

Structural Steel Framing

4.1 Design a purlin steel roof truss

Example:1

Design a purlin steel roof truss to suit the following data,

Span of the truss = 10m

Type of truss = pan type

Roof cover = Galvanization corrugated (GC) sheeting

Materials = Rolled steel angles

Spacing of roof truss = 4.5m

Wind pressure = 1 kN/m²

Draw the elevation of the roof truss and the details of joints.

Solution:

Step:1 Dimension of truss

Central rise = span/4

= 10/4

= 2.5m

Purlins are provided at intervals of 1.863m on the principal rafter

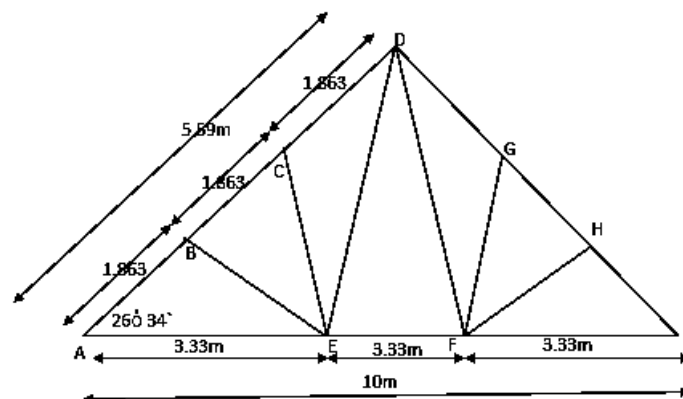


Fig.4.1 Roof truss

Step:2 Design of purlin

For continuous purlin, the max factored bending moment and shear force are computed as follow,

$$\begin{aligned} M &= (1.5 \times 1.305 \times 4.5^2) / 10 \\ &= 3.96 \text{ KNm} \end{aligned}$$

$$\begin{aligned} V &= (1.5 \times 1.305 \times 4.5) / 2 \\ &= 4.4 \text{ KN} \end{aligned}$$

Adopt ISA 100x75x8mm having section properties given below,

$$\begin{aligned} Z_x &= (4.38 \times 10^4) \text{ mm}^3 \\ D &= 100 \text{ mm} \\ b &= 75 \text{ mm} \\ t &= 8 \text{ mm} \end{aligned}$$

IS 800:2007 clause 3.7,

(a) Check for section classification is done by computed the ratios,

$$\begin{aligned} (b/t) &= 75/8 \\ &= 9.37 < 9.4 \end{aligned}$$

Hence the section considered as plastic .

(b) Check for shear capacity

$$\begin{aligned} A_v &= 100 \times 8 \\ &= 800 \text{ mm}^2 \end{aligned}$$

clause 8.4.1,

$$\begin{aligned}
 (A_v f_y w/\sqrt{3} \gamma_{mo}) &= (800 \times 250) / (\sqrt{3} \times 1.10 \times 10^3) \\
 &= 105 \text{ KN} > 4.40 \text{ KN}
 \end{aligned}$$

The shear capacity of the section is very large compared to the applied shear force.

(c) Check for moment capacity

$$\begin{aligned}
 M_d &= (\beta_b Z_x f_y) / \gamma_{mo} \\
 &= (1 \times 4.38 \times 10^4 \times 250) / (1.1 \times 10^6) \\
 M_d &= 9.95 \text{ KNm} > 3.96 \text{ KNm}
 \end{aligned}$$

Step:3 Load on truss

(a) Dead load

Sloping length of rafter,

$$\begin{aligned}
 AD &= \sqrt{5^2 + 2.5^2} \\
 &= 5.59 \text{ m}
 \end{aligned}$$

Spacing of trusses = 4.5m c/c

Weight of GC sheeting on half truss (plan area) at 0.18 KN/m²

$$\begin{aligned}
 &= 4.5 \times 5 \times 0.18 \\
 &= 4.05 \text{ KN}
 \end{aligned}$$

Weight of purlins (4nos) at 0.10 KN/m

$$\begin{aligned}
 &= 4 \times 0.1 \times 4.5 \\
 &= 1.8 \text{ KN}
 \end{aligned}$$

Self weight of roof truss = (span/300) + 0.05

$$\begin{aligned}
 &= (10/300) + 0.05 \\
 &= 0.083 \text{ KN/m}^2
 \end{aligned}$$

