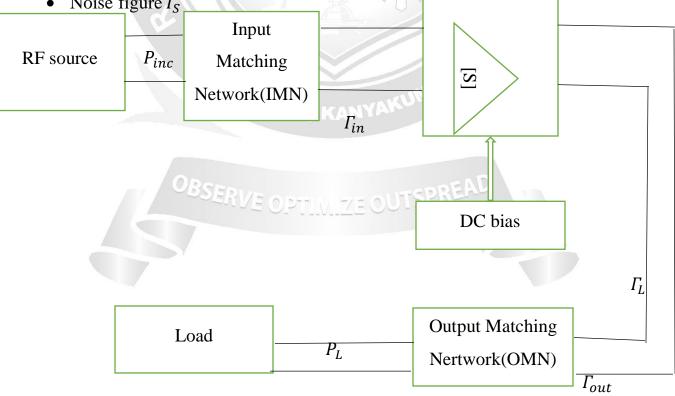
## **5.2 RF AMPLIFIERS:**

## **CHARACTERISTICS OF AMPLIFIERS:**

The most important and complex task is the amplification of an input signal through either a single or multistage transistor circuit. A generic single-stage amplifier configuration embedded between input and output matching networks, as shown in Fig 5.2.1.

Input and Output matching networks, are needed to reduce undesired reflections and thus improve the power flow capabilities. Interms of performance specifications, the following list constitutes a set of key amplifier parameters.

- Gain and gain flatness
- Operating frequency and bandwidth
- Output power
- Power supply requirements
- Input and output power reflections
- Noise figure  $\Gamma_S$



## Fig: 5.2.1 Generic amplifier system

i. Reflection Coefficient seen looking toward the load

$$\Gamma_L = \frac{Z_L - Z_O}{Z_L + Z_O}$$

ii. Reflection Coefficient seen looking toward the source

 $\Gamma_{S} = \frac{Z_{S} - Z_{O}}{Z_{S} + Z_{O}}$ iii. Input reflection Coefficient

 $\Gamma_{in} = S_{11} + \frac{S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L}$ iv. Output reflection Coefficient

$$\Gamma_{out} = S_{22} + \frac{S_{12} S_{21} \Gamma_S}{1 - S_{11} \Gamma_S}$$
  
From signal flow graph In figure,

$$b_{s} + a_{1}'\Gamma_{s} = b_{1}'$$

$$b_{s} = b_{1}' - a_{1}'\Gamma_{s}$$

$$b_{s} = b_{1}' \left[1 - \frac{a_{1}'}{b_{1}'}\Gamma_{s}\right]$$

$$b_{s} = b_{1}' \left[1 - \frac{b_{1}}{a_{1}}\Gamma_{s}\right]$$

$$b_{s} = b_{1}' \left[1 - \Gamma_{in}\Gamma_{s}\right] \qquad \dots \dots (1)$$

$$b_{1}' = \frac{b_{s}}{1 - \Gamma_{in}\Gamma_{s}} \qquad \dots \dots (2)$$

Incident power wave  $(P_{inc})$  associated with  $b_1'$  is given as,

$$P_{inc} = \frac{|b_1'|^2}{2}$$

$$P_{inc} = \frac{1}{2} \frac{|b_s|^2}{|1 - \Gamma_{in} \Gamma_s|^2} \qquad \dots \dots (3)$$

which is the power launched towards the amplifier,

$$\Gamma_{in} = 0 \& \Gamma_S \neq 0$$
$$P_{inc} = \frac{|b_s|^2}{2} \qquad \dots \dots (4)$$

The actual input power  $P_{in}$  is observed at the input terminal of the amplifier is composed of the incident & reflected power waves.

$$P_{in} = P_{inc} (1 - |\Gamma_{in}|^2)$$

$$P_{in} = \frac{1}{2} \frac{|b_s|^2}{|1 - \Gamma_{in} \Gamma_s|^2} (1 - |\Gamma_{in}|^2) \qquad \dots (5)$$

Maximum power transfer from the source to the amplifier is achieved if the input impedance is complex conjugate matched ( $Z_{in} = Z_v$ ) or, in terms of the reflection coefficients if  $\Gamma_{in} = \Gamma_S^*$ 

