

3.6. COMPOSITE BEAMS (FLITCHED BEAMS)

A beam made up of two or more different materials assumed to be rigidly connected together and behaving like a single piece is known as a composite beam or a wooden flitched beam. The strain at the common surface will be same for both materials. Also the total moment of resistance will be equal to the sum of the moments of individual sections.

Problem 3.6.1. a flitched beam consist of a wooden joist 10cm wide and 20cm deep strengthened by two steel plates 10mm thick and 20cm deep. If the max stress in the wooden joist is 7 N/mm². Find the corresponding max stress attained in steel. Find also the moment of resistance of the composite section. Take youngs modulus for steel = 2×10^5 N/mm² and for wood = 1×10^4 N/mm²

Given

Let width of wooden joist $b_2 = 10\text{cm}$

Depth of wooden joist $d_2 = 20\text{cm}$

Width of one steel plate $b_1 = 1\text{cm}$

Depth of one steel plate $d_1 = 20\text{cm}$

Number of steel plate = 2

Max stress in wood $\sigma_2 = 7\text{N/mm}^2$

E for steel $E_1 = 2 \times 10^5$ N/mm²

E for wood $E_2 = 1 \times 10^4$ N/mm²

Solution:

M.O.I. of wooden joist about N.A.

$$I_2 = b_2 d_2^3 / 12 = 6666.66\text{cm}^4$$

M.O.I of two steel plates about N.A

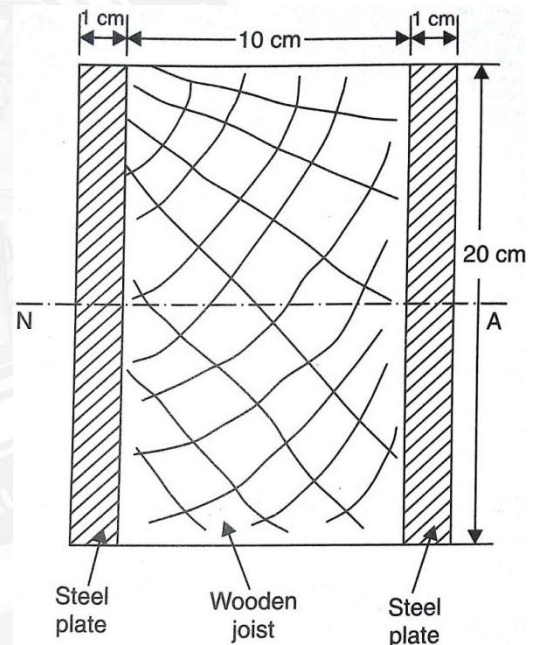
$$I_2 = 2 \times b_1 d_1^3 = 1333.33 \times 10^4 \text{ mm}^4$$

Now using $\sigma_1/E_1 = \sigma_2/E_2$

$$\sigma_1 = 20 \times 7 = 140 \text{ N/mm}^2$$

Total moment $M = M_1 + M_2$

$$\begin{aligned} \text{Where } M_1 &= \frac{\sigma_1}{y} \times I_1 \\ &= \frac{140}{100} \times 1333.33 \times 10^4 \\ &= 18666.620 \text{ Nm} \end{aligned}$$



$$\begin{aligned}
 M_2 &= \sigma_2 \times I_2 \\
 &= \frac{7}{100} \times 6666.66 \times 10^4 \text{ N mm} \\
 &= 4666.662 \text{ Nm} \\
 M &= M_1 + M_2 \\
 &= 18666.620 + 4666.662 \\
 &= \mathbf{23333.282 \text{ Nm}}
 \end{aligned}$$

IMPORTANT TERMS

Shear force	<p>Adding of vertical forces from right side to the consider point of the beam</p> <p>Symbol:</p> <p>Downward force = + ve</p> <p>Upward force = - ve</p>	<p>Diagram:</p> <p>Point load (W) = vertical line (upward force = downward line Downward force = upward line)</p> <p>UVL (w) – Inclined line</p> <p>UVL (w) – parabolic curve</p> <p>Cantilever Beam : +ve side</p> <p>SSB : + ve or – ve</p> <p>OHB : + ve or – ve</p>
Bending moment	<p>Adding of bending moment from right side to the consider point of the beam.</p> <p>Symbol:</p> <p>Clockwise direction = - ve</p> <p>Anticlockwise direction = +ve</p> <p>CLB : free end = 0</p> <p>SSB : Both end = 0</p> <p>OHB : Both end = 0</p>	<p>Diagram:</p> <p>Point load (W) – Inclined line (upward force = downward line Down force = upward line)</p> <p>UVL (w) – parabolic curve</p> <p>UVL (w) – Cubic Curve</p> <p>Cantilever Beam : - ve side</p> <p>SSB : + ve</p> <p>OHB : + ve or – ve</p>
Cantilever Beam	Adding of vertical forces	<p>PL = add only W</p> <p>UDL = Add (Force x distance)</p>
SSB	<p>Step 1: To find reaction forces at two support (R_A, R_B)</p> <p>Take moment about A = 0 to find Reaction R_B</p> <p>Sum of upward force = downward force; to find reaction R_A</p>	<p>UDL acting point = midpoint = $l/2$</p> <p>UVL = add ($wl/2$)</p> <p>UVL acting point from small end = $2l/3$</p> <p>UVL acting point from big end = $l/3$</p>

OHB	Same procedure as SSB SF with Reaction & without reaction calculate	Maximum bending moment at shear force become zero (SF = 0) Point of contraflexure act at Bending moment become zero (BM = 0)
BENDING STRESS IN BEAM		
Bending Equation	$\frac{M}{I} = \frac{\sigma_{max}}{y_{max}} = \frac{E}{R}$ <p>Based on type of beam with support to find M which is available in IV unit table</p>	<p><i>M = Bending Moment</i> <i>I = Moment of Inertia</i> <i>σ = Bending stress</i> <i>y = distance of Neutral axis</i> <i>E = Youngs modulus</i> <i>R = Bending radius</i></p>
Section Modulus	$Z = \frac{I}{y}$ $= \frac{bd^2}{6} \text{ for Rectangular section}$ $= \frac{1}{6D}(BD^3 - bd^3) \text{ hollow Rect}$	$= \frac{\pi d^3}{32} \text{ for circular section}$ $= \frac{\pi}{32D}(D^4 - d^4) \text{ hollow circlr}$
For Unsymmetrical section	<p>Step1: to find C.G of the section in y direction = \bar{y} but max value of y is used in bending eqn.</p> <p>Step2: to find Moment of inertia of the section = I</p> <p>Step3: from Moment eqn to find unknown value</p>	
Moment of resistance of a section	$M = \sigma \times Z$	
Composite beam(Flitched beams)	Strain remains same $e_1 = e_2 = \frac{\sigma_1}{E_1} = \frac{\sigma_2}{E_2}$	
Modular Ratio	$= \frac{E_1}{E_2}$	