

## 4.4 Code Provisions Design Of Steel Roof Truss

**Example:5**

Design a steel roof truss to suit the following data,

Span of the truss = 12m

Type of truss = pan type

Roof cover = Galvanization corrugated (GC) sheeting

Materials = Rolled steel angles

Spacing of roof truss = 5 m

Wind pressure =  $1 \text{ kN/m}^2$

Draw the elevation of the roof truss and the details of joints.

**Solution:**

**Step:1** Dimension of truss

$$\begin{aligned}\text{Central rise} &= \text{span}/4 \\ &= 12/4 \\ &= 3\text{m}\end{aligned}$$

Purlins are provided at intervals of 1.863m on the principal rafter

**Step:2** Dead loads

Self weight of GC sheeting per purlin at  $0.18 \text{ kN/m}^2$

$$= 0.18 \times 1.863$$

$$= 0.335 \text{ kNm}$$

Self weight of purlin at  $0.1 \text{ kN/m}$

$$= 0.10 \text{ kN/m}$$

Total dead load =  $0.435 \text{ kN/m}$

**Step:3** Live loads

$$\text{Slope of the truss} = 26^{\circ} 34'$$

Live load of the truss

$$= 0.75 - (10 \times 0.01 + 6.5 \times 0.02)$$

$$= 0.52 \text{ KN/m}^2$$

Live load per purlin per metre

$$= 0.52 \times 1.836 \times \cos 26^{\circ} 34'$$

$$= 0.87 \text{ KN}$$

**Step:4** Wind loads

$$F = (C_{pe} - C_{pi}) A p_d$$

$C_{pe}$  = external pressure coefficient

$C_{pi}$  = internal pressure coefficient

$A$  = Surface area of structural element or cladding unit

$p_d$  = design wind pressure

Slopping angle ,

$$\theta = 26^{\circ} 34'$$

$$C_{pe} = -0.7$$

$$C_{pi} = 0.2$$

$$F = (-0.7 - 0.2) p_d$$

$$= -0.9 p_d$$

$$= -0.9 \times 1$$

$$= -0.9 \text{ Kn/m}^2$$

Maximum wind load per purlin per metre

$$= (-0.9 \times 1.863 \times \cos 26^\circ 34')$$

$$= 1.5 \text{ KN}$$

**Step:5** Design of purlin

For continuous purlin, the max factored bending moment and shear force are computed as follow,

$$M = (1.5 \times 1.305 \times 5^2) / 10$$

$$= 4.89 \text{ KNm}$$

$$V = (1.5 \times 1.305 \times 5) / 2$$

$$= 4.9 \text{ KN}$$

Adopt ISA 100x75x8mm having section properties given below,

$$Z_x = (4.38 \times 10^4) \text{ mm}^3$$

$$D = 100 \text{ mm}$$

$$b = 75 \text{ mm}$$

$$t = 8 \text{ mm}$$

IS 800:2007 clause 3.7,

(a) Check for section classification is done by computed the ratios,

$$(b/t) = 75/8$$

$$= 9.37 < 9.4$$

Hence the section considered as plastic .

(b) Check for shear capacity

$$A_v = 100 \times 8$$

$$= 800 \text{ mm}^2$$

clause 8.4.1,

$$\begin{aligned} (A_v f_y w / \sqrt{3} \gamma_{mo}) &= (800 \times 250) / (\sqrt{3} \times 1.10 \times 10^3) \\ &= 105 \text{ KN} > 4.9 \text{ KN} \end{aligned}$$

The shear capacity of the section is very large compared to the applied shear force.

