubled but, only the bucket is split and elements are rehashed.
Finally, the output of hashing the given list of numbers is obtained.



- Hashing of 11 Numbers is thus Completed.