

**ROHINI COLLEGE OF ENGINEERING AND TECHNOLOGY**  
**Approved by AICTE & Affiliated to Anna University**  
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**DEPARTMENT OF MECHANICAL ENGINEERING**



**NAME OF THE SUBJECT: ENGINEERING MECHANICS**

**SUBJECT CODE : ME3351**

**REGULATION 2021**

**UNIT II: STATICS OF RIGID BODIES IN TWO  
DIMENSIONAL**





### Non current coplander force system:

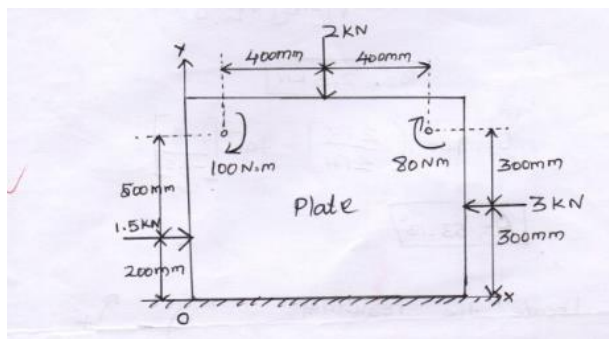
1. Resolve the given forces, if they are inclined to reference x and y Axis.
2. Find the sum of horizontal component of forces  $\sum F_H$
3. Find the sum of vertical component of forces  $\sum F_V$
4. Calculate the resultant force  $R = \sqrt{(\sum F_H)^2 + (\sum F_V)^2}$
5. Angle of inclination of resultant  $\theta = \tan^{-1} \left[ \frac{\sum F_V}{\sum F_H} \right]$
6. If the force moment system is converted into a single force, coordinate position is given by

$$\sum M_o = R \times x$$

$$\sum M_o = \sum F_v \times x$$

$$\sum M_o = \sum F_H \times y$$

A plate is acted upon by three forces and two couples as shown in fig. determine the resultant of these force couple system and find co-ordinate x of the point on the x axis through which the resultant is passed



Given

Three force  $1.5KN, 2KN, 3KN$

Two couple  $100N.m$   $80 N.m$

To find

Resultant force, location

Soln:

$$\text{Resultant force } R = \sqrt{(\sum F_H)^2 + (\sum F_V)^2}$$

Sum of horizontal

$$\sum F_H = 0$$

$$\sum F_H = 1.5 - 3$$

$$\sum F_H = -1.5KN$$

Sum of vertical force  $\sum F_V = 0$

$$\sum F_V = -2 KN$$

$$\text{Resultant } R = \sqrt{(\sum F_H)^2 + (\sum F_V)^2}$$

$$R = \sqrt{[-1.5]^2 + [-2]^2}$$

$$R = 2.5KN$$

$$\theta = \tan^{-1} \left[ \frac{\sum F_V}{\sum F_H} \right] = \tan^{-1} \left[ \frac{-2}{-1.5} \right]$$

$$\theta = 53.13^\circ$$

To locate the resultant

By varignon's Theorem  $\downarrow + \uparrow -$

$$\sum M_o = R \times x \text{ and } \sum M_o = \sum F_y \times x$$

$$\sum M_o = [3 \times 0.3] + [-2 \times 0.5] + [-1.5 \times 0.2] + [-0.1] + [-0.08] = 0$$