(c) Check for moment capacity

$$\begin{aligned} M_d &= (\beta_b Z_x f_y) / \gamma_{mo} \\ &= (1 \times 4.38 \times 10^4 \times 250) / (1.1 \times 10^6) \\ M_d &= 9.95 \text{ KNm} > 4.89 \text{ KNm} \end{aligned}$$

**Step:7** Load on truss

(a) Dead load

Sloping length of rafter,

$$\begin{aligned} AD &= \sqrt{(5^2 + 2.5^2)} \\ &= 5.59 \text{ m} \end{aligned}$$

Spacing of trusses = 5m c/c

Weight of GC sheeting on half truss ( plan area ) at 0.18 KN/m<sup>2</sup>

$$\begin{aligned} &= 5 \times 5 \times 0.18 \\ &= 4.5 \text{ KN} \end{aligned}$$

Weight of purlins (4nos) at 0.10 KN/m

$$\begin{aligned} &= 4 \times 0.1 \times 5 \\ &= 2 \text{ KN} \end{aligned}$$

$$\begin{aligned}
 \text{Self weight of roof truss} &= (\text{span}/300)+0.05 \\
 &= (10/300)+0.05 \\
 &= 0.083 \text{ KN/m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Weight of half roof truss} &= 0.083 \times 5 \times 5 \\
 &= 2.075 \text{ KN}
 \end{aligned}$$

$$\begin{aligned}
 \therefore \text{Total load on half truss} &= 4.5+2+2.075 \\
 &= 8.57 \text{ KN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Dead load on intermediate- panel point} \\
 &= 8.57/3 \\
 &= 2.85 \text{ KN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Dead load on end panel point} \\
 &= 2.85/2 \\
 &= 1.425 \text{ KN}
 \end{aligned}$$

(b) Live loads

$$\begin{aligned}
 \text{Live load on half truss} &= 0.52 \times 5 \times 5 \\
 &= 13 \text{ KN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Live load on intermediate panel point} \\
 &= 13/3 \\
 &= 4.3 \text{ KN}
 \end{aligned}$$

$$\begin{aligned}
 \text{Live load on end panel point} \\
 &= 4.3/2 \\
 &= 2.15 \text{ KN}
 \end{aligned}$$

## © Wind loads

Maximum wind load acting perpendicular to the sloping surface

$$= -0.9 \times 5 \times 5.59$$

$$= -25.155 \text{ KN}$$

Wind load on intermediate- panel point

$$= -(25.155/3)$$

$$= -8.38 \text{ KN}$$

Wind load on end panel point

$$= -(8.38/2)$$

$$= 4.19 \text{ KN}$$

**Step:8** Design of truss members

(a) Members AB, BC, CD

Maximum service load compressive force

$$= 36.17 \text{ KN}$$

Maximum factored compressive force

$$= 1.5 \times 36.17$$

$$= 54.25 \text{ KN}$$

Maximum service load tensile force

$$= 22.95 \text{ KN}$$

Maximum factored tensile force

$$= 1.5 \times 22.95$$

$$= 34.42 \text{ KN}$$

$$\text{Length (L)} = 1.863 \text{ m}$$

$$\text{Effective length (KL)} = 1.304\text{m}$$

Try two angle ISA 50x50x6mm placed back to back

$$\text{Area (A)} = 1136\text{mm}^2$$

Minimum radius of gyration

$$(\gamma_{\min}) = 15.1\text{mm}$$

$$\text{Slenderness ratio} = (KL/\gamma_{\min})$$

$$= 1304/15.1$$

$$= 86.3 < 180$$

Stress reduction factor  $\phi$  for column buckling class (c) corresponding to the slenderness

$$\text{ratio } 86.3 \text{ and } f_y = 250 \text{ N/mm}^2$$

$$\phi = 0.56$$

∴ Design compressive stress is computed as,

$$F_{cd} = \phi f_y / \gamma_{mo}$$

$$= (0.56 \times 250) / 1.25$$

$$= 112 \text{ N/mm}^2$$

Design compressive force is given by,

$$P_d = [A f_{cd}]$$

$$= (1136 \times 112) / 1000$$

$$= 127 \text{ KN} > 54.25 \text{ KN}$$

(b) Member DE

Maximum service load tension

$$= 12.83 \text{ KN}$$

Maximum factored load tension

$$= 1.5 \times 12.83$$

$$= 19.24 \text{ KN}$$

Maximum service load compression

$$= 9.57 \text{ KN}$$

Maximum factored load compression

$$= 1.5 \times 9.57$$

$$= 14.35 \text{ KN}$$

Effective length = 3m

Try a single angle ISA 50x50x5mm connected by 6mm thick gusset plate the junction with

two bolts of 16mm at 50mm.

