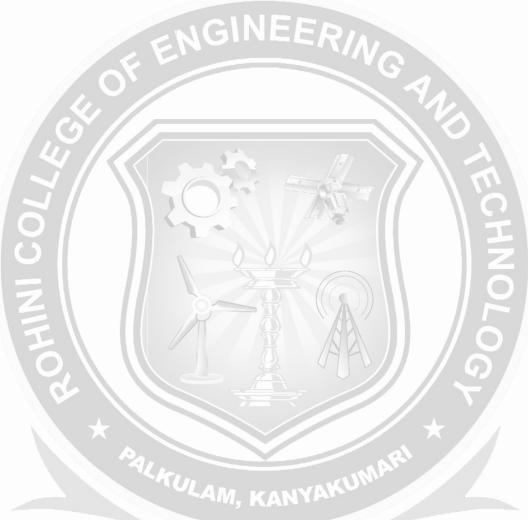
QUANTIZATION DUE TO TRUNCATION AND ROUNDIND, QUANTIZATION NOISE



Quantization:

- *Discuss the various methods of quantization.
- *Derive the expression for rounding and truncation errors
- * Discuss in detail about Quantization error that occurs due to finite word length of registers.

The common methods of quantization are

- 1. Truncation
- 2. Rounding

1. Truncation

- The abrupt termination of given number having a large string of bits (or)
- Truncation is a process of discarding all bits less significant than the LSB that is retained.
- Suppose if we truncate the following binary number from 8 bits to 4 bits, we obtain
 - 0.00110011 to 0.0011

(8 bits) (4 bits)

- 1.01001001 to 1.0100 (8 bits) (4 bits)
- When we truncate the number, the signal value is approximated by the highest quantization level that is not greater than the signal.
- 2. Rounding (or) Round off

Rounding is the process of reducing the size of a binary number to the last discountry size of 'b' bits such that the rounded b-bit number is closest to the original unquantised number.

Error Due to truncation and rounding:

- While storing (or) computation on a number we face registers length problems. Hence given number is quantized to truncation (or) round off.
 - i.e. Number of bits in the original number is reduced register length.

Truncation error in sign magnitude form:

Consider a 5 bit number which has value of

 0.11001_2 \rightarrow (0.7815)₁₀

This 5 bit number is truncated to a 4 bit number

 0.1100_{2} \rightarrow (0.75)₁₀

i.e. 5 bit number $\rightarrow 0.11001$ has '1' bits

4 bit number $\rightarrow 0.1100$ has 'b' bits

0.1100 - 0.11001Truncation error, e_t

-0.00001 \rightarrow (-0.03125)₁₀

Here original length is '1' bits. (1=5). The truncated length is 'b' bits.

2-b-2-1 The truncation error, e_t

 $-(2^{-1}-2^{-b})$ $-(2^{-5}-2^{-4})$

The truncation error for a positive number is

 $-(2^{-b}-2^{-l}) \le e_{\star} \le 0$ → Non causal

The truncation error for a negative number is $0 \le e_t \le (2^{-b} - 2^{-l})$ → Causal

Truncation error in two's complement:

- For a positive number, the truncation results in a smaller number and hence remains same as in the case of sign magnitude form.
- For a negative number, the truncation produces negative error in two's complement

$$-(2^{-b}-2^{-l}) \le e_t \le (2^{-b}-2^{-l})$$

Round off error (Error due to rounding):

Let us consider a number with original length as '5' bits and round off length as '4' bits.

 $\xrightarrow{\text{Round off to}}$ 0.1101 0.11001

Now error due to rounding $e_r = \frac{2^{-b} - 2^{-l}}{2}$

b-Number of bits to the right of binary point after rounding Where

L→Number of bits to the right of binary point before rounding

Rounding off error for positive Number:

 $-\frac{2^{-b}-2^{-l}}{2} \le e_r \le 0$

Rounding off error for negative Number: DIMZE OUTSPREAD $0 \le e_r \le \frac{2^{-b} - 2^{-l}}{2}$

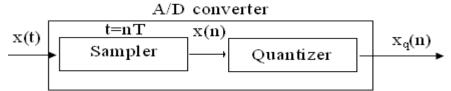
For two's complement

 $\frac{2^{-b} - 2^{-l}}{2} \le e_r \le \frac{2^{-b} - 2^{-l}}{2}$

Quantization Noise:

- *Derive the expression for signal to quantization noise ratio
- *What is called Quantization Noise? Derive the expression for quantization noise power.

Rohini College of Engineering and Technology



- The analog signal is converted into digital signal by ADC
- At first, the signal x(t) is sampled at regular intervals t=nT, where n=0,1,2... to create sequence x(n). This is done by a sampler.
- Then the numeric equivalent of each sample x(n) is expressed by a finite number of bits giving the sequence $x_q(n)$
- The difference signal $e(n) = x_q(n) x(n)$ is called quantization noise (or) A/D conversion noise.
- Let us assume a sinusoidal signal varying between +1 & -1 having a dynamic range 2
- ADC employs (b+1) bits including sign bit. In this case, the number of levels available for quantizing x(n) is 2^{b+1} .
- The interval between the successive levels is

$$q = \frac{2}{2^{b+1}} = 2^{-b}$$

Where $q \rightarrow$ quantization step size

If b=3 bits, then $q=2^{-3}=0.125$