$$\sum M_o = -0.58 \text{ KN.M}$$

$$\sum M_o = 0.58 \text{ KN.M [clock wise]}$$

The co-ordinate x of the point through which the resulted passes is given by

$$\sum M_o = \sum F_y \times x \qquad x = \frac{0.58}{2}$$

$$0.58 = 2 \times x$$

$$x = 0.29 \text{ m}$$

$$x = 290 \text{ mm}$$

we want to find the intersection

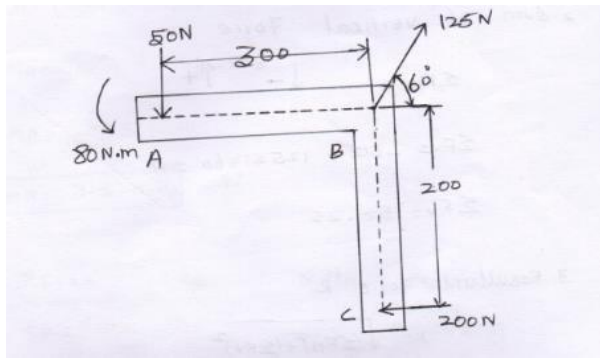
$$\sum M_o = \sum F_H \times y$$

$$0.581.5 \times y$$

$$y = 0.387 \text{ m}$$

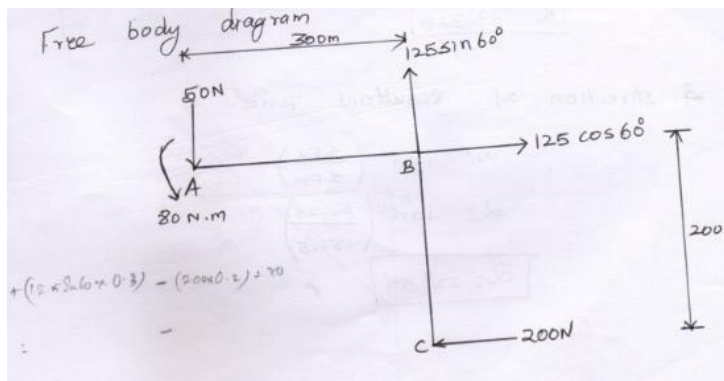
The three forces and a couple shown below are applied to an angel bracket

- (i) Find the Resultant of this system of forces
- (ii) Locate the points where the line of action of the resultant intersects line AB and the line BC



Soln

Free body diagram



1. Sum of Horizontal force

$$\sum F_H = 0 \quad \begin{array}{c} + \\ \rightarrow \leftarrow \\ - \end{array}$$

$$\sum F_H = +125 \cos 60 - 200 = 0$$

$$\sum F_H = -137.5 N$$

2. Sum of Vertical Force

$$\sum F_V = 0 \quad \begin{array}{c} \downarrow - \uparrow + \end{array}$$

$$\sum F_V = -50 + 125 \sin 60 = 0$$

$$\sum F_V = 58.25$$

3. Resultant force 'R'

$$R = \sqrt{(\sum F_H)^2 + (\sum F_V)^2}$$

$$R = \sqrt{[-137.5]^2 + [58.23]^2}$$

$$R = 149.32N$$

4. Direction of Resultant force  $\alpha$

$$\alpha = \tan^{-1}\left(\frac{\sum F_V}{\sum F_H}\right)$$

$$\alpha = \tan^{-1}\left(\frac{58.25}{137.5}\right)$$

$$\alpha = 22^\circ 57'$$

Location of Resultant Force:

By Varignon's Theorem

$$\sum M_A = \sum F_V \times x \text{ and } \sum M_A = \sum F_H \times y$$

$$\sum M_A = (200 \times 0.2) + (-125 \sin 60 \times 0.3) - 80 \times 0$$

$$\sum M_A = 40 - 32.47 - 80$$

$$\sum M_A = -72.47 \text{ N.m}$$

$$\sum M_A = \sum F_V \times x$$



$$7.5 = 58.25 \times x$$

$$x = 7.5/58.25 = 0.12 \text{ m}$$

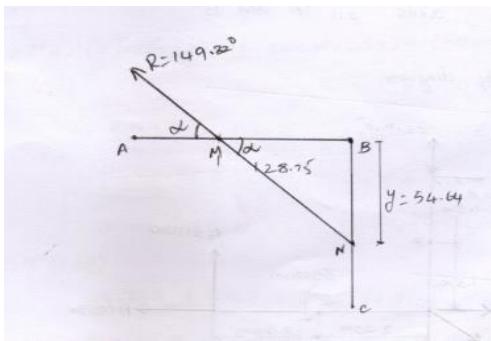
$$x = 128.75 \text{ mm}$$

$$\sum M_A = \sum F_v \times y$$

$$7.5 = 137.25 \times y$$

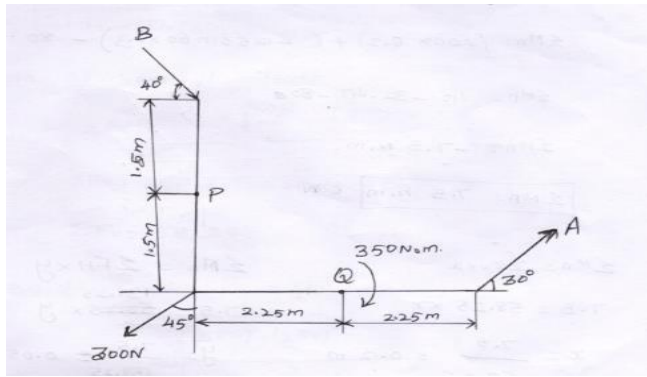
$$y = 7.5/137.25 = 0.05 \text{ m}$$

$$y = 54.64 \text{ mm}$$



Problem:

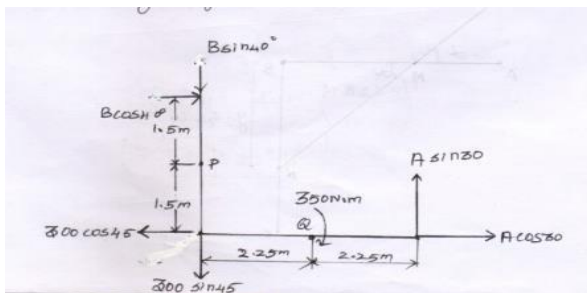
A system of forces acts as shown in fig. find the magnitude of A and B so that resultant of the force system passes through P and Q



To Find:

Forces acts on A and B

Soln: Free body diagram



The resultant forces passes through P and Q is moment About P is zero and also moment about Q=0

It only means that the algebraic sum of moment about P and Q is equal to zero

$$\sum M_P = 0 \quad \downarrow + \quad \uparrow -$$

$$\begin{aligned} \sum M_P &= (+B \cos 40 \times 1.5) \\ &+ (300 \cos 45 \times 1.5) + 350 \\ &+ (-A \sin 30 \times 4.5) + (-A \cos 30 \times 1.5) = 0 \end{aligned}$$

$$\sum M_P = 1.149 B + 318.19350 - 2.25A - 1.29$$

$$\sum M_P = 1.49B + 668.19 - 3.54A = 0$$

$$-3.54A + 1.149B = -668.19 \text{ _____} > (1)$$

$$\Sigma M_Q = 0 \quad \downarrow + \uparrow -$$

$$\Sigma M_Q = (B \cos 40 \times 3) + (-B \sin 40 \times 2.25) + (-300 \sin 45 \times 2.25) + 350 + (-A \sin 30 \times 2.25) = 0$$

$$2.29B - 1.44B - 477 + 350 - 1.125A = 0$$

$$0.85B - 127 - 1.125A = 0$$

$$-1.25A + 0.85B = 127 \text{ -----} \rightarrow (2)$$

Solve 1&2

$$-3.54A + 1.149B = -668.19 \text{ ---} (1)$$

$$-1.125A + 0.85B = 127 \text{ -----} (2)$$

$$(1) \times 1.25 \Rightarrow -3.982A + 1.292B = -751.7$$

$$(2) \times 3.54 \Rightarrow 3.982A + (-) 3.009B = < - > 449.58$$

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$$-171B = -1201.29$$

$$B = (-1201.29)/(-1.71)$$

$$B = 702.508N$$

B Value substituting in Eqn (1)

$$-3.54A + 1.149 \times 702.508 = -668.19$$

$$-3.54A + 807.182 = -668.19$$

$$-3.54A = -668.19 - 807.182$$

$$-3.54A = -1475.37$$

$$A = (-1475.37)/(-3.54)$$

$$A = 416.77 \text{ N}$$

Result:-

$$\text{Force on A} = 416.77 \text{ N}$$

$$\text{Force on B} = 702.508 \text{ N}$$

Take moment about 'A'

$$\sum M_A = 0$$

$$\sum M_A = (500 \times 11) + (-200 \times 7) + (1200 \times 5) + (-300 \times 2)$$

