EC 3352 - DIGITAL SYSTEM DESIGN

## UNIT - III : SYNCHRONOUS SEOUENTIAL CIRCUITS

### 3.2 ANALYSIS AND DESIGN OF CLOCKED SEQUENTIAL CIRCUITS Triggering Of Flip-Flops

The state of a Flip-Flop is switched by a momentary change in the input signal. This momentary change is called a trigger and the transition it causes is said to trigger the Flip-Flop. Clocked Flip-Flops are triggered by pulses. A clock pulse starts from an initial value of 0 , goes momentarily to 1 and after a short time, returns to its initial 0 value.

Latches are controlled by enable signal, and they are level triggered, either positive level triggered or negative level triggered. The output is free to change according to the S and R input values, when active level is maintained at the enable input.

Flip-Flops are different from latches. Flip-Flops are pulse or clock edge triggered instead of level triggered.


Fig : 3.12 - Various types of triggering

## EDGE TRIGGERED FLIP-FLOPS

Flip-Flops are synchronous bistable devices (has two outputs Q and Q'). In this case, the term synchronous means that the output changes state only at a specified point on the triggering input called the clock (CLK), i.e., changes in the output occur in synchronization with the clock.

An edge-triggered Flip-Flop changes state either at the positive edge (rising edge) or at the negative edge (falling edge) of the clock pulse and is sensitive to its inputs only at this transition of the clock. The different types of edge-triggered Flip- Flops are-xS-R Flip-Flop, xJ-K Flip-Flop, xD Flip-Flop, xT Flip-Flop.

Although the S-R Flip-Flop is not available in IC form, it is the basis for the D and J-K Flip-Flops. Each type can be either positive edge-triggered (no bubble at C input) or negative edge-triggered (bubble at C input). The key to identifying an edge- triggered Flip-Flop by its logic symbol is the small triangle inside the block at the clock $(\mathrm{C})$ input. This triangle is called the dynamic input indicator.

## S-R Flip-Flop

The $S$ and R inputs of the S-R Flip-Flop are called synchronous inputs because data on these inputs are transferred to the Flip-Flop's output only on the triggering edge of the clock pulse. The circuit is similar to SR latch except enable signal is replaced by clock pulse (CLK). On the positive edge of the clock pulse, the circuit responds to the S and R inputs.


Fig : 3.13 - SR Flip-Flop

When S is HIGH and R is LOW, the Q output goes HIGH on the triggering edge of the clock pulse, and the Flip-Flop is SET. When S is LOW and R is HIGH, the Q output goes LOW on the triggering edge of the clock pulse, and the Flip- Flop is RESET. When both S and R are LOW, the output does not change from its prior state.

An invalid condition exists when both $S$ and $R$ are HIGH.

| CL <br> $\mathbf{K}$ | $\mathbf{S}$ | $\mathbf{R}$ | Qn | Qn+ <br> $\mathbf{1}$ | State |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | 0 | 0 | No Change (NC) |
| 1 | 0 | 0 | 1 | 1 |  |
| 1 | 0 | 1 | 0 | 0 | Reset |
| 1 | 0 | 1 | 1 | 0 |  |
| 1 | 1 | 0 | 0 | 1 | Set |
| 1 | 1 | 0 | 1 | 1 |  |
| 1 | 1 | 1 | 0 | xx | Indeterminate |
| 1 | 1 | 1 | 1 |  | $*$ |
| 0 | x | x | 0 | 0 | No Change (NC) |
| 0 | x | x | 1 | 1 |  |

Truth table for SR Flip-Flop


Fig : 3.14-Input and output waveforms of SR Flip-Flop

## J-K Flip-Flop:

JK means Jack Kilby, Texas Instrument (TI) Engineer, who invented IC in 1958. JK Flip-Flop has two inputs $\mathrm{J}($ set ) and K(reset). A JK Flip-Flop can be obtained from the clocked SR Flip-Flop by augmenting two AND gates as shown below.


Fig : 3.15- JK Flip Flop
The data input J and the output Q ' are applied o the first AND gate and its output (JQ') is applied to the S input of SR Flip-Flop. Similarly, the data input K and the output Q are applied to the second AND gate and its output ( KQ ) is applied to the R input of SR Flip-Flop.