Under maximum power transfer condition, the available power  $P_A$  as,

$$P_{A} = P_{in}|_{\Gamma_{in} = \Gamma_{S}^{*}}$$

$$P_{A} = \frac{1}{2} \frac{|b_{S}|^{2}}{|1 - \Gamma_{in} \Gamma_{S}^{*}|^{2}} (1 - |\Gamma_{in}|^{2})|_{\Gamma_{in} = \Gamma_{S}^{*}}$$

$$P_{A} = \frac{1}{2} \frac{|b_{S}|^{2}}{|1 - |\Gamma_{S}^{*}|^{2}|^{2}} (1 - |\Gamma_{S}^{*}|^{2})$$

$$P_{A} = \frac{1}{2} \frac{|b_{S}|^{2}}{(1 - |\Gamma_{S}^{*}|^{2})} \dots (6)$$
Power delivered to the load is given by,  

$$P_{L} = \frac{1}{2} |b_{2}|^{2} (1 - |\Gamma_{L}^{*}|^{2}) \dots (7)$$
**TRANDUCER POWER GAIN**

$$G_{T} = \frac{p_{OWER delivered to the load}{available power from the source} \dots (1)$$

$$G_{T} = \frac{P_{L}}{P_{av(S)}} = \frac{P_{L}}{P_{A}} \dots (2)$$

$$P_{L} = \frac{1}{2} |b_{2}|^{2} (1 - |\Gamma_{L}^{*}|^{2}) \dots (3)$$

$$P_{A} = \frac{|b_{S}|^{2}}{(1 - |\Gamma_{S}^{*}|^{2})} \dots (4)$$
Sub equ (3) and (4) in equ (2),

 $G_T = \frac{\frac{1}{2} |b_2|^2 (1 - |\Gamma_L|^2)}{\frac{|b_S|^2}{(1 - |\Gamma_S|^2)}}$ 

The reflected wave at port 2 is  $b_2$ ,

By rearranging the above equation (6),

$$b_{2}(1 - S_{22} \Gamma_{L}) = a_{1}S_{21}$$
$$a_{1} = \frac{b_{2}(1 - S_{22}\Gamma_{L})}{S_{21}} \qquad \dots \dots (7)$$

The source reflection coefficient  $b_s$  is given by,

$$b_s = (1 - \Gamma_s \Gamma_{in}) a_1 \qquad \dots \dots (8)$$

The input reflection coefficient  $\Gamma_{in}$  is given by,

$$\Gamma_{in} = S_{11} + \frac{S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L} \qquad \dots \dots \dots (9)$$

By rearranging the equ (11) by,

$$\Gamma_{in} = \frac{S_{11} \left(1 - S_{22} \Gamma_L\right) + S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L}$$

To find 1-  $\Gamma_{S}\Gamma_{in}$ :

$$\begin{split} \Gamma_{S}\Gamma_{in} &= \frac{S_{11} \left(1 - S_{22} \Gamma_{L}\right)\Gamma_{S} + S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ 1 - \Gamma_{S}\Gamma_{in} &= 1 - \frac{S_{11} \left(1 - S_{22} \Gamma_{L}\right)\Gamma_{S} + S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ &= 1 - \frac{S_{11} \Gamma_{S} - S_{11} S_{22} \Gamma_{L} \Gamma_{S} + S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ &= \frac{\left(1 - S_{22} \Gamma_{L}\right) - S_{11} \Gamma_{S} - S_{11} S_{22} \Gamma_{L} \Gamma_{S} - S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ &= \frac{\left(1 - S_{22} \Gamma_{L}\right) - S_{11} \Gamma_{S} (1 - S_{22} \Gamma_{L}) - S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ &= \frac{\left(1 - S_{22} \Gamma_{L}\right) \left(1 - S_{11} \Gamma_{S}\right) - S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ &= \frac{\left(1 - S_{22} \Gamma_{L}\right) \left(1 - S_{11} \Gamma_{S}\right) - S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}} \\ \end{array}$$

To find  $b_s$ :

