

## 5.6 Definition of Key Terms

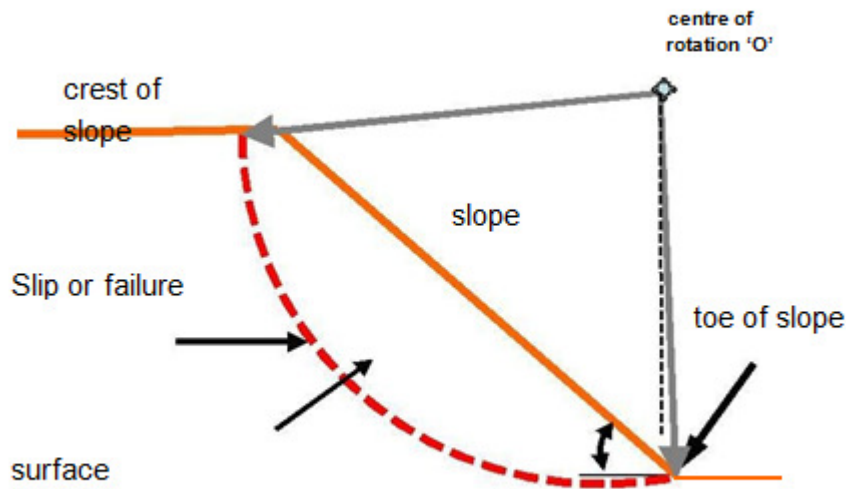


Fig 5.25 Slip circle

**Slip or failure zone:** It is a thin zone of soil that reaches the critical state or residual state and results in movement of the upper soil mass.

**Slip plane or failure plane or slip surface or failure surface:** It is the surface of sliding.

**Sliding mass:** It is the mass of soil within the slip plane and the ground surface.

**Slope angle (i):** It is the angle of inclination of a slope to the horizontal. The slope angle is sometimes referred to as a ratio, for example, 2:1 (horizontal: vertical).

### 5.6.1 Factor of safety

Factor of safety of a slope is defined as the ratio of average shear strength ( $\tau_f$ ) of a soil to the average shear stress ( $\tau_d$ ) developed along the potential failure surface.

$$FS = \frac{\tau_f}{\tau}$$

FS = Factor of safety

$\tau_f$  = average shear strength of the soil

$\tau_d$  = average shear stress developed along the potential surface.

### 5.6.2 Shear Strength:-

Shear strength of a soil is given by

$$\tau_f = c + \sigma \tan \phi$$

Where, c = cohesion

$\phi$  = angle of internal friction

$\sigma$  = Normal stress on the potential failure surface

Similarly, the mobilized shear strength is given by

$$\tau_d = c_d + \sigma \tan \phi_d$$

Let  $C_d$  and  $\phi$  are the cohesion and angle of internal friction that develop along the potential failure surface.

$$FS = \frac{\tau_f}{\tau}$$

$$FS = \frac{c + \sigma \tan \phi}{c_d + \sigma \tan \phi_d}$$

$$F_c = \frac{C}{C_d}$$

$$F = \frac{\tan \phi}{\tan \phi_d}$$

When  $F_c = F$  it gives Factor of safety w.r.t strength

$$C = \tan \phi$$

$$C_d = \tan \phi_d$$

$$\text{Then } F_s = F_c = F$$

When  $FS = 1$ , then the slope is said to be in a state of failure

### **5.6.3 USE OF STABILITY NUMBER [OR] TAYLOR'S STABILITY NUMBER [OR] STABILITY NUMBER [OR] STABILITY NUMBEREDR**

Taylor Stability number is a dimensionless quantity denoted by  $S_n$  and defined as