(a) Using SR flipflop

(b) Graphic symbol

Fig : 3.16- JK Flipflop using SR Flipflop
$\mathbf{J}=\mathbf{K}=\mathbf{0}$
When $\mathrm{J}=\mathrm{K}=0$, both AND gates are disabled. Therefore clock pulse have no effect, hence the Flip-Flop output is same as the previous output.
$\mathbf{J}=\mathbf{0}, \mathbf{K}=\mathbf{1}$
When $\mathrm{J}=0$ and $\mathrm{K}=1$, AND gate 1 is disabled i.e., $\mathrm{S}=0$ and $\mathrm{R}=1$. This condition will reset the Flip-Flop to 0 .

$$
\mathbf{J}=\mathbf{1}, \mathrm{K}=\mathbf{0}
$$

When $\mathrm{J}=1$ and $\mathrm{K}=0$, AND gate 2 is disabled i.e., $\mathrm{S}=1$ and $\mathrm{R}=0$. Therefore the Flip-Flop will set on the application of a clock pulse.
$\mathbf{J}=\mathbf{K}=\mathbf{0}$
When $\mathrm{J}=\mathrm{K}=1$, it is possible to set or reset the Flip-Flop. If Q is High, AND gate 2 passes on a reset pulse to the next clock. When Q is low, AND gate 1 passes on a set pulse to the next clock. Eitherway, Q changes to the complement of the last state i.e., toggle. Toggle means to switch to the opposite state.The truth table of JK Flip-Flop is given below.

| CLK | Inputs |  | Output | State |
| :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{J}$ | $\mathbf{K}$ | $\mathbf{Q n + 1}$ |  |
| 1 | 0 | 0 | Qn | No Change |
| 1 | 0 | 1 | 0 | Reset |
| 1 | 1 | 0 | 1 | Set |
| 1 | 1 | 1 | Q $_{\mathrm{n}}{ }^{\prime}$ | Toggle |



Fig : 3.17- Input and output waveforms of JK Flip-Flop

## Characteristic table and Characteristic equation:

The characteristic table for JK Flip-Flop is shown in the table below. Fromthe table, K-map for the next state transition $\left(\mathrm{Q}_{\mathrm{n}+1}\right)$ can be drawn and the simplified logic expression which represents the characteristic equation of JK Flip-Flop can be found.

| Qn | $\mathbf{J}$ | $\mathbf{K}$ | $\mathbf{Q n +}$ |
| :---: | :---: | :---: | :---: |
| $\mathbf{1}$ |  |  |  |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 |

## Characteristic table

## K-map Simplification:

| JK |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 | 1 |

Characteristic equation: $\mathbf{Q}_{\mathbf{n}+1}=\mathbf{J Q}{ }^{\prime}+$

## K'Q.D Flip-Flop:

Like in D latch, in D Flip-Flop the basic SR Flip-Flop is used with complemented inputs. The D Flip-Flop is similar to D-latch except clock pulse isused instead of enable input.


Fig : 3.18 - D Flip-Flop
To eliminate the undesirable condition of the indeterminate state in the RS Flip-Flop is to ensure that inputs $S$ and $R$ are never equal to 1 at the same time. This is done by D Flip-Flop. The D (delay) Flip-Flop has one input called delay input and clock pulse input. The D Flip-Flop using SR Flip-Flop is shown below.

(a) Using SR flipflop

(b) Graphic symbol

Fig : 3.19 - D Flipflop using SR
FlipflopThe truth table of D Flip-Flop is given below.

| Cloc <br> $\mathbf{k}$ | $\mathbf{D}$ | Qn+ | State |
| :---: | :---: | :---: | :---: |
| 1 | 0 | 0 | Reset |
| 1 | 1 | 1 | Set |
| 0 | x | Qn | No Change |

Truth table for D Flip-Flop


Fig : 3.20 - Input and output waveforms of clocked D Flip-Flop

Looking at the truth table for D Flip-Flop we can realize that $\mathrm{Q}_{\mathrm{n}+1}$ function follows the D input at the positive going edges of the clock pulses.