Weight of half roof truss = 0.083 x 5 x 4.5

$$= 1.86 \text{ KN}$$

$$\text{Total load on half truss} = 4.05 + 1.8 + 1.86$$

$$= 7.71 \text{ KN}$$

Dead load on intermediate- panel point

$$= 7.71/3$$

$$= 2.57 \text{ KN}$$

$$\text{Dead load on end panel point} = 2.57/2$$

$$= 1.285 \text{ KN}$$

(b) Live loads

$$\text{Live load on half truss} = 0.52 \times 5 \times 4.5$$

$$= 11.7 \text{ KN}$$

Live load on intermediate panel point

$$= 11.7/3$$

$$= 3.9 \text{ KN}$$

Live load on end panel point = 3.9/2

$$= 1.95 \text{ KN}$$

(c) Wind loads

Maximum wind load acting perpendicular to the sloping surface

$$= 0.9 \times 4.5 \times 5.59$$

$$= -22.63 \text{ KN}$$

Wind load on intermediate- panel point

$$= -(22.68/3)$$

$$= -7.5 \text{ KN}$$

$$\begin{aligned}\text{Wind load on end panel point} &= -(7.5/2) \\ &= 3.75 \text{ KN}\end{aligned}$$

Step:4 Design of truss members

(a) Members AB, BC, CD

$$\begin{aligned}\text{Maximum service load compressive force} \\ &= 36.17 \text{ KN}\end{aligned}$$

$$\begin{aligned}\text{Maximum factored compressive force} \\ &= 1.5 \times 36.17 \\ &= 54.25 \text{ KN}\end{aligned}$$

$$\begin{aligned}\text{Maximum service load tensile force} \\ &= 22.95 \text{ KN}\end{aligned}$$

$$\begin{aligned}\text{Maximum factored tensile force} \\ &= 1.5 \times 22.95 \\ &= 34.42 \text{ KN}\end{aligned}$$

$$\text{Length (L)} = 1.863 \text{ m}$$

$$\text{Effective length (KL)} = 1.304 \text{ m}$$

Try two angle ISA 50x50x6mm placed back to back

$$\text{Area (A)} = 1136 \text{ mm}^2$$

$$\text{Minimum radius of gyration } (\gamma_{\min}) = 15.1 \text{ mm}$$

$$\text{Slenderness ratio} = (KL/\gamma_{\min})$$

$$= 1304/15.1$$

$$= 86.3 < 180$$

Stress reduction factor x for column buckling class (c) corresponding to the slenderness

$$\text{ratio } 86.3 \text{ and } f_y = 250 \text{ N/mm}^2$$

$$x = 0.56$$

∴ Design compressive stress is computed as,

$$\begin{aligned} F_{cd} &= x f_y / \gamma_{mo} \\ &= (0.56 \times 250) / 1.25 \\ &= 112 \text{ N/mm}^2 \end{aligned}$$

Design compressive force is given by,

$$\begin{aligned} P_d &= [A f_{cd}] \\ &= (1136 \times 112) / 1000 \\ &= 127 \text{ KN} > 54.25 \text{ KN} \end{aligned}$$

(b) Member DE

$$\begin{aligned} \text{Maximum service load tension} \\ &= 12.83 \text{ KN} \end{aligned}$$

$$\begin{aligned} \text{Maximum factored load tension} \\ &= 1.5 \times 12.83 \\ &= 19.24 \text{ KN} \end{aligned}$$

$$\begin{aligned} \text{Maximum service load compression} \\ &= 9.57 \text{ KN} \end{aligned}$$

$$\begin{aligned} \text{Maximum factored load compression} \\ &= 1.5 \times 9.57 \\ &= 14.35 \text{ KN} \end{aligned}$$

$$\text{Effective length} = 3\text{m}$$

Try a single angle ISA 50x50x5mm connected by 6mm thick gusset plate the junction with

two bolts of 16mm at 50mm.

$$\text{Gross area (A)} = 479\text{mm}^2$$

$$\gamma_{\min} = 15.2\text{mm}$$

Using 16mm dia bolts,

$$A_{nc} = [50-18]5$$

$$= 160\text{mm}^2$$

$$A_{go} = [50-5]5$$

$$= 225\text{mm}^2$$

$$A_g = 479\text{mm}^2$$

(a) Strength governed by rupture of critical section

$$T_{dn} = [0.9 A_{nc} f_y / \gamma_{mi}] + [\beta A_{go} f_y / \gamma_{mo}]$$

where,

$$\beta = 1.4 - 0.076(w/t)(f_y/f_u)(b_s/L_c)$$

$$= 1.4 - 0.076(50/5)(250/410)(50+25/50)$$

$$\beta = 0.70$$

$$T_{dn} = [0.9 \times 160 \times 410 / 1.25] + [0.7 \times 225 \times 250 / 1.10] \times 10^3$$

$$= 83.02 \text{ KN} = T_0$$

(b) Strength governed by yielding of gross section

$$T_{dg} = A_g f_y / \gamma_{mo}$$

$$= (470 \times 250 \times 10^3) / 1.10$$

$$= 108.8 \text{ KN}$$

(c) Strength governed by block shear

$$A_{vg} = 5[50+50]$$

$$= 500\text{mm}^2$$

$$A_{vn} = 5[50+50] - [1.5 \times 18]$$

$$= 473\text{mm}^2$$

$$A_{tg} = [5 \times 25]$$

$$= 125\text{mm}^2$$

$$A_{tn} = [(5 \times 25) - (0.5 \times 18)]$$

$$= 116\text{mm}^2$$

The block shear strength is the smaller of the value of T_{db1} and T_{db2} as computed using