Sub equ (12) in equ (8),

From equ (8),  $b_{\rm s} = (1 - \Gamma_{\rm s} \Gamma_{\rm in}) a_1$  $b_{s} = \left[\frac{(1 - S_{22} \Gamma_{L})(1 - S_{11} \Gamma_{S}) - S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}}\right] a_{1} \dots \dots (13)$ Sub equ (7) in equ (13),  $b_{s} = \left[\frac{(1 - S_{22} \Gamma_{L})(1 - S_{11} \Gamma_{S}) - S_{12} S_{21} \Gamma_{L} \Gamma_{S}}{1 - S_{22} \Gamma_{L}}\right] \ge \frac{b_{2}(1 - S_{22} \Gamma_{L})}{S_{21}}$  $\frac{b_s}{b_2} = \frac{(1 - S_{22} \Gamma_L)(1 - S_{11} \Gamma_S) - S_{12} S_{21} \Gamma_L \Gamma_S}{S_{21}} \quad \dots \dots (14)$ To find  $\left|\frac{b_s}{b_s}\right|^2$ :  $\left|\frac{b_{s}}{b_{2}}\right|^{2} = \frac{|S_{21}|^{2}}{\left|(1 - S_{22}\Gamma_{s})(1 - S_{12}\Gamma_{s}) - S_{12}S_{21}\Gamma_{s}\Gamma_{s}\right|^{2}} \quad \dots \dots (15)$ To find  $G_T$ , From equ (5),  $G_T = \left|\frac{b_2}{b_1}\right|^2 (1 - |\Gamma_L|^2) (1 - |\Gamma_s|^2)$  $G_T = \frac{|S_{21}|^2 (1 - |\Gamma_L|^2) (1 - |\Gamma_S|^2)}{|(1 - S_{21} \Gamma_L)(1 - S_{11} \Gamma_S) - S_{12} S_{21} \Gamma_L \Gamma_S|^2}$  $G_T = \frac{|S_{21}|^2 (1 - |\Gamma_L|^2) (1 - |\Gamma_S|^2)}{|1 - S_{22} \Gamma_L|^2 |1 - \Gamma_S \Gamma_{in}|^2}$ 

#### **Problem 1:**

DESERVE OPTIMIZE OUTSPREAD

An amplifier has the following S-parameters :  $S_{11}=0.3 \perp -70$ ,  $S_{12}=0.2 \perp -10$ ,  $S_{21}=3.5 \perp 85$  and  $S_{22}=0.4 \perp -45$ . Furthermore, input side of the amplifier is connected to a voltage source with  $V_S = 5V \perp 0$  and the source impedance  $Z_S = 40$ ohm. The output is utilized to drive the antenna which has an impedance of  $Z_L = 73$ ohm. Assuming that the S-parameters of the amplifier are measured with reference to a  $Z_0 = 50$ ohm characteristic impedance, Calculate

- a) transducer gain, unilateral transducer gain, available gain, operating power gain.
- b) Power delivered to the load, available power and incident power to the amplifier.

### Given data:

S<sub>11</sub>=0.3 ∟ -70  $S_{12}=0.2 \bot -10$  $S_{21}=3.5 \bot 85$  $S_{22}=0.4 \sqcup -45$  $Z_S = 40 \text{ohm}$  $Z_L = 730hm$  $Z_0 = 50$  ohm  $V_S = 5V \sqcup 0$  $\Gamma_L = \frac{Z_L - Z_O}{Z_L + Z_O}$  $\Gamma_L = \frac{73 - 50}{73 + 50}$  $\Gamma_L = 0.187$  $\Gamma_S = \frac{Z_S - Z_0}{Z_S + Z_0}$  $\Gamma_S = \frac{40-50}{40+50}$  $\Gamma_{S} = -0.111$  $b_s = \frac{\sqrt{Z_0}}{Z_s + Z_0} \mathbf{V}_s$  $b_s = \frac{\sqrt{50}}{40+50}$  5  $b_s = 0.392$  $\Gamma_{in} = S_{11} + \frac{S_{12} S_{21 \Gamma_L}}{1 - S_{22} \Gamma_L}$ 