$$\sum M_A = 5500 = 1400 + 6000 - 600$$

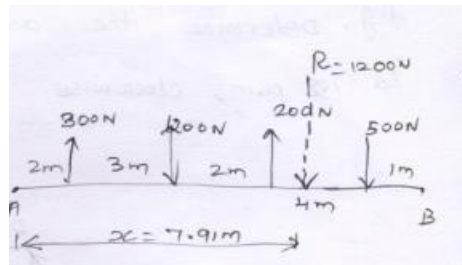
$$\sum M_A = 9500 \text{ N.m}$$

By varignon's theorem

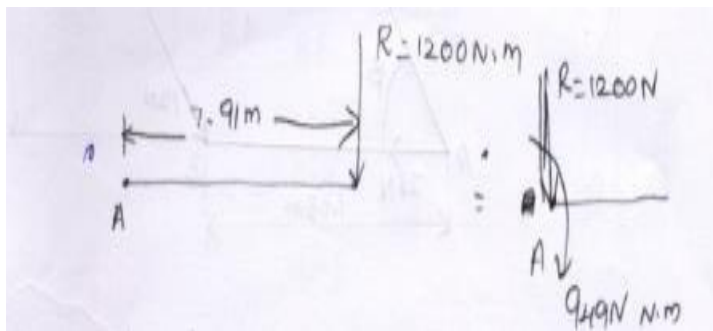
$$\sum M_A = R \times x$$

$$9500 = 1200 \times x$$

$$x = 7.91 \text{ m}$$



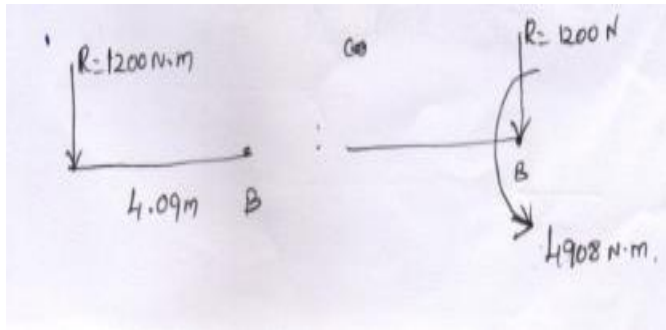
Force couple systemant 'A'



$$\text{Couple at A} = 1200 \times 7.91$$

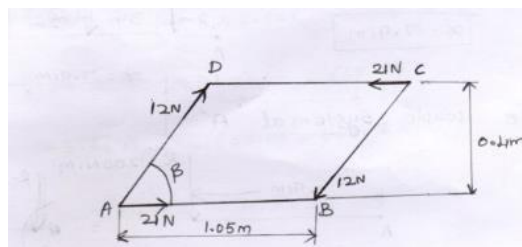
$$A = 9492 \text{ N.m}$$

Couple system at B



Problem:

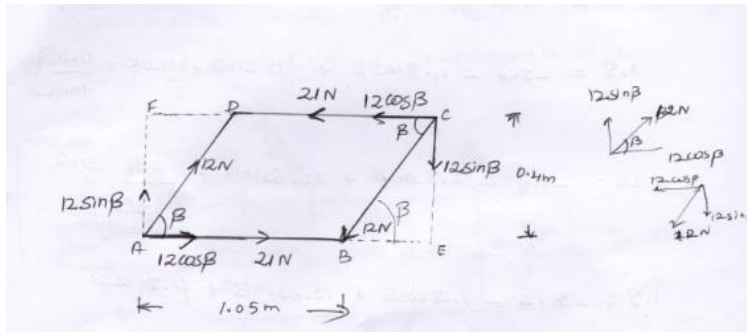
A plate ABCD in the shape of parallelogram is acted upon the two couples, as shown in the fig. Determine the angle B if the resultant couple is 1.8 N.m clockwise



Given:

Resultant couple = 1.8 N.m

Free body diagram



Distance of  $AE = AB + BE$

$$AB = 1.05 \text{ m}$$

To find BE

$$\tan \beta = \frac{CE}{BE} = \frac{0.4}{BE}$$

$$BE = 0.4 / \tan \beta$$

$$AE = AB + BE$$

$$AE = 1.05 + \frac{0.4}{\tan \beta}$$

Given the resultant couple  $\sum M_A = 1.8 \text{ N.M}$

Take moment about A

$$\sum M_A = [-21 \times 0.4] + [-12 \cos \beta \times 0.4] + [12 \sin \beta \times AE]$$

$$\sum M_A = 1.8 \text{ N.M}$$

$$1.8 = -8.4 - 4.8 \cos \beta + 12 \sin \beta \times \left[1.05 + \frac{0.4}{\tan \beta}\right]$$

$$1.8 = -8.4 - 4.8 \cos \beta + 12.6 \sin \beta + \frac{4.8}{\frac{\sin \beta}{\cos \beta}} \sin \beta$$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$1.8 = -8.4 - 4.8 \cos\beta + 12.6 \sin\beta + 4.8 \cos\beta$$

$$1.8 + 8.4 = -4.8 \cos\beta + 12.6 \sin\beta + 4.8 \cos\beta$$

$$10.2 = 12.6 \sin\beta$$

$$\sin\beta = \frac{10.2}{12.6}$$

$$B = \sin^{-1}\left(\frac{10.2}{12.6}\right) \quad B = 54^\circ$$