$$\text{Gross area (A)} = 479 \text{ mm}^2$$

$$\gamma_{\min} = 15.2 \text{ mm}$$

Using 16mm dia bolts,

$$A_{nc} = [50 - 18] \times 5$$

$$= 160 \text{ mm}^2$$

$$A_{go} = [50 - 5] \times 5$$

$$= 225 \text{ mm}^2$$

$$A_g = 479 \text{ mm}^2$$

(a) Strength governed by rupture of critical section

$$T_{dn} = [0.9 A_{nc} f_y / \gamma_{mi}] + [\beta A_{go} f_y / \gamma_{mo}]$$

where,

$$\beta = 1.4 - 0.076(w/t)(f_y/f_u)(b_s/L_c)$$



$$= 1.4 - 0.076(50/5)(250/410)(50+25/50)$$

$$\beta = 0.70$$

$$T_{dn} = [0.9 \times 160 \times 410 / 1.25] + [0.7 \times 225 \times 250 / 1.10] \times 10^3$$

$$= 83.02 \text{ KN}$$

$$= T_0$$

(b) Strength governed by yielding of gross section

$$T_{dg} = A_g f_y / \gamma_{mo}$$

$$= (470 \times 250 \times 10^3) / 1.10$$

$$= 108.8 \text{ KN}$$

(c) Strength governed by block shear

$$A_{vg} = 5[50+50]$$

$$= 500 \text{ mm}^2$$

$$A_{vn} = 5[50+50] - [1.5 \times 18]$$

$$= 473 \text{ mm}^2$$

$$A_{tg} = [5 \times 25]$$

$$= 125 \text{ mm}^2$$

$$A_{tn} = [(5 \times 25) - (0.5 \times 18)]$$

$$= 116 \text{ mm}^2$$

The block shear strength is the smaller of the value of  $T_{db1}$  and  $T_{db2}$  as computed using

the equation given below,

$$T_{db1} = [A_{vg} f_y / \sqrt{3} \gamma_{mo}] + [0.9 A_{tn} f_u / \gamma_{mi}]$$

$$= [(500 \times 250) / (\sqrt{3} \times 1.1) + (0.9 \times 116 \times 410) / 1.25] \times 10^{-3}$$

$$= 99.92 \text{ KN}$$

$$T_{db2} = [0.9 A_{vn} f_u / \sqrt{3} \gamma_{mi}] + [A_{tg} f_y / \gamma_{mo}]$$

$$= [(0.9 \times 473 \times 410) / (\sqrt{3} \times 1.25) + (125 \times 250) / 1.10] \times 10^{-3}$$

$$= 109.12 \text{ KN}$$

Hence,  $T_{db} = 109.12 \text{ KN}$

The design shear strength is the least of the three value computed under (a)(b)(c) , which are 108.8 KN, 83.02KN, 109.12KN.

