DFA (DETERMINISTIC FINITE AUTOMATA)

o   DFA refers to deterministic finite automata. Deterministic refers to the uniqueness of the computation. The finite automata are called deterministic finite automata if the machine is read an input string one symbol at a time.

o   In DFA, there is only one path for specific input from the current state to the next state.

o   DFA does not accept the null move, i.e., the DFA cannot change state without any input character.

o   DFA can contain multiple final states. It is used in Lexical Analysis in Compiler.

In the following diagram, we can see that from state q0 for input a, there is only one path which is going to q1. Similarly, from q0, there is only one path for input b going to q2.
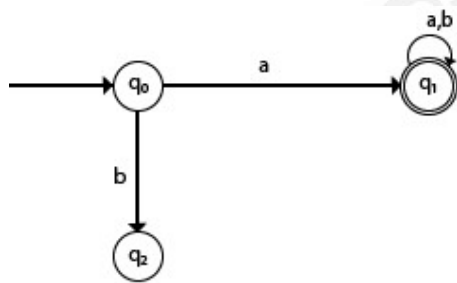

Fig:- DFA

Formal Definition of DFA

A DFA is a collection of 5-tuples same as we described in the definition of FA.

1. Q: finite set of states
2. $\sum$: finite set of the input symbol
3. q0: initial state
4. F: **final** state
5. δ: Transition function

Transition function can be defined as:

1. δ: Q x $\sum$→Q

Graphical Representation of DFA

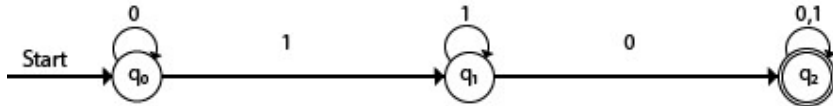A DFA can be represented by digraphs called state diagram. In which:

1. The state is represented by vertices.

2. The arc labeled with an input character show the transitions.

3. The initial state is marked with an arrow.

4. The final state is denoted by a double circle.

Example :

1. Q = {q0, q1, q2}
2. Σ = {0, 1}
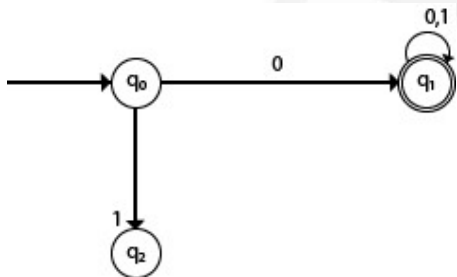3. q0 = {q0}
4. F = {q2}

Solution:

Transition Diagram:

Transition Table:

Present State	Next state for Input 0	Next State of Input 1
→q0	q0	q1
q1	q2	q1
*q2	q2	q2

Example :

DFA with Σ = {0, 1} accepts all starting with 0.
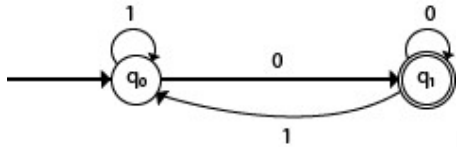
Solution:

Explanation:

- In the above diagram, we can see that on given 0 as input to DFA in state q0 the DFA changes state to q1 and always go to final state q1 on starting input 0. It can accept 00, 01, 000,

001....etc. It can't accept any string which starts with 1, because it will never go to final state on a string starting with 1.

Example :

DFA with $\sum$ = {0, 1} accepts all ending with 0.

Solution:

Explanation:

In the above diagram, we can see that on given 0 as input to DFA in state q0, the DFA changes state to q1. It can accept any string which ends with 0 like 00, 10, 110, 100....etc. It can't accept any string which ends with 1, because it will never go to the final state q1 on 1 input, so the string ending with 1, will not be accepted or will be rejected.
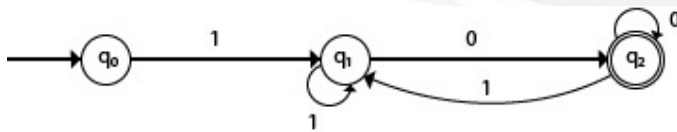
 Examples of DFA

Example :

Design a FA with $\sum$ = {0, 1} accepts those string which starts with 1 and ends with 0.

Solution:

The FA will have a start state q0 from which only the edge with input 1 will go to the next state.

