

**3.5 SINGLE STUB MATCHING USING SMITH CHART:****PROBLEM 1:**

A 30m long lossless transmission line with  $Z_0 = 50$  ohm operating at 2 MHz is terminated with a load  $Z_L = 60 + j40$  ohm. If  $v = 0.6c$  on the line, find Reflection coefficient, the standing wave ratio and the input impedance.

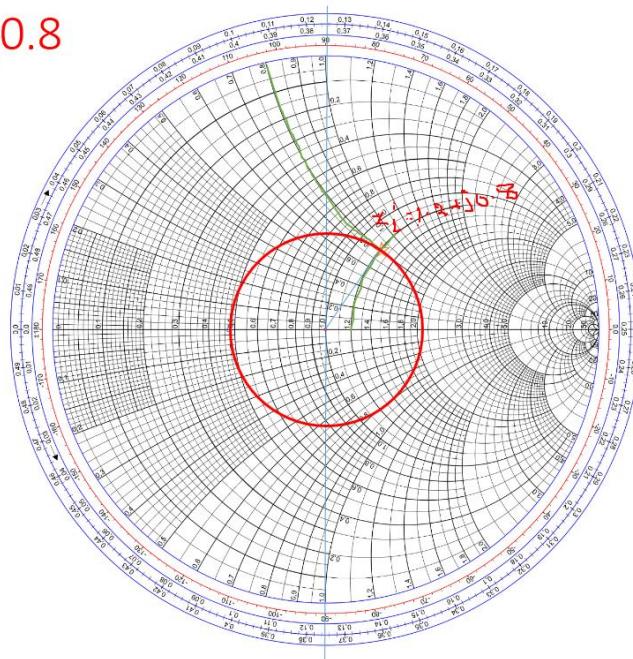
**STEP 1:**

- To find The normalized load impedance is
- $Z_L' = \frac{Z_L}{Z_0}$
- $Z_L' = \frac{60 + j40}{50}$
- $Z_L' = 1.2 + j0.8$

