

DECIMAL ADDER

BCD (Binary coded decimal) Adder:

If two BCD digits are added then their sum result will not always be in BCD. Consider the two given examples.

Correct: Result is in BCD.

$$\begin{array}{r} 0110 = 6 \\ +0011 = +3 \\ \hline 1001 = 9 \end{array}$$

Wrong: Result is not in BCD.

$$\begin{array}{r} 0101 = 5 \\ +0111 = +7 \\ \hline 1100 = 12 \end{array}$$

In the first example, result is in BCD while in the second example it is not in BCD.

Four bits are needed to represent all BCD digits (0 - 9). But with four bits we can represent up to 16 values (0000 through 1111). The extra six values (1010 through 1111) are **not valid** BCD digits.

Whenever the sum result is ≥ 9 , it will not be in BCD and will require correction to get a valid BCD result.

Z3	Z2	Z1	Z0	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

Correction is done through the addition of 6 to the result to skip the six invalid values as shown in the truth table by **yellow** color.

Consider the given examples of non-BCD sum result and its correction.

Non-BCD	0101 = 5
	+0111 = +7
BCD correction	1100 = 12
	+0110 = +6
In BCD	1 0010 = 12

Non-BCD	1001 = 9
	+0110 = +6
BCD correction	1111 = 15
	+0110 = +6
In BCD	1 0101 = 15

Non-BCD	1001 = 9
	+1001 = +9
BCD correction	1 0010 = 18
	+0110 = +6
In BCD	1 1000 = 18

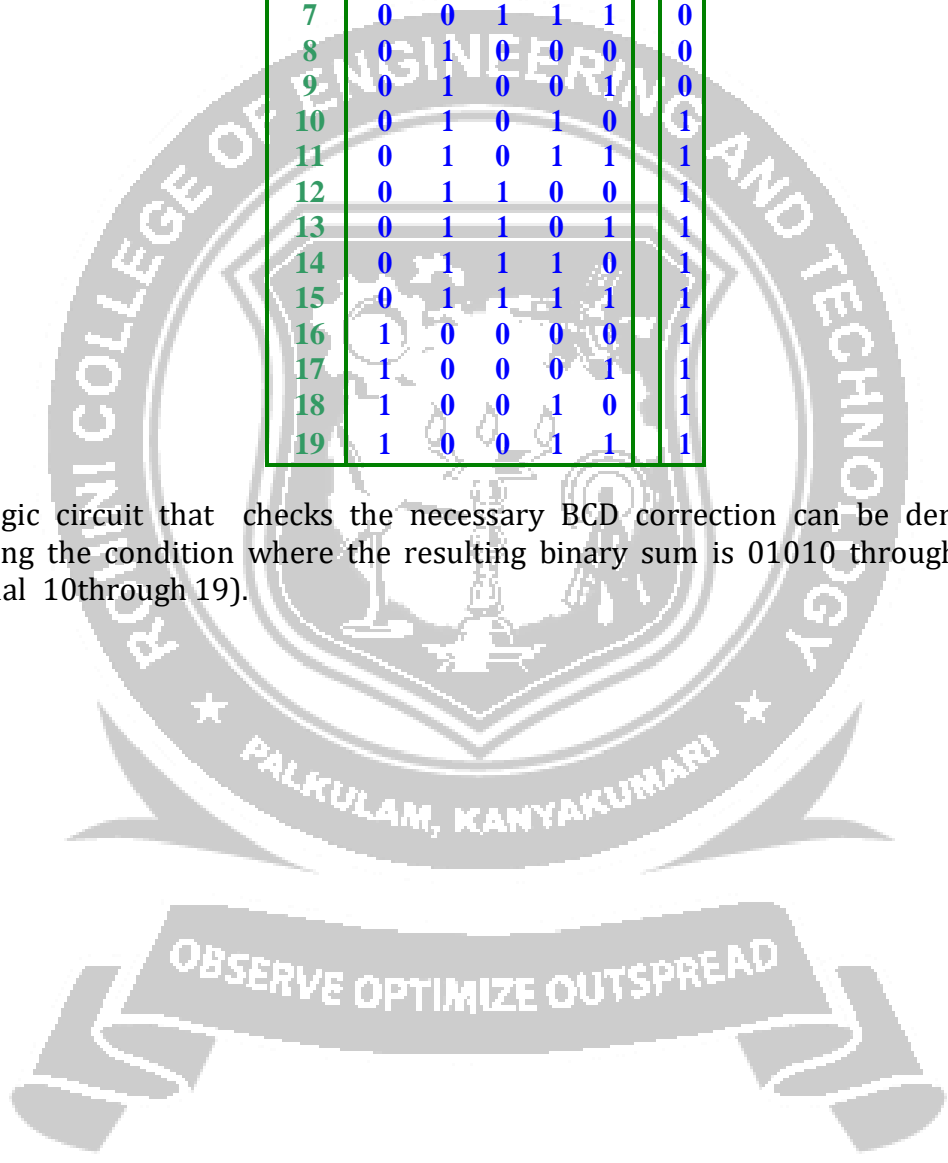
A BCD adder is a circuit that adds two BCD digits in parallel and produces a sum BCD digit and a carry out bit.

