### 4.1 REVIEW OF NUMBER SYSTEMS

Many number systems are in use in digital technology. The most common are the decimal, binary, octal, and hexadecimal systems. The decimal system is clearly the most familiar to us because it is tools that we use every day.

Types of Number Systems are

1. Decimal Number system
2. Binary Number system
3. Octal Number system
4. Hexadecimal Number system

| DECIMAL | BINARY | OCTAL | HEXADECIMAL |
| :---: | :---: | :---: | :---: |
| 0 | 0000 | 0 | 0 |
| 1 | 0001 | 1 | 1 |
| 2 | 0010 | 2 | 2 |
| 3 | 0011 | 3 | 3 |
| 4 | 0100 | 4 | 4 |
| 5 | 0101 | 5 | 5 |
| 6 | 0110 | 6 | 6 |
| 7 | 0111 | 7 | 7 |
| 8 | 1000 | 10 | 8 |
| 9 | 1001 | 11 | 9 |
| 10 | 1010 | 12 | A |
| 11 | 1011 | 13 | B |
| 12 | 1100 | 14 | C |
| 13 | 1101 | 15 | D |



1. Decimal system: Decimal system is composed of 10 numerals or symbols. These 10 symbols are $0,1,2,3,4,5,6,7,8,9$. Using these symbols as digits of a number, we can express any quantity. The decimal system is also called the base-10 system because it has 10 digits. Even though the decimal system has only 10 symbols, any number of any magnitude can be expressed by using our system of positional weighting.

| $10^{3}$ | $10^{2}$ | $10^{1}$ | $10^{0}$ |  | $10^{-1}$ | $10^{-2}$ | $10^{3}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $=1000$ | $=100$ | $=10$ | =1 | - | $=0.1$ | $\begin{gathered} =0.0 \\ 1 \end{gathered}$ | $=0.001$ |
| $\begin{gathered} \hline \text { Most Significant } \\ \text { Digit } \\ \hline \end{gathered}$ |  |  |  | Decimal point |  |  | Least Significant Digit |

2. Binary System: In the binary system, there are only two symbols or possible digit values, 0 and 1 . This base- 2 system can be used to represent any quantity that can be represented in decimal or other base system.

| $\mathbf{2}^{\mathbf{3}}$ | $\mathbf{2}^{\mathbf{2}}$ | $\mathbf{2}^{\mathbf{1}}$ | $\mathbf{2}^{\mathbf{0}}$ |  | $\mathbf{2}^{\mathbf{- 1}}$ | $\mathbf{2}^{\mathbf{- 2}}$ | $\mathbf{2}^{\mathbf{- 3}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $=8$ | $=4$ | $=2$ | $=\mathbf{1}$ | $\mathbf{\bullet}$ | $=0.5$ | $=0.25$ | $=0.125$ |
| Most <br> Significant <br> Digit |  |  |  | Binary <br> point |  |  | Least <br> Significant <br> Digit |

In digital systems the information that is being processed is usually presented in binary form. Binary quantities can be represented by any device that has only two operating states or possible conditions. E.g.. A switch is only open or closed. We arbitrarily (as we define them) let an open switch represent binary 0 and a closed switch represent binary 1. Thus we can represent any binary number by using series of switches.
3. Octal System: The octal number system has a base of eight, meaning that it has eight possible digits: $0,1,2,3,4,5,6,7$.

| $\mathbf{8}^{\mathbf{3}}$ | $\mathbf{8}^{\mathbf{2}}$ | $\mathbf{8}^{\mathbf{1}}$ | $\mathbf{8}^{0}$ |  | $\mathbf{8}^{\mathbf{- 1}}$ | $\mathbf{8}^{-2}$ | $\mathbf{8}^{\mathbf{3}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $=512$ | $=64$ | $=8$ | $=1$ |  | $=1 / 8$ | $=1 / 64$ | $=1 / 512$ |
| Most Significant <br> Digit |  |  |  | Octal <br> point |  |  | Least <br> Significant <br> Digit |

4. Hexadecimal System: The hexadecimal system uses base 16. Thus, it has 16 possible digit symbols. It uses the digits 0 through 9 plus the letters $\mathrm{A}, \mathrm{B}, \mathrm{C}, \mathrm{D}, \mathrm{E}$, and F as the 16 digit symbols.

| $\mathbf{1 6}^{\mathbf{3}}$ | $\mathbf{1 6}^{\mathbf{2}}$ | $\mathbf{1 6}^{\mathbf{1}}$ | $\mathbf{1 6}^{\mathbf{0}}$ |  | $\mathbf{1 6}^{\mathbf{- 1}}$ | $\mathbf{1 6}^{\mathbf{- 2}}$ | $\mathbf{1 6}^{\mathbf{- 3}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $=4096$ | $=256$ | $=16$ | $=1$ | . | $=1 / 16$ | $=1 / 256$ | $=1 / 4096$ |
| Most <br> Significant <br> Digit |  |  |  | Hexadeci <br> mal point |  |  | Least <br> Significant <br> Digit |