The design tensile strength of angle

$$= 83.02 \text{ KN} > 19.24 \text{ KN}$$

(C) Member BC ,EB

Service load compressive force

$$= 6.95 \text{ KN}$$

Factored compressive force

$$= 1.5 \times 6.95$$

$$= 10.42 \text{ KN}$$

Service load tensile force

$$= 6.38 \text{ KN}$$

Factored tensile force =  $1.5 \times 6.38$

$$= 9.57 \text{ KN}$$

Effective length (kL) =  $0.7 \times 1.6$

$$= 1.12 \text{ m}$$

Use minimum size angle ISA 50x50x5mm,

$$\text{Area (A)} = 479 \text{ mm}^2$$

$$\gamma_{\min} = 9.7 \text{ mm}$$

$$\begin{aligned} \text{Slenderness ratio } (\lambda) &= 1120/9.7 \\ &= 115 \end{aligned}$$

The stress reduction factor  $x$  corresponding to

$$f_y = 250 \text{ N/mm}^2 \text{ and}$$

$$\lambda = 115$$

$$x = 0.39$$

Design compressive stress is computed as,

$$\begin{aligned} f_{cd} &= x f_y / \gamma_{mo} \\ &= (0.39 \times 250) / 1.25 \\ &= 78 \text{ N/mm}^2 \end{aligned}$$

Design compressive force is given by ,

$$\begin{aligned} P_d &= A f_{cd} \\ &= [479 \times 78] / 1000 \\ &= 37.36 \text{ KN} > 10.42 \text{ KN} \end{aligned}$$

(d) Member EA and EF

Max service load tension

$$= 32.21 \text{ KN}$$

Factored tension = 1.5 x 32.21

$$= 748.31 \text{ KN}$$

Max service load compression

$$= 18.84 \text{ KN}$$

Factored compression

$$= 1.5 \times 18.84$$

$$= 28.26 \text{ KN}$$

Length of member = 3.33m

Effective length (kL) = 0.7 × 3.33

$$= 2.331 \text{ m}$$

Try minimum two angle ISA 50x50x6mm connect by guesst plate 6mm thick with two 16mm dia bolts spaced at 50mm

Area (A) = 2 × 598

$$= 113.6 \text{ mm}^2$$

$\gamma_{\min}$  = 15.1mm

i) Design strength due to yielding of cross section ,

$$T_{dj} = A_g f_y / \gamma_{mo}$$

$$= [(1136 + 250) / 1.10] \times 10^{-3}$$

$$= 258 \text{ KN}$$

(d) Member EA and EF

Max service load tension

$$= 32.21 \text{ KN}$$

Factored tension = 1.5 × 32.21

$$= 748.31 \text{ KN}$$

Max service load compression

$$= 18.84 \text{ KN}$$

$$\begin{aligned}\text{Factored compression} &= 1.5 \times 18.84 \\ &= 28.26 \text{ KN}\end{aligned}$$

$$\text{Length of member} = 3.33 \text{ m}$$

$$\begin{aligned}\text{Effective length (kL)} &= 0.7 \times 3.33 \\ &= 2.331 \text{ m}\end{aligned}$$

Try minimum two angle ISA 50x50x6mm connect by gusset plate 6mm thick with two 16mm dia bolts spaced at 50mm

$$\begin{aligned}\text{Area (A)} &= 2 \times 598 \\ &= 1196 \text{ mm}^2\end{aligned}$$

$$\gamma_{\min} = 15.1 \text{ mm}$$

i) Design strength due to yielding of cross section ,

$$\begin{aligned}T_{dj} &= A_g f_y / \gamma_{mo} \\ &= [(1196 \times 250) / 1.10] \times 10^{-3} \\ &= 271 \text{ KN}\end{aligned}$$

ii) Design strength governed by tearing at net section,

$$T_{dn} = \alpha A_n f_u / \gamma_{mi}$$

Assume a single line of 16mm dia bolts of two number spaced 50mm apart  $x=0.6$

$$\begin{aligned}A_n &= [(50-18)(6 \times 2)] \\ &= 384 \text{ mm}^2\end{aligned}$$

$$\begin{aligned}T_{dn} &= [(0.6 \times 384 \times 410) / 1.25] \times 10^{-3} \\ &= 75.5 \text{ KN} > 48.31 \text{ KN}\end{aligned}$$

Hence, the angle section designed for the truss can safely resist the factored loads.