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$$\begin{split} & \Gamma_{in} = 0.3 \sqcup -70 + \frac{(0.2 \bot -10)(3.5 \bot 85)(0.187)}{1 - (0.4 \bot -45)(0.187)} \\ & \Gamma_{in} = 0.3 \sqcup -70 + \frac{(0.7 \bot 75)(0.187)}{1 - (0.0748 \bot -45)} \\ & \Gamma_{in} = 0.3 \sqcup -70 + \frac{(0.1309 \bot 75)}{1 - (0.0748 \bot -45)} \\ & \Gamma_{in} = 0.3 \sqcup -70 + 0.138 \bot 71.81 \\ & \Gamma_{in} = 0.209 \sqcup -45.98 \\ & \Gamma_{out} = S_{22} + \frac{S_{12}S_{21}\Gamma_S}{1 - S_{11}\Gamma_S} \\ & \Gamma_{out} = 0.4 \sqcup -45 + \frac{(0.2 \bot -10)(3.5 \bot 85)(-0.111)}{1 - (0.3 \bot -70)(-0.111)} \\ & \Gamma_{out} = 0.4 \sqcup -45 + \frac{(0.7 \bot 75)(-0.111)}{1 - 0.333 \bot -70} \\ & \Gamma_{out} = 0.4 \sqcup -45 + \frac{(0.0777 \bot 75)}{1 - 0.333 \bot -70} \\ & \Gamma_{out} = 0.4 \sqcup -45 + 0.0767 \sqcup 76.77 \\ & \Gamma_{out} = 0.445 \sqcup -53.42 \end{split}$$

# **a**) Transducer gain, unilateral transducer gain, available gain, operating power gain.

$$G_{T} = \frac{|S_{21}|^{2} (1 - |\Gamma_{L}|^{2}) (1 - |\Gamma_{s}|^{2})}{|1 - S_{11} \Gamma_{s}|^{2} |1 - \Gamma_{out} \Gamma_{L}|^{2}}$$

$$G_{T} = \frac{(3.5)^{2} (1 - (0.187)^{2}) (1 - (-0.111)^{2})}{|1 - (0.187)(0.445 \bot - 53.42)|^{2} |1 - (0.3 \bot - 70)(-0.111)|^{2}}$$

$$G_{T} = 12.556$$

$$G_{T}(dB) = 10 \ log_{10} (G_{T})$$

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$$G_{T}(dB) = 10.988 \ dB$$

$$G_{TU} = \frac{|S_{21}|^{2} (1 - |\Gamma_{L}|^{2}) (1 - |\Gamma_{s}|^{2})}{|1 - S_{22} \Gamma_{L}|^{2} |1 - S_{11} \Gamma_{S}|^{2}}$$

$$G_{TU} = 12.68$$

 $G_{TU}(dB) = 10 \ log_{10} \ (G_{TU})$   $G_{TU}(dB) = 10 \ log_{10} \ (12.68)$   $G_{TU}(dB) = 11.03 \ Db$   $G_A = \frac{|S_{21}|^2 \ (1 - |\Gamma_s|^2)}{|1 - S_{11} \ \Gamma_s|^2 \ (1 - |\Gamma_{out}|^2)}$   $G_A = 14.74$   $G_A(dB) = 10 \ log_{10} \ (G_A)$   $G_A(dB) = 10 \ log_{10} \ (14.74)$   $G_A(dB) = 10 \ log_{10} \ (14.74)$   $G_B = \frac{|S_{21}|^2 \ (1 - |\Gamma_L|^2)}{(1 - |\Gamma_{in}|^2)|1 - S_{22} \ \Gamma_L|^2}$  G = 13.75  $G(dB) = 10 \ log_{10} \ (13.75)$   $G(dB) = 11.38 \ dB$ 

## b) Power delivered to the load , available power and incident power to the

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amplifier.

 $\boldsymbol{P}_{inc} = \frac{1}{2} \frac{|\boldsymbol{b}_{s}|^{2}}{|1 - \boldsymbol{\Gamma}_{in} \boldsymbol{\Gamma}_{s}|^{2}}$ 

 $P_{inc} = 0.0733 W$ 

$$P_{inc} (dBm) = 10 \log_{10} \left( \frac{P_{inc} (watts)}{1mW} \right)$$

$$P_{inc} (dBm) = 10 \log_{10} \left( \frac{0.0733}{1 \times 10^{-3}} \right)$$

 $P_{inc}$  (dBm) = 18.65 dBm

$$P_A = \frac{1}{2} \frac{|b_s|^2}{(1 - |\Gamma_s|^2)}$$
$$P_A = \frac{1}{2} \frac{(0.392)^2}{(1 - (-0.111)^2)}$$
$$P_A = 0.0778 \text{ W}$$