$$S_n = \frac{C_m}{\gamma H}$$

$C_m$ - Mobilized cohesion on slip  $\gamma$ - Unit

weight of soil

$H$ - Height of slope

$$\text{Also, } F_c = \frac{C}{C_m} \text{ so that, } C_m = \frac{C}{F_c}$$

Substituting in above equation, we get,

$$S_n = \frac{C}{F_c \gamma H}$$

Factor of safety is also expressed in terms of critical height

$$F_H = F_c = \frac{H_c}{H}$$

So that  $F_c H = H_c$

Substitute in above equation we get,

$$S_n = \frac{C_m}{\gamma H_c}$$

$H_c$  – critical height of slope

Table 5.1 Taylors stability number for cohesive soil

$\phi \rightarrow$	$0^\circ$	$5^\circ$	$10^\circ$	$15^\circ$	$20^\circ$	$25^\circ$
$i \downarrow$						
$90^\circ$	0.261	0.239	0.218	0.199	0.182	0.166
$75^\circ$	0.219	0.195	0.173	0.152	0.134	0.117
$60^\circ$	0.191	0.162	0.138	0.116	0.097	0.079
$45^\circ$	(0.170)	0.136	0.108	0.083	0.062	0.044
$30^\circ$	(0.156)	(0.110)	0.075	0.046	0.0625	0.009
$15^\circ$	(0.145)	(0.068)	(0.023)	–	–	–

Table 5.2 values of  $S_n$  for slope in cohesive soils( $\phi=0$ )with depth factors

Slope angle	Stability number $S_n$				
	Depth factor $D_f$				
	1	1.5	2	3	$\infty$
90	0.261				
75	0.219				
60	0.191				
53	0.181	0.181	0.181	0.181	0.181
45	0.164	0.174	0.177	0.180	0.181
30	0.133	0.164	0.172	0.178	0.181
22.5	0.113	0.153	0.166	0.175	0.181
15	0.083	0.128	0.150	0.167	0.181
7.5	0.054	0.080	0.107	0.140	0.181

The stability number is expressed as a function of cohesion, Factor of safety, Unitweight and Height of slope.

The stability number is directly proportional to cohesion and indirectly proportional to unit weight and the height of the slope. This is also called as Taylor's stability number ( $S_n$ )

The factor of safety with respect to cohesion is given by

$$F_c = C/C_m$$

Since Taylor stability number  $S_n$  is based on Factor of safety with respect to cohesion,  $F_c$ , the table and chart give ' $S_n$ ' only for the case where  $\phi$  is assumed to be fully mobilized. But in cases where factor of safety is applicable to both cohesion and friction, we have mobilized shearing resistance given by,

$$\phi_m = \tan^{-1} \left( \frac{\tan \phi}{F} \right)$$

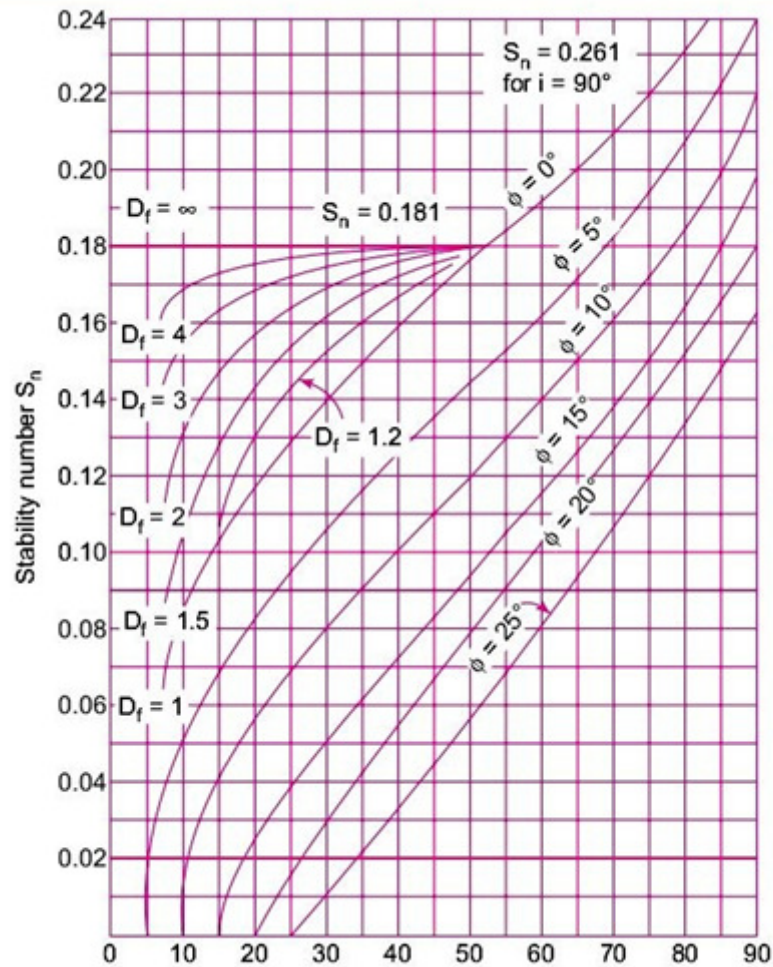


Fig5.26 chart of Taylors stability number

$$F_c = \frac{C}{S_n \gamma H}$$

As an appropriation  $\phi_m$  may be taken equal to  $\phi_F$

For cohesionless soil ( $C = 0$ )  $S_n$  is zero. It is not applicable.

$$F = \frac{\tan \phi}{\tan i}$$

For long term stability –  $C'$  and  $\phi'$  to be used,

Fully submerged slope –  $\gamma'$  should be used for  $S_n$

Saturated slope –  $\gamma_{sat}$  should be used for  $S_n$

Purely friction soil –  $S_n = 0$

Sudden draw down –  $\phi'$  replaced by  $\phi_w$

$$\phi_w = \frac{\gamma'}{\gamma_{sat}} \phi$$

**Problems:**

1) A canal with a depth of 5m has banks with slope 1:1. The properties of soil are :  $C = 20 \text{ KN/m}^2$  ;  $\phi = 15^\circ$  ;  $e = 0.7$  ;  $G = 2.6$

Calculate the factor of safety with respect to cohesion

- When canal runs full
- It is suddenly and completely emptied

Given:  $C = 20 \text{ KN/m}^2$

$$\phi = 15^\circ$$

$$e = 0.7$$

$$G = 2.6 ; H = 5\text{m}$$

Solution:

Case (1): When canal runs full, the side slopes are submerged ( $S=1$ )

$$\begin{aligned} \gamma_{sat} &= \frac{(G + e S) \gamma_w}{1 + e} \\ &= \frac{(2.6 + 0.7) 9.81}{1 + 0.7} \\ &= 19.04 \text{ KN/m}^2 \end{aligned}$$

$$\gamma' = \gamma_{sat} - \gamma_w = 19.04 - 9.81 = 9.23 \text{ KN/m}^2$$

From Taylor's stability chart,

For  $i=45^\circ$  and  $\phi = 15^\circ$ ,  $S_n = 0.083$

$$F_c = \frac{C}{S_n \gamma H}$$

$$F_c = \frac{20}{0.083 \times 9.81 \times 5} = 5.22$$

Case(ii) When canal is suddenly and completely emptied:

For sudden drawdown condition,  $S_n$  is to be obtained for slope angle  $i$  and weighted frictional angle  $\phi_w$ .

$$\phi_w = \frac{\gamma'}{\gamma_{sat}} \phi$$

$$\phi_w = \frac{9.23}{19.04} (15) = 7.3$$

From Taylors stability chart,

For  $i=45^\circ$  ;  $\phi_w = 7.3^\circ$  ;  $S_n = 0.122$

$$F_c = \frac{C}{S_n \gamma H}$$

$$F_c = \frac{20}{0.122 \times 9.81 \times 5}$$

$$= 1.72$$

2) A temporary cutting 8m deep is to be made in a clay having a unit weight of  $18 \text{ kN/m}^3$  and an average cohesion of  $20 \text{ kN/m}^2$ . A hard stratum of rock exists at a depth of 12m below the ground surface. Use Taylor's stability curves to estimate if a  $30^\circ$  slope is safe. If a factor of safety of 1.25 is considered necessary, find the safe slope angle.