## Characteristic table and Characteristic equation:

The characteristic table for D Flip-Flop shows that the next state of the Flip- Flop is independent of the present state since $\mathrm{Q}_{\mathrm{n}+1}$ is equal to D . This means that an input pulse will transfer the value of input D into the output of the Flip-

Flop independent of the value of the output before the pulse was applied. The characteristic equation is derived from K-map.

| Qn | D | Qn+ <br> $\mathbf{1}$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

## Characteristic table

K-map simplification

| Qn ${ }^{\text {D }}$ |  |  |
| :---: | :---: | :---: |
| 0 | 0 | 1 |
| 1 | 0 | 1 |

Characteristic equation: $\mathbf{Q}_{\mathbf{n}+1}=\mathbf{D}$.

## T Flip-Flop

The T (Toggle) Flip-Flop is a modification of the JK Flip-Flop. It is obtainedfrom JK Flip-Flop by connecting both inputs J and K together, i.e., single input.

Regardless of the present state, the Flip-Flop complements its output when the clock pulse occurs while input $\mathrm{T}=1$.


Fig : 3.21-T Flip-Flop

When $T=0, Q_{n+1}=Q_{n}$, ie., the next state is the sameas the present state and no change occurs. When $\mathrm{T}=1, \mathrm{Qn}+1=\mathrm{Qn}$, ie., the next state is the complement of the present state.


Fig : 3.22 - T flipflop using JK
FlipflopThe truth table of T Flip-Flop is given below.

| $\mathbf{T}$ | Qn+1 | State |
| :---: | :---: | :---: |
| 0 | Qn | No Change |
| 1 | Qn' | Toggle |
|  |  |  |

Truth table for T Flip-
FlopCharacteristic table and Characteristic equation:

The characteristic table for T Flip-Flop is shown below andcharacteristic equation is derived using K-map.

| Qn | T | Qn+ <br> $\mathbf{1}$ |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

K-map Simplification:


Characteristic equation: $\mathbf{Q}_{\mathbf{n + 1}}=\mathbf{T} \mathbf{Q}_{\mathbf{n}}{ }^{\mathbf{+}}+\mathbf{T}^{\mathbf{\prime}} \mathbf{Q}_{\mathbf{n}}$.

## Master-Slave JK Flip-Flop

A master-slave Flip-Flop is constructed using two separate JK FlipFlops. The first Flip-Flop is called the master. It is driven by the positive edge of the clock pulse. The second Flip-Flop is called the slave. It is driven by the negative edge of the clock pulse. The logic diagram of a master-slave JK Flip-Flop isshown below.


Fig : 3.32 - Logic diagram
When the clock pulse has a positive edge, the master acts according to
its J- K inputs, but the slave does not respond, since it requires a negative edge at the clock input.

When the clock input has a negative edge, the slave Flip-Flop copies the master outputs. But the master does not respond since it requires a positive edge at its clock input. The clocked master-slave J-K Flip-Flop using NAND gates is shown below.


Fig : 3.33-Master-Slave JK Flip-Flop

## APPLICATION TABLE (OR) EXCITATION TABLE:

The characteristic table is useful for analysis and for defining the operation of the Flip-Flop. It specifies the next state $\left(\mathrm{Q}_{\mathrm{n}+1}\right)$ when the inputs and present state are known.

The excitation or application table is useful for design process. It is used to find the Flip-Flop input conditions that will cause the required transition, when the present state $\left(\mathrm{Q}_{\mathrm{n}}\right)$ and the next state $\left(\mathrm{Q}_{\mathrm{n}+1}\right)$ are known.