In state q1, if we read 1, we will be in state q1, but if we read 0 at state q1, we will reach to state q2 which is the final state. In state q2, if we read either 0 or 1, we will go to q2 state or q1 state respectively. Note that if the input ends with 0, it will be in the final state.

Example :

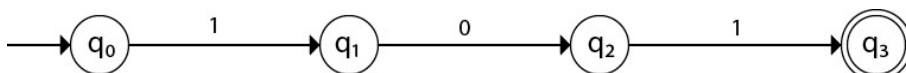Design a FA with $\sum$ = {0, 1} accepts the only input 101.
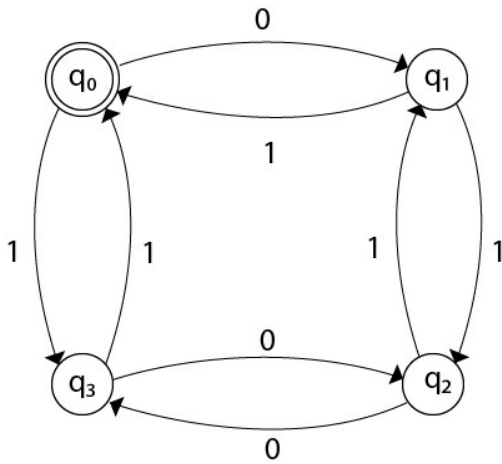
Solution:

Fig: FA

In the given solution, we can see that only input 101 will be accepted. Hence, for input 101, there is no other path shown for other input.

Example :

Design FA with $\sum = \{0, 1\}$ accepts even number of 0's and even number of 1's.

Solution:

This FA will consider four different stages for input 0 and input 1. The stages could be:

Here q0 is a start state and the final state also. Note carefully that a symmetry of 0's and 1's is maintained. We can associate meanings to each state as:

q0:	state	of	even	number	of	0's	and	even	number	of	1's.
q1:	state	of	odd	number	of	0's	and	even	number	of	1's.
q2:	state	of	odd	number	of	0's	and	odd	number	of	1's.

q3: state of even number of 0's and odd number of 1's.

Example 4:

Design FA with $\sum = \{0, 1\}$ accepts the set of all strings with three consecutive 0's.

Solution:

The strings that will be generated for this particular languages are 000, 0001, 1000, 10001, ... in which 0 always appears in a clump of 3. The transition graph is as follows:
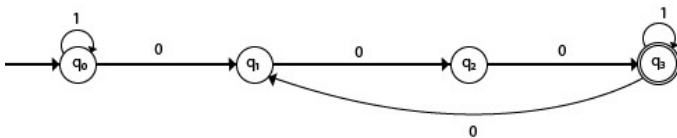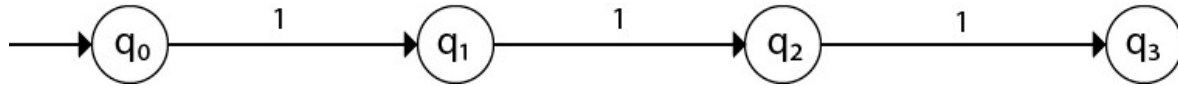
Note that the sequence of triple zeros is maintained to reach the final state.
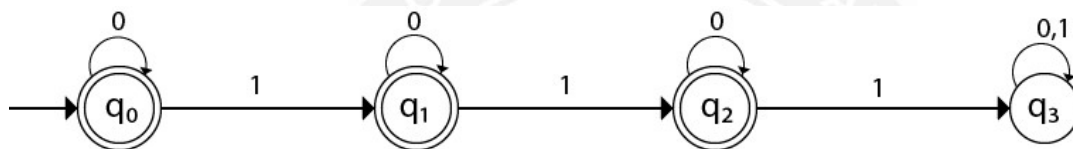
Example 5:

Design a DFA L(M) = {w | w ε {0, 1}*} and W is a string that does not contain consecutive 1's.

Solution:

When three consecutive 1's occur the DFA will be:

Here two consecutive 1's or single 1 is acceptable, hence

The stages q0, q1, q2 are the final states. The DFA will generate the strings that do not contain consecutive 1's like 10, 110, 101,..... etc.

Example 6:

Design a FA with $\sum$ = {0, 1} accepts the strings with an even number of 0's followed by single 1.

Solution:

The DFA can be shown by a transition diagram as: