4.7 POTENTIAL GRADIENT

Under operating conditions, the insulation of a cable is subjected to electrostatic forces. This is known as dielectric stress. The dielectric stress at any point in a cable is infact the potential gradient (or electric intensity) at that point.

Consider a single core cable with core diameter d and internal sheath diameter D. The electric intensity at a point x metres from the centre of the cable is

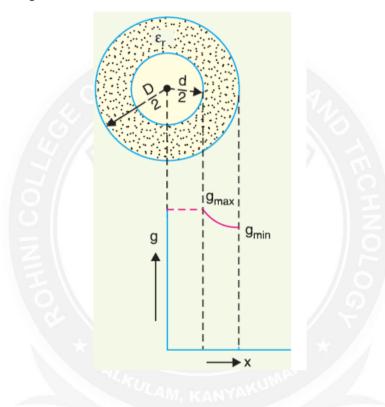


Figure 4.7.1 Potential Gradient – Cable

[Source: "Principles of Power System" by V.K.Mehta Page: 277]

$$E_x = \frac{Q}{2\pi \, \varepsilon_o \, \varepsilon_r \, x}$$
 volts/m

By definition, electric intensity is equal to potential gradient. Therefore, potential gradient g at a point x metres from the centre of cable is

$$g = E_{x}$$

$$g = \frac{Q}{2\pi \,\varepsilon_{o} \,\varepsilon_{r} \,x} \text{ volts/m}$$
.....(i)

$$V = \frac{Q}{2\pi\varepsilon_{o}\varepsilon_{r}}\log_{e}\frac{D}{d} \text{ volts}$$

$$Q = \frac{2\pi\varepsilon_{o}\varepsilon_{r}V}{\log_{e}\frac{D}{d}}$$
.....(ii)

Substituting the value of Q from exp. (ii) in exp. (i), we get,

$$g = \frac{2\pi \varepsilon_o \varepsilon_r V}{\frac{\log_e D/d}{2\pi \varepsilon_o \varepsilon_r x}} = \frac{V}{x \log_e \frac{D}{d}} \text{ volts/m}$$
.....(iii)

It is clear from exp. (*iii*) that potential gradient varies inversely as the distance x. Therefore, potential gradient will be maximum when x is minimum i.e., when x = d/2 or at the surface of the conductor. On the other hand, potential gradient will be minimum at x = D/2 or at sheath surface.

Maximum potential gradient is,

$$g_{max} = \frac{2V}{d \log_e \frac{D}{d}} \text{ volts/m}$$
 [Putting $x = d/2$ in exp. (iii)]

Minimum potential gradient is,

$$g_{min} = \frac{2V}{D \log_e \frac{D}{d}}$$
 volts/m