Solution:

$$\text{Depth factor } D_f = \frac{12}{8} = 1.5$$

From Taylor's stability curve  $D_f=1.5, i=30^\circ, S_n=0.163$

$$F_c = \frac{C}{S_n \gamma H}$$

$$= \frac{20}{0.163 \times 18 \times 18} = 0.85$$

For  $F_c=1.25$  the stability number  $S_n$ ,

$$\begin{aligned}
 S_n &= \frac{C}{F_c \gamma H} \\
 &= \frac{20}{1.25 \times 18 \times 18} \\
 &= 0.11
 \end{aligned}$$

From Taylor's curve  $S_n = 0.11$  and  $D_f = 1.5$

We get  $i = 12^\circ$

3) A new canal is excavated to a depth of 5m below ground level, through a soil having the following characteristics,  $c = 14 \text{ kN/m}^2$ ,  $\phi = 15^\circ$ ,  $e = 0.8$  and  $G = 2.7$ . The slope of banks is 1 in 1. Calculate the factor of safety with respect to cohesion when the canal runs full. If it is suddenly and completely emptied, what will be the factor of safety?

Solution:

$$\begin{aligned}
 \gamma_{sat} &= \frac{G + e}{1 + e} \gamma_w \\
 &= \frac{2.7 + 0.8}{1 + 0.8} \times 9.81 \\
 &= 19.08 \text{ kN/m}^3
 \end{aligned}$$

$$\gamma' = 19.08 - 9.81 = 9.27 \text{ kN/m}^3$$

$$i = 45^\circ; \phi = 15^\circ$$

i) submerged Case: For  $i = 45^\circ$ ;  $\phi = 15^\circ$ ;  $S_n = 0.083$

$$F_c = \frac{C}{S_n \gamma' H} = \frac{14}{0.083 \times 9.27 \times 5} = 3.64$$

ii) Drawdown case: Taking  $F_\phi = 1$  and  $\phi_m = \phi$

$$\phi_w = \frac{\gamma'}{\gamma_{sat}} \phi$$



$$\phi_w = \frac{9.27}{19.08}(15) = 7.3^\circ$$

For  $i=45^\circ$ ;  $\phi=7.3^\circ$ ;  $S_n=0.122$

$$F_c = \frac{C}{S_n \gamma_{sat} H} = \frac{14}{0.122 \times 19.08 \times 5} = 1.2$$

4) Calculate the factor of safety with respect to cohesion of a clay slope laid at 1 in 2 to a height of 10m, if the angle of internal friction  $\phi=10^\circ$ ;  $c=25\text{KN/m}^2$  and  $\gamma=19\text{KN/m}^3$ . What will be the critical height of the slope in this soil?

Solution:

$$i = \tan^{-1} \left( \frac{1}{2} \right) = 26.5^\circ \text{ and } \phi=10^\circ, C=25\text{KN/m}^2 \text{ and } \phi=10^\circ, S_n=0.064$$

For  $i=26.5^\circ$

$$S_n = \frac{C}{F_c \gamma H}$$

$$F_c = \frac{C}{S_n \gamma H} = \frac{25}{0.064 \times 19 \times 10} = 2.06$$

The critical height  $H_c$  is given by

$$H_c = F_c \cdot H = 2.06 \times 10 = 20.6\text{m}$$

Alternatively,

$$H_c = \frac{c}{\gamma S_n} = \frac{25}{0.064 \times 19} = 20.6\text{m}$$

5) A slope is to be constructed at an inclination of  $30^\circ$  with the horizontal. Determine the safe height of the slope at factor of safety of 1.5. The soil has the following properties  $C=15\text{N/m}^2$ ,  $\phi=22.5^\circ$  and  $\gamma=19\text{KN/m}^3$ .

The mobilised frictional angle  $\phi_m$  is given by

$$\varphi_m = \frac{\varphi}{F} = \frac{22.5}{1.5} = 15^\circ$$

For  $i=30^\circ$  and  $\varphi_m=15^\circ, S_n=0.046$

$$S_n = \frac{C}{F_c \gamma H}$$

$$H = \frac{C}{F_c \gamma S_n} = \frac{15}{0.046 \times 1.5 \times 19} = 11.5m$$