## SR Flip-Flop:

| Present <br> State | Inputs |  | Next <br> State |
| :---: | :---: | :---: | :---: |
| Qn | $\mathbf{S}$ | $\mathbf{R}$ | Qn+1 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | $x$ |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | $x$ |


| Present <br> State | Next <br> State | Inputs |  | Inputs |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Qn | Qn+1 | S | R | S | R |
| 0 | 0 | 0 | 0 | 0 | $x$ |
| 0 | 0 | 0 | 1 |  |  |
| 0 | 1 | 1 | 0 | 1 | 0 |
| 1 | 0 | 0 | 1 | 0 | 1 |
| 1 | 1 | 0 | 0 | $x$ | 0 |
| 1 | 1 | 1 | 0 |  |  |

Characteristic Table
Modified Table

| Present <br> State | Next <br> State | Inputs |  |
| :---: | :---: | :---: | :---: |
| Qn | Qn+ <br> $\mathbf{1}$ | $\mathbf{S}$ | $\mathbf{R}$ |
| 0 | 0 | 0 | x |
| 0 | 1 | 1 | 0 |
| 1 | 0 | 0 | 1 |
| 1 | 1 | x | 0 |

Excitation Table

The above table presents the excitation table for SR Flip-Flop. It consists of present state $\left(\mathrm{Q}_{\mathrm{n}}\right)$, next state $\left(\mathrm{Q}_{\mathrm{n}+1}\right)$ and a column for each input to show how the required transition is achieved.

There are 4 possible transitions from present state to next state. The required Input conditions for each of the four transitions are derived from the information available in the characteristic table. The symbol ' $x$ ' denotes the don't care condition, it does not matter whether the input is 0 or 1 .

## JK Flip-Flop:

| Present <br> State | Inputs |  | Next <br> State |
| :---: | :---: | :---: | :---: |
| Qn | J | K | Qn+1 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 0 |
| 0 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 |
| 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 0 |


| Present <br> State | Next State | Inputs |  | Inputs |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Qn | Qn+1 | J | K | J | K |
| 0 | 0 | 0 | 0 | 0 | x |
| 0 | 0 | 0 | 1 |  |  |
| 0 | 1 | 1 | 0 | 1 | x |
| 0 | 1 | 1 | 1 |  |  |
| 1 | 0 | 0 | 1 | X | 1 |
| 1 | 0 | 1 | 1 |  |  |
| 1 | 1 | 0 | 0 | X | 0 |
| 1 | 1 | 1 | 0 |  |  |

Characteristic Table
Modified Table

| Present |  |  |  |
| :---: | :---: | :---: | :---: |
| State | Next <br> State | Inputs |  |
| Qn | Qn+ | J | K |
| 0 | 0 | 0 | x |
| 0 | 1 | 1 | x |
| 1 | 0 | x | 1 |
| 1 | 1 | x | 0 |

## Excitation Table

## D Flip-Flop

| Present <br> State | Input | Next <br> State |
| :---: | :---: | :---: |
| Qn | D | Qn+1 |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

Characteristic Table

| Present <br> State | Next <br> State | Input |
| :---: | :---: | :---: |
| Qn | Qn+1 | D |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

Excitation Table

## T Flip-Flop

| Present <br> State | Input | Next <br> State |
| :---: | :---: | :---: |
| Qn | T | Qn+1 |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

Characteristic Table

| Present <br> State | Next <br> State | Input |
| :---: | :---: | :---: |
| $\mathbf{Q n}$ | $\mathbf{Q n + 1}$ | $\mathbf{T}$ |
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

Modified Table

REALIZATION OF ONE FLIP-FLOP USING OTHER FLIP-FLOPS
1 SR Flip-Flop to D

2 D Flip-Flop SR

3 JK Flip Flop to SR

4 T Flip-FlopSR Flip

5 SR Flop to T Flip

6 JK Flip-Flop to T
$7 \quad$ T Flip-Flop JKFlip
$8 \quad$ Flop to D Flip

9 T Flop D Flip-Flop

10 D to T Flip-Flop

1. Write the characteristic table for required Flip-Flop (D Flip-Flop). x Write theexcitation table for given Flip-Flop (SR Flip-Flop).
2. Determine the expression for the given Flip-Flop inputs (S and R) by using K-map.
3. Draw the Flip-Flop conversion logic diagram to obtain the required FlipFlop(D Flip-Flop) by using the above obtained expression.

The excitation table for the above conversion is

| Required Flip-Flop (D) |  | Given Flip- <br> Flop <br> (SR) |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Inpu <br> t | Present <br> state | Next state | Flip-Flop Inputs |  |
| D | Qn | Qn+1 | S | R |
| 0 | 0 | 0 | 0 | x |
| 0 | 1 | 0 | 0 | 1 |
| 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 1 | x | 0 |

## K -map simplication

## For $\$$ <br> For R

Logic dagram

$\$=$ D

$R=\bar{D}$

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## SR Flip-Flop to JK Flip-Flop

The excitation table for the above conversion is,

| Inputs |  | Present <br> state | Next state | Flip- <br> Flop <br> Input |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{J}$ | $\mathbf{K}$ | $\mathbf{Q n}$ | Qn+1 | $\mathbf{S}$ | $\mathbf{R}$ |
| 0 | 0 | 0 | 0 | 0 | x |
| 0 | 0 | 1 | 1 | x | 0 |
| 0 | 1 | 0 | 0 | 0 | x |
| 0 | 1 | 1 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 1 | x | 0 |
| 1 | 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 1 |  |

K-map simplification

## For S



| K $\mathrm{Q}_{\mathrm{n}}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 00 | 01 | 11 | 10 |
| 0 | x | 0 | 1 | x |
| 1 | 0 | 0 | 1 | 0 |

$$
\mathrm{S}=\mathrm{J} \overline{\mathrm{Q}}_{\mathrm{n}} \quad \mathrm{R}=\mathrm{K} \mathrm{Q}_{\mathrm{n}}
$$



| Inpu <br> $\mathbf{t}$ | Present <br> state | Next state | Flip-Flop <br> Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| T | Qn | Qn+1 | S | R |
| 0 | 0 | 0 | 0 | x |
| 0 | 1 | 1 | x | 0 |
| 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 1 |

K-map simplification
For $S$

For R

$\mathrm{R}=\mathrm{T} \mathrm{Q}_{\mathrm{n}}$

Logic diagram


$$
\mathrm{S}=\mathrm{T} \overline{\mathrm{Q}}_{\mathrm{n}}
$$

p-Flop
The excitation table for the above conversion is

| Inpu <br> $\mathbf{t}$ | Present <br> state | Next state | Flip-Flop <br> Inputs |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | $\mathbf{Q n}$ | $\mathbf{Q n + 1}$ | $\mathbf{J}$ | $\mathbf{K}$ |
| 0 | 0 | 0 | 0 | x |
| 0 | 1 | 1 | x | 0 |
| 1 | 0 | 1 | 1 | x |
| 1 | 1 | 0 | x | 1 |

K-map simplification
For J

$\mathrm{J}=\mathrm{T}$

For K

$K=T$

Logic diagram


## JK Flip-Flop to D Flip-Flop

The excitation table for the above conversion is


## D Flip-Flop to T Flip-Flop

The excitation table for the above conversion is

| Inpu <br> $\mathbf{t}$ | Present <br> state | Next state | Flip- <br> Flop <br> Input |
| :---: | :---: | :---: | :---: |
| $\mathbf{T}$ | Qn | Qn+1 | $\mathbf{D}$ |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |

K-map simplification
Logic diagram


$$
\begin{aligned}
\mathrm{D} & =\overline{\mathrm{T}} \mathrm{Q}_{\mathrm{n}}+\mathrm{T} \overline{\mathrm{Q}}_{\mathrm{n}} \\
& =\mathrm{T} \oplus \mathrm{Q}_{\mathrm{n}}
\end{aligned}
$$

## T Flip-Flop to D Flip-Flop

The excitation table for the above conversion is

| Inpu <br> $\mathbf{t}$ | Present <br> state | Next state | Flip- <br> Flop <br> Input |
| :---: | :---: | :---: | :---: |
| $\mathbf{D}$ | Qn | Qn+1 | $\mathbf{T}$ |
| 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 |

K -map simplification

| $\mathrm{Q}_{\mathrm{n}}$ |  |  |
| :---: | :---: | :---: |
|  | 0 | 1 |
| 0 | 0 | (1) |
| 1 | (1) | 0 |

$\mathrm{T}=\mathrm{D} \overline{\mathrm{Q}}_{\mathrm{n}}+\overline{\mathrm{D}} \mathrm{Q}_{\mathrm{n}}$
$=\mathrm{D} \oplus \mathrm{Q}_{\mathrm{n}}$

Logic diagram