**STEP 2:**

- Fig 3.5.1, draw the normalized load impedance in smith chart

$$z_L' = 1.2 + j0.8$$

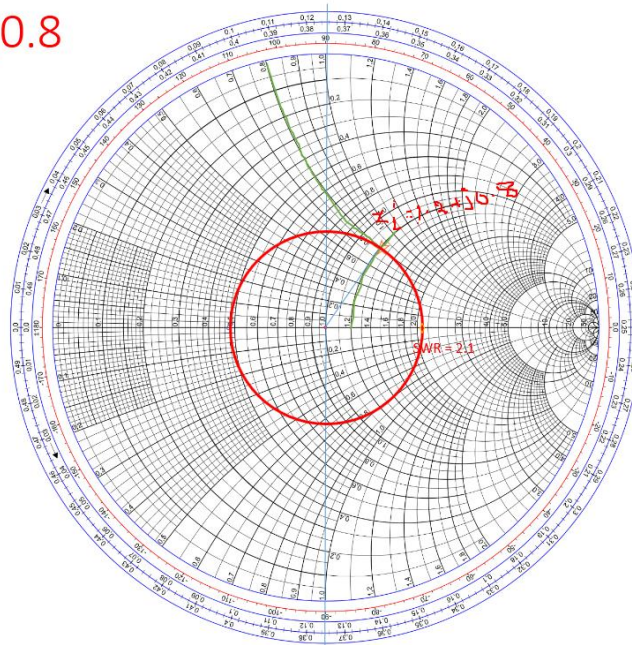


**Fig: 3.5.1 Normalized load impedance**

**STEP 3:**

- Fig 3.5.2, mark the value of Standing Wave Ratio in smith chart

$$z'_L = 1.2 + j0.8$$

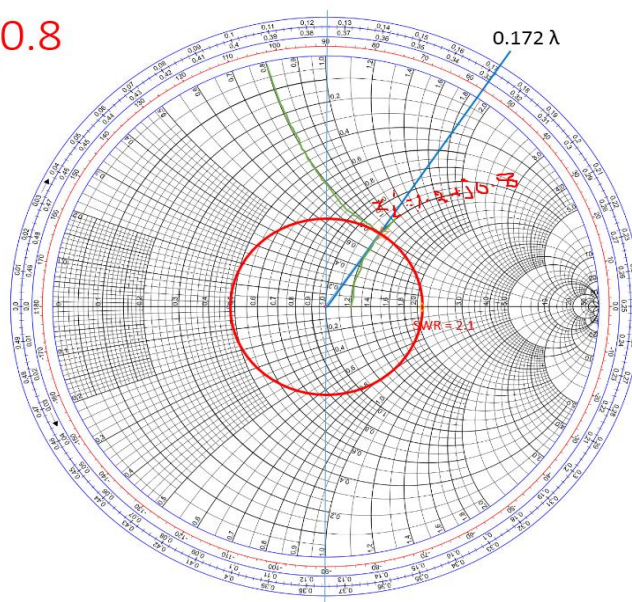


**Fig 3.5.2 Standing Wave Ratio**

**STEP 4:**

- Fig 3.5.3, mark the wavelength in smith chart

$$z'_L = 1.2 + j0.8$$



**Fig: 3.5.3 wavelength**

**STEP 5:**

- Calculate the velocity and wavelength using 30m long transmission line

$$v = 0.6c$$

$$= 0.6 \times 3 \times 10^8$$

$$= 1.8 \times 10^8$$

$$\lambda = \frac{v}{f}$$

$$\lambda = \frac{1.8 \times 10^8}{2 \times 10^6}$$

$$\lambda = 90\text{m}$$

$$L = 30\text{m}$$

$$1\text{ m} = 30 \times \frac{\lambda}{90}$$

$$L = \frac{\lambda}{3}$$