the equation given below,

$$T_{db1} = [A_{vg} f_y / \sqrt{3} \gamma_{mo}] + [0.9 A_{tn} f_u / \gamma_{mi}]$$

$$= [(500 \times 250) / (\sqrt{3} \times 1.1)] + [(0.9 \times 116 \times 410) / 1.25]$$

$$= 99.92 \text{ KN}$$

$$T_{db2} = [0.9 A_{vn} f_u / \sqrt{3} \gamma_{mi}] + [A_{tg} f_y / \gamma_{mo}]$$

$$= [(0.9 \times 473 \times 410) / (\sqrt{3} \times 1.25)] + [(125 \times 250) / 1.10]$$

$$= 109.12 \text{ KN}$$

$$\text{Hence, } T_{db} = 109.12 \text{ KN}$$

The design shear strength is the least of the three value computed under (a)(b)(c) , which are 108.8 KN, 83.02KN, 109.12KN.

The design tensile strength of angle = 83.02KN > 19.24 KN

(C) Member BC ,EB

$$\text{Service load compressive force} = 6.95 \text{ KN}$$

$$\begin{aligned} \text{Factored compressive force} &= 1.5 \times 6.95 \\ &= 10.42 \text{ KN} \end{aligned}$$

$$\text{Service load tensile force} = 6.38 \text{ KN}$$

$$\begin{aligned} \text{Factored tensile force} &= 1.5 \times 6.38 \\ &= 9.57 \text{ KN} \end{aligned}$$

$$\begin{aligned} \text{Effective length (kL)} &= 0.7 \times 1.6 \\ &= 1.12 \text{ m} \end{aligned}$$

Use minimum size angle ISA 50x50x5mm,

$$\text{Area (A)} = 479 \text{ mm}^2$$

$$\gamma_{\min} = 9.7 \text{ mm}$$

$$\begin{aligned} \text{Slenderness ratio } (\lambda) &= 1120/9.7 \\ &= 115 \end{aligned}$$

The stress reduction factor x corresponding to $f_y = 250 \text{ N/mm}^2$ and $\lambda = 115$

$$x = 0.39$$

Design compressive stress is computed as,

$$\begin{aligned} f_{cd} &= x f_y / \gamma_{mo} \\ &= (0.39 \times 250) / 1.25 \\ &= 78 \text{ N/mm}^2 \end{aligned}$$

Design compressive force is given by ,

$$\begin{aligned} P_d &= A f_{cd} \\ &= [479 \times 78] / 1000 \\ &= 37.36 \text{ KN} > 10.42 \text{ KN} \end{aligned}$$

(d) Member EA and EF

$$\text{Max service load tension} = 32.21 \text{ KN}$$

$$\begin{aligned}\text{Factored tension} &= 1.5 \times 32.21 \\ &= 748.31 \text{ KN}\end{aligned}$$

$$\begin{aligned}\text{Max service load compression} &= 18.84 \text{ KN}\end{aligned}$$

$$\begin{aligned}\text{Factored compression} &= 1.5 \times 18.84 \\ &= 28.26 \text{ KN}\end{aligned}$$

$$\text{Length of member} = 3.33 \text{ m}$$

$$\begin{aligned}\text{Effective length (kL)} &= 0.7 \times 3.33 \\ &= 2.331 \text{ m}\end{aligned}$$

Try minimum two angle ISA 50x50x6mm connect by gusset plate 6mm thick with two 16mm dia bolts spaced at 50mm

$$\begin{aligned}\text{Area (A)} &= 2 \times 598 \\ &= 1136 \text{ mm}^2\end{aligned}$$

$$\gamma_{\min} = 15.1 \text{ mm}$$

i) Design strength due to yielding of cross section ,

$$\begin{aligned}T_{dj} &= A_g f_y / \gamma_{mo} \\ &= [(1136 + 250) / 1.10] \times 10^{-3} \\ &= 258 \text{ KN}\end{aligned}$$

ii) Design strength governed by tearing at net section,

$$T_{dn} = \alpha A_n f_u / \gamma_{mi}$$

Assume a single line of 16mm dia bolts of two number spaced 50mm apart $x=0.6$

$$A_n = [(50-18)(6 \times 2)]$$

$$= 384 \text{ mm}^2$$

$$T_{dn} = [(0.6 \times 384 \times 410) / 1.25] \times 10^{-3}$$

$$= 75.5 \text{ kN} > 48.31 \text{ kN}$$

Hence, the angle section designed for the truss can safely resist the factored loads.

