

SHANNON–HARTLEY THEOREM

In information theory, the Shannon–Hartley theorem tells the maximum rate at which information can be transmitted over a communications channel of a specified bandwidth in the presence of noise. It is an application of the noisy channel coding theorem to the archetypal case of a continuous-time analog communications channel subject to Gaussian noise. The theorem establishes Shannon's channel capacity for such a communication link, a bound on the maximum amount of error-free digital data (that is, information) that can be transmitted with a specified bandwidth in the presence of the noise interference, assuming that the signal power is bounded, and that the Gaussian noise process is characterized by a known power or power spectral density. The law is named after Claude Shannon and Ralph Hartley.

$$C = B \log_2 \left(1 + \frac{S}{N} \right) = \frac{B \log_{10} \left(1 + \frac{S}{N} \right)}{\log_{10}(2)}$$

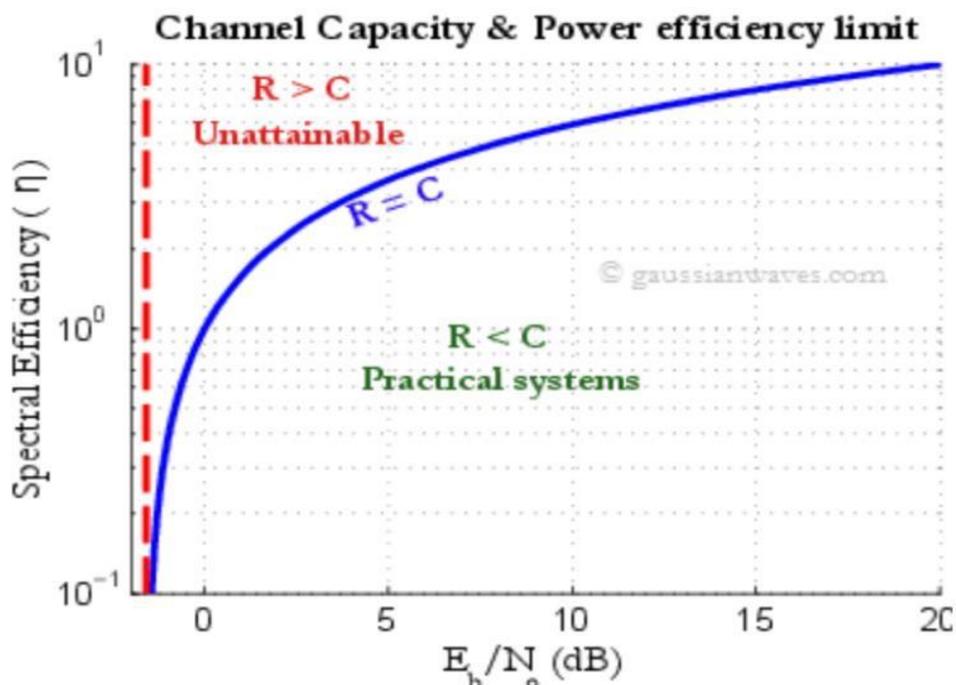


Fig 1.5 Shannon–Hartley Theorem

(Source:<https://www.google.com/search?q=Shannon%E2%80%93Hartley+Theorem&tbm>)

Considering all possible multi-level and multi-phase encoding techniques, the Shannon–Hartley theorem states the channel capacity C , meaning the theoretical tightest upper bound on the information rate (excluding error correcting codes) of clean (or arbitrarily low bit error rate) data that can be sent with a given average signal power S through an analog communication channel subject to

additive white Gaussian noise of power N , is:

$$C = B \log_2 \left(1 + \frac{S}{N} \right)$$

Where C is the channel capacity in bits per second;

B is the bandwidth of the channel in hertz (pass band bandwidth in case of a modulated signal);

S is the average received signal power over the bandwidth (in case of a modulated signal, often denoted C , i.e. modulated carrier), measured in watts (or volts squared);

N is the average noise or interference power over the bandwidth, measured in watts (or volts squared); and

S/N is the signal-to-noise ratio (SNR) or the carrier-to-noise ratio (CNR) of the communication signal to the Gaussian noise interference expressed as a linear power ratio (not as logarithmic decibels).

APPLICATION & ITS USES:

1. Huffman coding is not always optimal among all compression methods.
2. Discrete memory less channels.
3. To find 100% of efficiency using these codings.