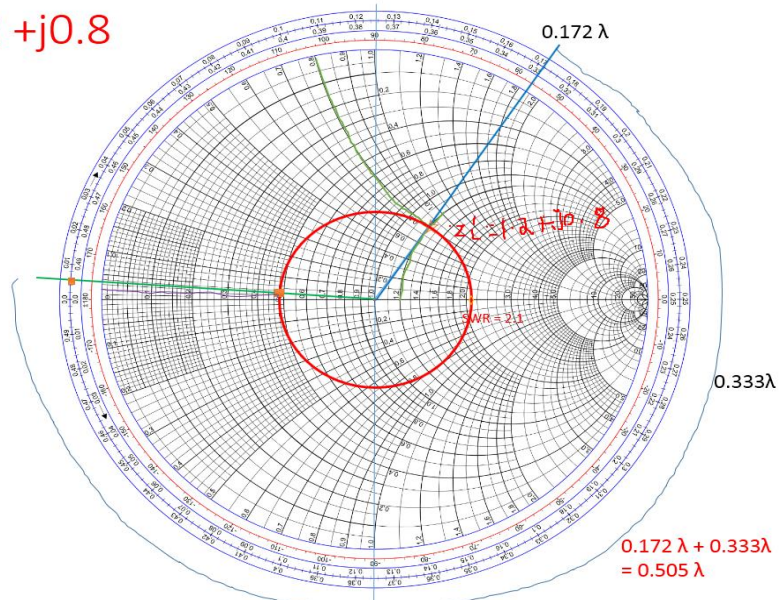
$$L = 0.333 \lambda$$

**STEP 6:**

- Fig 3.5.4, draw the new wavelength in smith chart



$$z_L' = 1.2 + j0.8$$



**Fig: 3.5.4 new wavelength**

**STEP 7:**

**Fig 3.5.5, calculate the normalized input impedance and mark the  $Z_{in}$  in smith chart**

$$Z_{in} = Z_{in}' Z_0$$

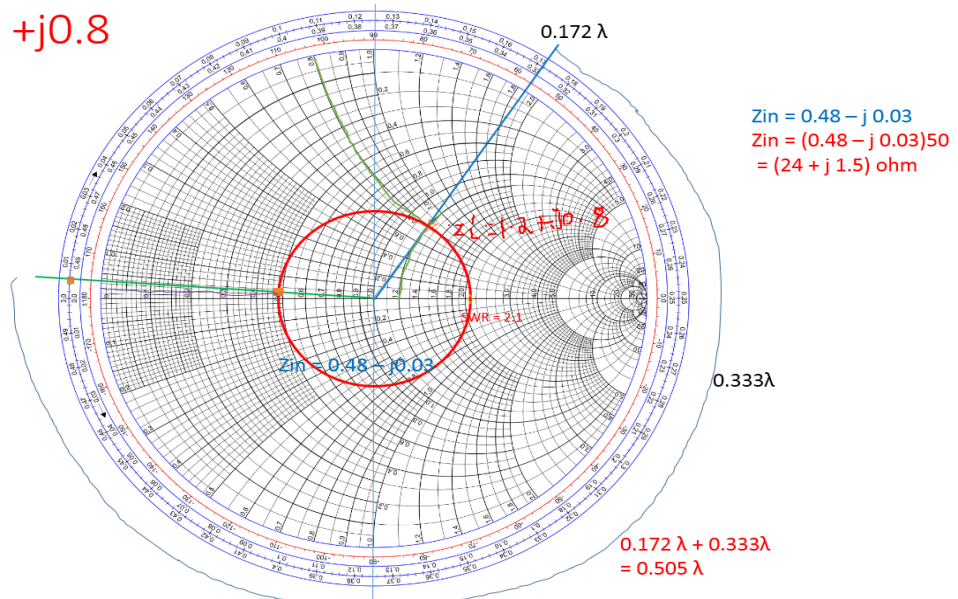
$$Z_{in}' = 0.48 - 0.03$$

$$Z_{in} = (0.48 - j0.03) 50$$

$$Z_{in} = 24 + j1.5 \text{ ohm}$$



$$z_L' = 1.2 + j0.8$$



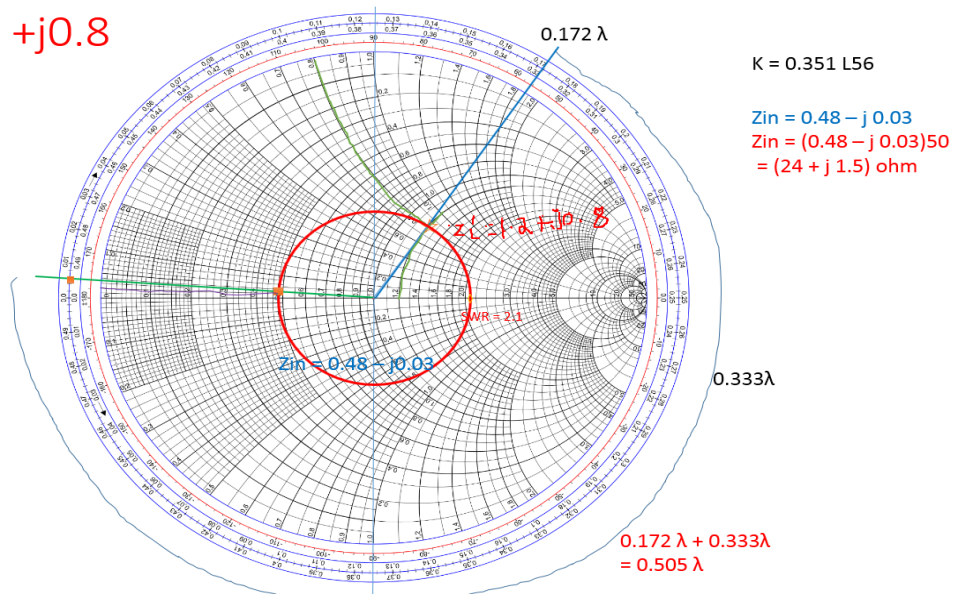
**Fig: 3.5.5 Normalized input impedance**

**STEP 8:**

- Fig 3.5.6, mark the reflection coefficient and phase angle in smith chart



$$z_L' = 1.2 + j0.8$$



**Fig: 3.5.6 Reflection coefficient and phase angle**

[Source: John D Ryder, —Networks, lines and fields, 2nd Edition, Prentice Hall India, 2015]