

### 3.1 Power in the Wind:

Wind has kinetic energy due to its motion. This kinetic energy can be given by

$$KE = \frac{1}{2} \dot{m} u_0^2$$

$$\dot{m} = \frac{dm}{dt}$$

Where,

$\dot{m}$  = mass of air passing through an area A per unit time

If  $u_0$  is the speed of free wind in unperturbed state,

the volume of air column passing through an area A per unit time is given by  $Au_0$ .

If  $\rho$  is the density of air,

the air mass flow rate, through area A, is given as,  $\rho Au_0$

Power ( $P_0$ ) available in wind, is equal to kinetic energy rate associated with the mass of moving air,

i.e.:

$$P_0 = \frac{1}{2} (\rho Au_0) u_0^2$$

(Or)

$$P_0 = \frac{1}{2} (\rho A) u_0^3$$

Power available in wind per unit area:

$$\frac{P_0}{A} = \frac{1}{2} (\rho) u_0^3$$

This indicates that power available in wind is proportional to the cube of wind speed.

The air density  $\rho$  varies in direct proportion with air pressure and inverse proportion with temperature as:

$$\rho = \frac{P}{RT}$$

Where,

**P** is air pressure in Pa,

**T** is air temperature in kelvin and

**R** is the gas constant, (= 287 J/kg K).

At the standard value of air pressure,  $1.0132 \times 10^5$  Pa (i.e. 1 atmosphere), and at  $15^\circ\text{C}$ , the value of air density

$$\rho = \frac{1.0132 \times 10^5}{287 \times 288} = 1.226 \frac{\text{J}}{\text{Kg}} \text{K/m}^3$$

Assuming the above value of wind density,  $\rho$  at  $15^\circ\text{C}$  and at sea level, the power available in moderate wind of 10 m/s is 613 W/m<sup>2</sup>.