The maximum sum result of a BCD input adder can be 19. As maximum number in BCD is 9 and may be there will be a carry from previous stage also, so $9 + 9 + 1 = 19$

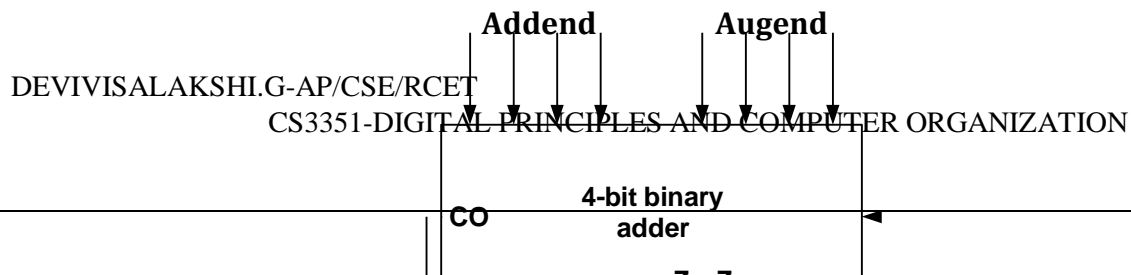
The following truth table shows all the possible sum results when two BCD digits are added.

Dec	CO	Z ₃	Z ₂	Z ₁	Z ₀	F
0	0	0	0	0	0	0
1	0	0	0	0	1	0
2	0	0	0	1	0	0
3	0	0	0	1	1	0
4	0	0	1	0	0	0
5	0	0	1	0	1	0
6	0	0	1	1	0	0
7	0	0	1	1	1	0
8	0	1	0	0	0	0
9	0	1	0	0	1	0
10	0	1	0	1	0	1
11	0	1	0	1	1	1
12	0	1	1	0	0	1
13	0	1	1	0	1	1
14	0	1	1	1	0	1
15	0	1	1	1	1	1
16	1	0	0	0	0	1
17	1	0	0	0	1	1
18	1	0	0	1	0	1
19	1	0	0	1	1	1

The logic circuit that checks the necessary BCD correction can be derived by detecting the condition where the resulting binary sum is 01010 through 10011 (decimal 10 through 19).

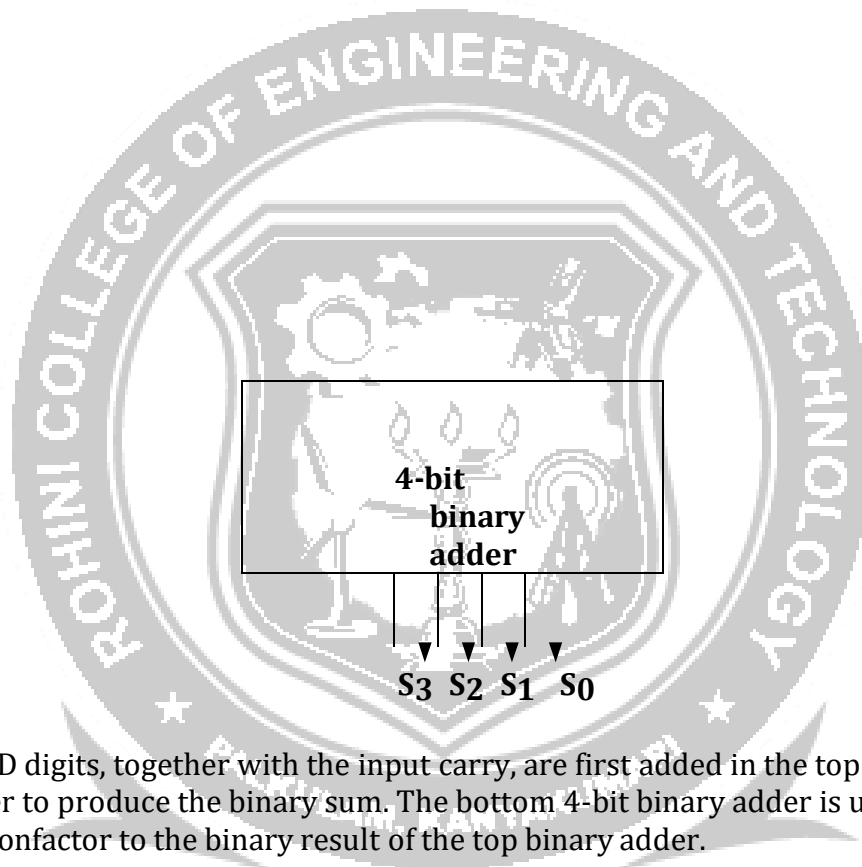


The circuit of the BCD adder will be as shown in the figure.



Carry
out

Carry
in



The two BCD digits, together with the input carry, are first added in the top 4-bit binary adder to produce the binary sum. The bottom 4-bit binary adder is used to add the correction factor to the binary result of the top binary adder.

- When the **Output carry** is equal to **zero**, the correction factor equals zero.
- When the **Output carry** is equal to **one**, the correction factor is 0110.

The output carry generated from the bottom binary adder is ignored, since it supplies information already available at the **output-carry** terminal.

A decimal parallel adder that adds **n** decimal digits needs **n** BCD adder stages. The output carry from one stage must be connected to the input carry of the next higher-order stage.