

### 3.6 State Tables and State Diagrams

In this model the effect of all previous inputs on the outputs is represented by a state of the circuit. Thus, the output of the circuit at any time depends upon its current state and the input. These also determine the next state of the circuit. The relationship that exists among the inputs, outputs, present states and next states can be specified by either the state table or the state diagram. **State Table** The state table representation of a sequential circuit consists of three sections labelled present state, next state and output. The present state designates the state of flip-flops before the occurrence of a clock pulse. The next state shows the states of flip-flops after the clock pulse, and the output section lists the value of the output variables during the present state. **State Diagram** In addition to graphical symbols, tables or equations, flip-flops can also be represented graphically by a state diagram. In this diagram, a state is represented by a circle, and the transition between states is indicated by directed lines (or arcs) connecting the circles. An example of a state diagram is shown in Figure 3.6.1 below

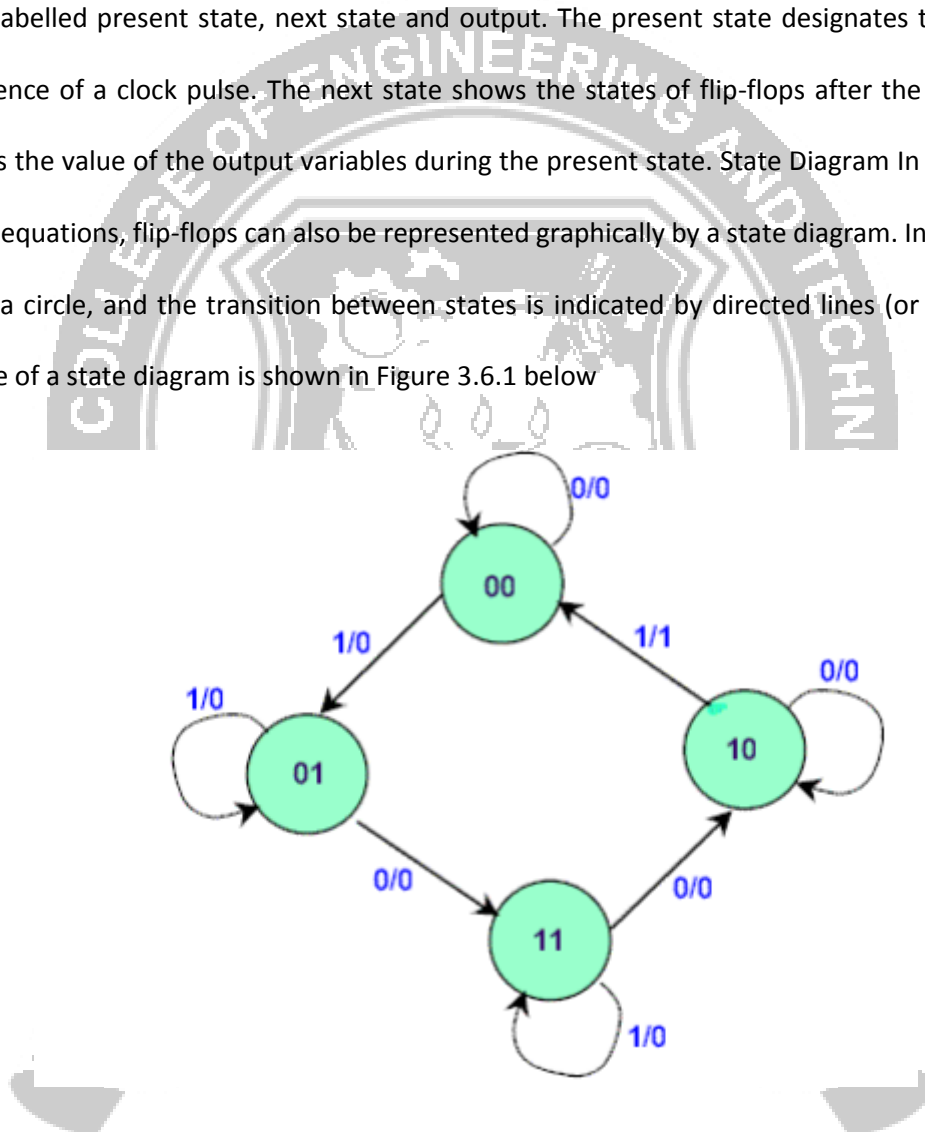


Fig 3.6.1 state diagram

The binary number inside each circle identifies the state the circle represents. The directed lines are labelled with two binary numbers separated by a slash (/). The input value that causes the state transition is labelled first. The number after the slash symbol / gives the value of the output. For example, the directed line from state 00 to 01 is labelled 1/0, meaning that, if the sequential circuit is in a present state and the input is 1, then the next state is 01

and the output is 0. If it is in a present state 00 and the input is 0, it will remain in that state. A directed line connecting a circle with itself indicates that no change of state occurs. The state diagram provides exactly the same information as the state table and is obtained directly from the state table. Consider a sequential circuit shown in Figure 4. It has one input  $x$ , one output  $Z$  and two state variables  $Q_1Q_2$  (thus having four possible present states 00, 01, 10, 11).

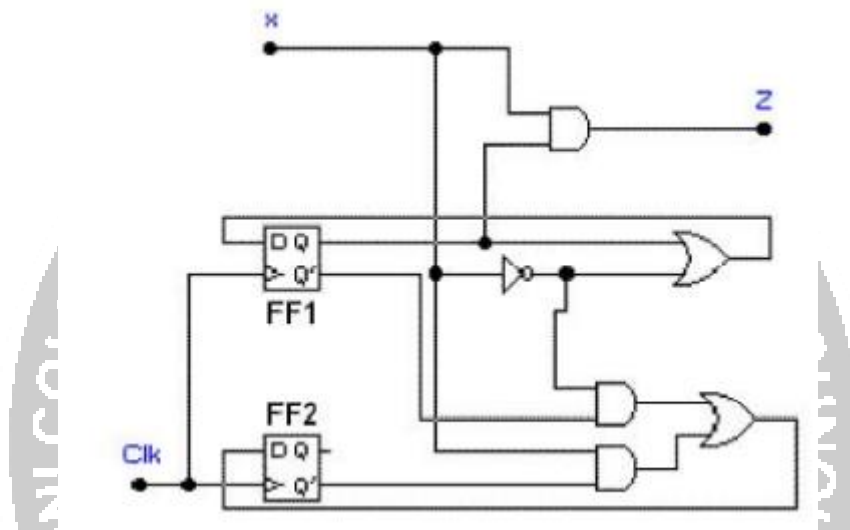


Fig 3.6.2 Sequential Circuit

The behaviour of the circuit is determined by the following Boolean expressions:  $Z = x * Q_1$   $D_1 = x' + Q_1$   $D_2 = x * Q_2' + x' * Q_1'$  These equations can be used to form the state table. Suppose the present state (i.e.  $Q_1Q_2$ ) = 00 and input  $x = 0$ . Under these conditions, we get  $Z = 0$ ,  $D_1 = 1$ , and  $D_2 = 1$ .

Thus the next state of the circuit  $D_1D_2 = 11$ , and this will be the present state after the clock pulse has been applied. The output of the circuit corresponding to the present state  $Q_1Q_2 = 00$  and  $x = 1$  is  $Z = 0$ . This data is entered into the state table as shown in Table 3.6.1.

Present State Q1Q2	Next State		Output	
	x = 0	x = 1	x = 0	x = 1
00	11	01	0	0
01	11	00	0	0
10	10	11	0	1
11	10	10	0	1

Table 3.6.1 State table

